

# Stellar winds from B supergiant stars: Exploring the $\delta$ -slow hydrodynamic solution



Roberto O. J. Venero

Institute of Astrophysics of La Plata  
(CONICET-UNLP)

Facultad de Ciencias Astronómicas y  
Geofísicas (FCAG)

La Plata National University (UNLP)

Argentina



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## The wind of rotating B supergiants – II. The $\delta$ -slow hydrodynamic regime

R. O. J. Venero<sup>1,2\*</sup>, M. Curé,<sup>3\*</sup> J. Puls,<sup>4</sup> L. S. Cidale,<sup>1,2\*</sup> M. Hauke,<sup>5</sup> I. Araya<sup>6</sup>,  
A. Gormaz-Matamala<sup>7,8,9</sup> and C. Arcos<sup>9</sup>

<sup>1</sup>Departamento de Espectroscopía, Facultad de Ciencias Astronómicas y Geofísicas, Universidad Nacional de La Plata, Paseo del Bosque S/N, BF1900FWA La Plata, Buenos Aires, Argentina  
<sup>2</sup>Instituto de Astrofísica de La Plata, CCT La Plata, CONICET-UNLP, Paseo del Bosque S/N, BF1900FWA La Plata, Buenos Aires, Argentina  
<sup>3</sup>Instituto de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 1111, Casilla 5030, Valparaíso, Chile  
<sup>4</sup>LMU München, University Observatory, Scheinerstr. 1, 81679 München, Germany  
<sup>5</sup>Facultad de Ingeniería, Universidad Nacional de La Plata, Av. 1 No. 750, B1900TAG La Plata, Buenos Aires, Argentina  
<sup>6</sup>Centro Multidisciplinario de Física, Vicerrectoría de Investigación, Universidad Mayor, 8580745 Santiago, Chile  
<sup>7</sup>Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, ul. Bartycka 18, 00-716 Warsaw, Poland  
<sup>8</sup>Departamento de Ciencias, Facultad de Artes Liberales, Universidad Adolfo Ibáñez, Av. Padre Hurtado 750, Viña del Mar, Chile  
<sup>9</sup>Instituto de Astrofísica, Facultad de Física, Pontificia Universidad Católica de Chile, 782-0436 Santiago, Chile

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### ABSTRACT

The theory of line-driven winds can explain many observed spectral features in early-type stars, though our understanding of the winds of B supergiants remains incomplete. The hydrodynamic equations for slowly rotating stellar winds predict two regimes based on the line-force parameter: the fast and the  $\delta$ -slow solution. In this paper, we aim to explore the capabilities of the latter

# B-type supergiant stars

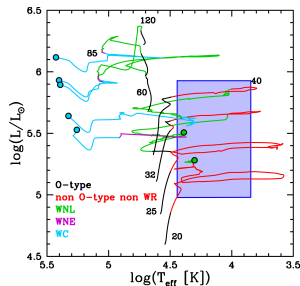
## Main properties

- Heterogeneous group of stars.
- Diversity of evolutionary phases (blue region  $\leftrightarrow$  red region of HR diagram).
- Photometric and spectroscopic variability.

## Fundamental parameters

- $8 M_{\odot} \lesssim \text{Mass} \lesssim 50 M_{\odot}$
- $10^{4,7} L_{\odot} \lesssim \text{Luminosity} \lesssim 10^{5,6} L_{\odot}$
- $12000 \text{ K} \lesssim T_{\text{eff}} \lesssim 25000 \text{ K}$
- $1.7 \lesssim \log g \lesssim 3$
- $20 R_{\odot} \lesssim \text{Radius} \lesssim 70 R_{\odot}$
- $v \sin i \lesssim 100 \text{ km s}^{-1}$

## Region of the HR diagram occupied by B-type supergiant stars



(Georgy+,2017)

# B-type supergiant stars

## Wind Parameters

- Mass-loss rates:

From  $\dot{M} \sim 10^{-7}$  to  $5 \times 10^{-6} M_{\odot} \text{ yr}^{-1}$

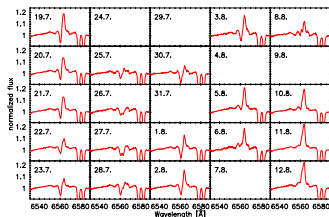
- Terminal velocities:

From  $v_{\infty} \sim 200 \text{ km s}^{-1}$  (late) to  $1500 \text{ km s}^{-1}$  (early)

*Optical depth invariant - Wind strength parameter*

$$\left\{ \begin{array}{ll} Q_{res} = \frac{\dot{M}}{R_* v_{\infty}^2} & \text{Resonance lines} \\ Q_{rec} = \frac{\dot{M}}{(R_* v_{\infty})^{1.5}} & \text{Recombination lines (H}\alpha\text{)} \end{array} \right.$$

## Spectral variability



H $\alpha$  line profiles of 55 Cygni (B3 Ia) from July to August 2013 (Haucke+, 2016).

# Rotating radiation-driven winds

## Equations for a rotating wind

1D symmetry in the equatorial plane.

Mass conservation:  $F_m = 4\pi r^2 \rho v = \text{constant}$

Momentum equation:  $v \frac{dv}{dr} = -\frac{1}{\rho} \frac{dp}{dr} - \frac{G M_*(1 - \Gamma)}{r^2} + \frac{v_\phi^2(r)}{r} + g^L \left( \rho, \frac{dv}{dr}, n_e \right)$

Energy equation  $\rightarrow$  Isothermal wind

### Centrifugal force

$$v_\phi^2/r = v_{\text{rot}}^2 R_*^2/r^3$$

$v_{\text{rot}}$  is the equatorial rotation speed

### Rotational rate $\Omega$

$$\Omega = v_{\text{rot}}/v_{\text{crit}} \quad 0 \leq \Omega < 1$$

$$v_{\text{crit}} = \sqrt{\frac{2GM_*}{3R_*}}$$

Maeder & Meynet (2000).

# Parameterization of the radiation force

## Castor, Abbott, & Klein (1975)

$$g_{rad}^L = \frac{\sigma_e F}{c} \mathcal{M}(t)$$

## Force multiplier

$$\mathcal{M}(t) = \sum_{lines} \frac{\Delta\nu_D F_\nu}{F} \frac{1}{t} (1 - e^{-\eta t})$$

$$\eta = \frac{\pi e^2}{m_e c} g_u f_{ul} \frac{n_l / g_l - n_u / g_u}{\rho \sigma_e \Delta\nu_D}$$

## Force multiplier (Abbott, 1982)

$$\mathcal{M}(t) = k t^{-\alpha} \left( \frac{n_e}{W(r)} \right)^\delta$$

with parameters  $k$ ,  $\alpha$  y  $\delta$

## Interpretation of parameters

- $k$  → Effective number of contributing lines for momentum
  - $\alpha$  → Slope of line intensity distribution
- $$dN(\nu, \kappa_L) = -N_0 f_\nu(\nu) \kappa_L^{\alpha-2} d\nu d\kappa_L$$
- $\delta$  → changes in ionization along the wind

## Line-force parameters

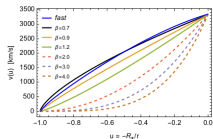
$T_{eff}$ [K]	$\log g$	$k$	$\alpha$	$\delta$	Fuente
10 000	1.5	0.36	0.54	0.05	A82
15 000	2.0	0.26	0.51	0.12	A82
20 000	2.5	0.32	0.56	0.02	P86
30 000	3.5	0.17	0.59	0.09	P86

A82: Abbott(1982) - P86: Pauldrach+(1986)

# Hydrodynamic solutions

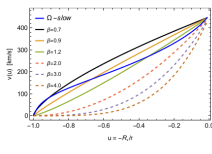
## Fast Solution

- Classical ( $\sim$ m-CAK) solution
- High values of the terminal velocity
- $\Omega < 0.75$  (slow rotators)



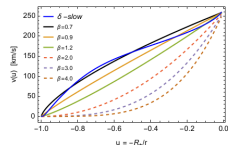
## $\Omega_{\text{slow}}$ solution

- Found by Curé (2004)
- $\Omega > 0.75$  (high rotators)
- Low terminal velocities and dense flows



## $\delta_{\text{slow}}$ solution

- Found by Curé et al. (2011)
- For high values of parameter  $\delta$  (changes in ionization)
- Low terminal velocities and dense flows



Figures from Curé & Araya (2023)  
 O5V star with  $T_{\text{eff}} = 45\,000$  K,  
 $\log g = 4.0$ ,  $R/R_{\odot} = 12$

# Hydrodynamic solutions

## $\beta$ -velocity law

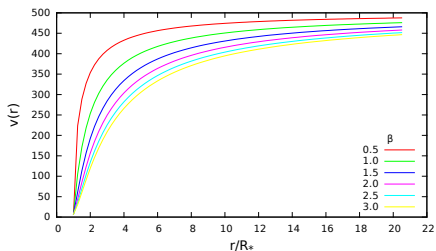
Approximation to the hydrodynamic solution

$$v(r) = v_{\infty} \left(1 - b \frac{R_*}{r}\right)^{\beta}$$

with

$$b = 1 - \left(\frac{v(R_*)}{v_{\infty}}\right)^{\frac{1}{\beta}}$$

This velocity law is commonly used with  $\beta$  values of 2, 3 or higher, particularly in B supergiants.





## Questions to answer

What hydrodynamic solutions can we use to model the wind of supergiants B?

Most of B-type supergiants are not fast rotators ( $\Omega \leq 0.6$ )

i.e.: Howarth(2004), Hunter+(2008), Vink+(2010), de Burgos+(2023)

We can rule out the  $\Omega_{\text{slow}}$  solution

We can choose between *fast* and  $\delta_{\text{slow}}$  solutions

### Questions

- In what cases does each solution appear? Can the **domains of each solution** be delimited in the space of the radiation force parameters?
- Can the wind of **B-type supergiants** be effectively **modeled** using  $\delta_{\text{slow}}$  solutions?
- Could the transition between one solution and another explain the **variability** observed in the spectrum?

# Calculation of wind models

## Option 1

Self-consistent models

## Input values

$T_{\text{eff}}$ ,  $\log g$ ,  $R_*$ , abundances,  $\Omega$ .

## Method

- 1) Solving hydrodynamic equations and radiation transport in moving media, including radiative acceleration calculated consistently with NLTE rates.
  - 2) Generating the synthetic spectrum.
  - 3) Comparison with observations.
  - 4) Iterative refinement process.
- Mostly for O-type and WR stars.

Pauldrach+(1994), Krtićka & Kubát(2001, 2017),  
Sander+(2017), Sundqvist+(2019), Björklund+(2021),  
Poniatowski+(2021,2022).

## Option 2

Partially consistent models

## Input values

$T_{\text{eff}}$ ,  $\log g$ ,  $R_*$ ,  $\Omega$ , abundances,  $\alpha$ ,  
 $\delta$ ,  $k$ .

## Method

- 1) Solving the hydrodynamic equations adopting a parameterization for the radiative acceleration.
- 2) Solving the radiation transport equation for moving media, using the hydrodynamic solution.
- 3) Generating the synthetic spectrum.
- 4) Comparison with observations.
- 5) Iterative refinement process.

Taresch+(1997), Pauldrach+(2001), Noebauer &  
Sim(2015), Lattimer & Cranmer(2021)

## Option 3

Non-consistent models

## Input values

$T_{\text{eff}}$ ,  $\log g$ ,  $R_*$ ,  $\Omega$ , abundances,  $\beta$ ,  
 $M$ ,  $v_{\infty}$ .

## Method

- 1) Employing a  $\beta$  velocity law instead of solving the hydrodynamic equations.
- 2) Solving the radiation transport equation for moving media, using the  $\beta$  law.
- 3) Obtaining the synthetic spectrum.
- 4) Comparison with observations.
- 5) Process iteration.

Crowther+(2006), Markova & Puls(2008),  
Searle+(2008), Haucke+(2018)

# Calculation codes

We choose [option 2](#) because, currently, there are no self-consistent codes that produce the  $\delta_{\text{slow}}$  solution.

## Hydrodynamic equations

### HYDWIND

Curé and collaborators (Univ. Valparaíso, Chile)

#### Basic features

- Input: Fundamentales parameters,  $\Omega$ ,  $k$ ,  $\alpha$  y  $\delta$ .
- Spherical Symmetry - Equatorial plane
- Inner boundary condition adopted:

$$\int_{R_*}^{\infty} \sigma_{\epsilon} \rho(r) dr = 2/3 \text{ or } \rho(R_*) = \rho_*$$

- Execution time: few minutes.
- It gives *fast*,  $\Omega_{\text{slow}}$ , or  $\delta_{\text{slow}}$  solutions.
- Output: radial grid, velocities and densities for the wind.

## Radiative transfer

### FASTWIND

Puls and collaborators (LMU Munich)

#### Basic features

- Input: Fundamental parameters, hydro solution (or  $\beta$ ,  $v_{\infty}$ ,  $\dot{M}$ ).
- Spherical Symmetry.
- NLTE code considering *line blanketing*.
- Radiative transfer in Sobolev approximation and CMF.
- Unified model (photosphere + wind).
- Diagnostic range: optical.
- Execution time: 15 - 30 min.
- Output: continuum radiation distribution + line profiles (H, He, Si, C, N, O).

# Most suitable $\delta$ values for B-type supergiants

$\delta$   
values  
for  
BSGs

Do values of  $\delta$  higher than  $\sim 0.25$  exist in a stellar wind to achieve a  $\delta_{\text{slow}}$  solution?

Early calculations indicate  $\delta \lesssim 0.12$  (Abbott, 1982; Pauldrach+. 1986).

Most recent non-LTE calculations for line-force parameters assume the material to be 'frozen in ionization' ( $\delta = 0$ ), e.g. Noebauer & Sim(2015), Lattimer & Cranmer (2021), or are limited to O-type supergiants (Gormaz-Matamala+2019,2022).

Puls, Springmann & Lennon (2000) analytically derived  $\delta \gtrsim 1/3$  for a medium composed of neutral hydrogen as a trace element.

Kudritzki (2002) demonstrated that  $\delta \sim 1$  for winds of low optical depth and very low metallicity.

**We postulate that BSGs have a different ionization structure compared with O-type stars.**

# Solution domains in $\delta$ and $\Omega$ space

First, we examine the distribution of solution domains based on the values of the line-force parameters ( $k$ ,  $\alpha$ ,  $\delta$ ).

## Model T19

$$T_{\text{eff}} = 19 \text{ kK}$$

$$\log g = 2.50$$

$$R_* = 40 R_{\odot}$$

S. Type:  $\sim$  B2 I

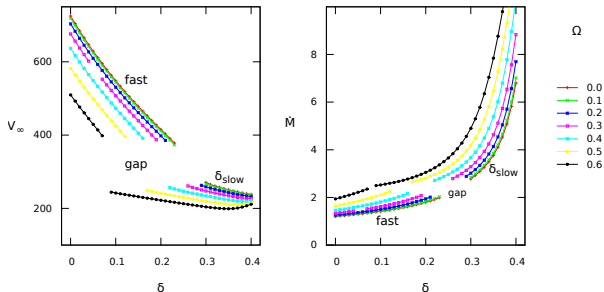
$$\alpha = 0.5$$

$$k = 0.32$$

$$[\dot{M}] \equiv 10^{-6} M_{\odot} \text{ yr}^{-1}$$

$$[v_{\infty}] \equiv \text{km s}^{-1}$$

## Distribution of solutions



There exists a distinct **gap** between *fast* and  $\delta_{\text{slow}}$  solutions. The HYDWIND code does not identify any stationary solution within the gap.

The gap is consistently present in all models, regardless of the values of  $T_{\text{eff}}$ ,  $\log g$ , or  $\Omega$ .

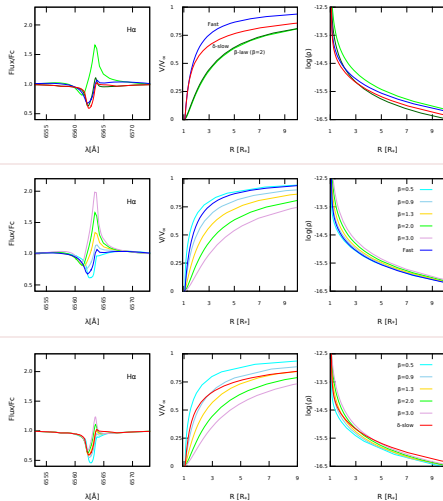
# Line profiles from different wind regimes

## H $\alpha$ line profiles

Comparison of line profiles from *fast* and  $\delta_{\text{slow}}$  models with those from the  $\beta$  velocity law.

The models have nearly identical values of  $Q$ .

The H $\alpha$  profiles generated by the *fast* and  $\delta_{\text{slow}}$  regimes are quite similar.



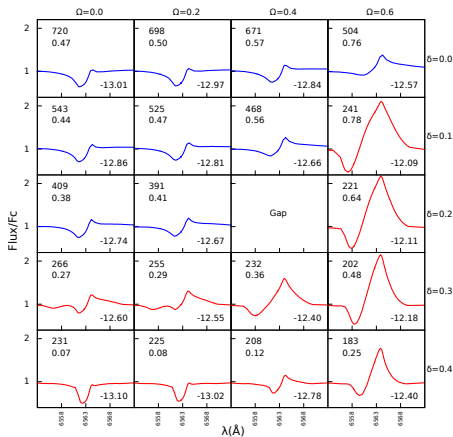
# H $\alpha$ line profiles

## H $\alpha$ line profiles for different wind regimes (model T19)

### Dependence of H $\alpha$ on $\Omega$ and $\delta$

Sample of H $\alpha$  line profiles for model T19.

Terminal velocities and mass-loss rates [in units of  $10^{-6} M_{\odot} \text{ yr}^{-1}$ ]. The values of log Q are at bottom right.



# Comparison with observations

Previous work by Haucke et al. (2018)  
H $\alpha$  line profile fittings computed with  $\beta$   
velocity laws.

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Astronomy  
Astrophysics

### Wind properties of variable B supergiants

Evidence of pulsations connected with mass-loss episodes\*

M. Haucke<sup>1,2</sup>, L. S. Cidale<sup>1,3</sup>, R. O. J. Venero<sup>1,4</sup>, M. Cas<sup>5</sup>, M. Kesz<sup>6</sup>, S. Kamae<sup>7</sup>, and C. Acero<sup>8</sup>

<sup>1</sup>Departamento de Experimentación, Facultad de Ciencias Astronómicas y Geofísicas, Universidad Nacional de La Plata, Paseo del

Trilce 455, La Plata, Argentina

<sup>2</sup>Consejo Nacional de Investigaciones Científicas, CONICET, Ciudad Universitaria, La Plata, Argentina

<sup>3</sup>Instituto de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 111, Casilla 3600, Valparaíso,

Chile

<sup>4</sup>Observatorio Astronómico de La Plata, UNLP, Calle 47, 1900 La Plata, Argentina

<sup>5</sup>San Observatorio, Turismo, INTA, Buenos Aires, Argentina

<sup>6</sup>San Observatorio, Turismo, INTA, Buenos Aires, Argentina

<sup>7</sup>San Observatorio, Turismo, INTA, Buenos Aires, Argentina

<sup>8</sup>San Observatorio, Turismo, INTA, Buenos Aires, Argentina

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### ABSTRACT

Context. Variable B supergiants (VBs) constitute a heterogeneous group of stars with complex photometric and spectroscopic behavior. They exhibit mass-loss variations and experience different types of outburst events, and show a growing evidence for magnetic field and magnetospheric activity-related signals.

Aims. We study the wind properties and variability of VBs stars, we derive new  $\beta$  velocity laws and wind parameters for a sample of 16 VBs stars by fitting observed H $\alpha$  profiles with  $\beta$  and  $\beta$  velocity laws, and compare them with previous literature data.

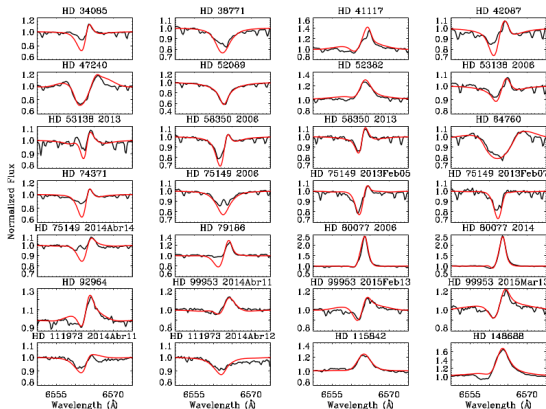
Methods. The stellar line profiles are compared with the new local homogeneous equilibrium (LH) atmosphere code (LH), which is able to solve the hydrodynamic equations.

Results. The new line sets of  $\beta$  velocity laws have been derived for the first time. The global properties of  $\beta$  velocity laws in VBs stars are well represented by  $\beta$  law with  $\beta = 2.0$  to  $\beta = 3.0$  for the two temperature wind structure, however, larger values of  $\beta$  are found for the  $\beta$  law. The  $\beta$  law parameters are related to the stellar mass, radius, and surface gravity. The  $\beta$  law parameters are also related to the stellar mass, radius, and surface gravity. The  $\beta$  law parameters are also related to the stellar mass, radius, and surface gravity.

Conclusions. The results also suggest that stellar pulsations are well correlated with mass-loss episodes. The  $\beta$  law parameters are also related to the stellar mass, radius, and surface gravity. The  $\beta$  law parameters are also related to the stellar mass, radius, and surface gravity.

Keywords. stars: early-type – supergiants – mass transfer – mass loss, winds

1. Introduction  
Massive stars have a significant impact on the local environment, and are one of the most important sources of ionizing radiation, and one of the most important sources of ionizing radiation, and one of the most important sources of ionizing radiation.





# Comparison with observations

Star	Spectral type	$T_{\text{eff}}$ (kK)	$\log g$ (dex)	$R_*$ ( $R_{\odot}$ )	$\log LL_{\odot}$ (dex)	$v \sin i$ ( $\text{km s}^{-1}$ )	$v_{\text{rot}}$ ( $\text{km s}^{-1}$ )	$v_{\text{mic}}$ ( $\text{km s}^{-1}$ )	$v_{\text{mac}}$ ( $\text{km s}^{-1}$ )
HD 47240	B1 Ib	19.0	2.40	30	5.02	95	122	10	60
HD 99953	B1/2 Iab/b	19.0	2.30	25	4.87	50	64	18	50
HD 41117	B2 Ia	19.0	2.30	23	4.79	40	51	10	65
HD 80077	B2 Ia + e	17.7	2.20	195	6.53	10	13	10	10*
HD 92964	B2.5 Ia	18.0	2.20	70	5.67	45	58	11	40
HD 53138	B3 Ia	18.0	2.25	46	5.30	40	51	10	80*
HD 75149	B3 Ia	16.0	2.10	61	5.34	40	51	11	52
HD 42087	B4 Ia	16.5	2.45	55	5.31	80	103	15	80
HD 58350	B5 Ia	15.0	2.00	54	5.12	40	51	12	70
HD 79186	B5 Ia	15.8	2.00	61	5.32	40	51	11	53
HD 74371	B6 Iab/b	13.7	1.80	73	5.23	30	39	10	60
HD 34085	B8 Iae	12.7	1.70	72	5.08	30	39	10	52

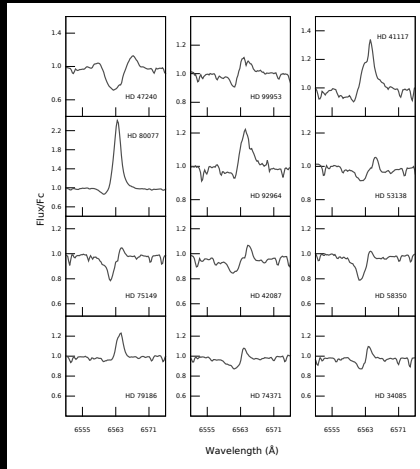
We adopt the stellar parameters from Haucke et al. (2018)

## Comparison with observations

### H $\alpha$ line profiles

Observations were performed at CASLEO using the REOSC spectrograph (2005-2015).

A subsample of stars was selected based on the presence of emission in the H $\alpha$  line profile.

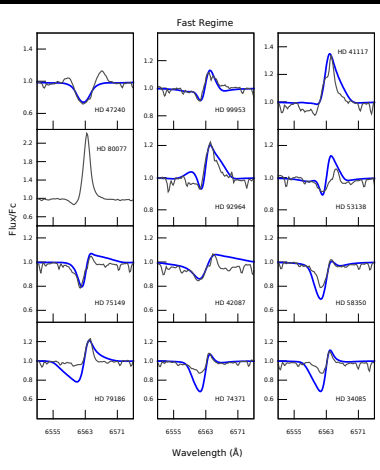


## Comparison with observations

### H $\alpha$ line profiles

#### Fast regime fittings

When fitting the line profiles, we primarily focus on adjusting the emission component of the P Cygni profile.



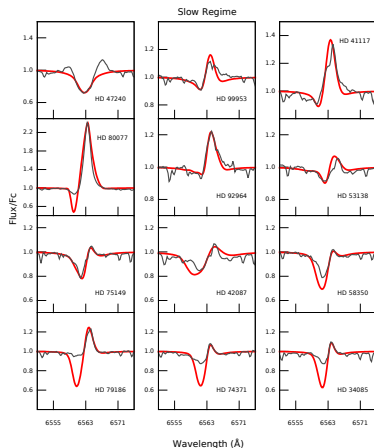
## Comparison with observations

### H $\alpha$ line profiles

$\delta_{\text{slow}}$  regime fittings

The wings appear slightly improved compared to the *fast* case.

However, many absorption components are still too deep.

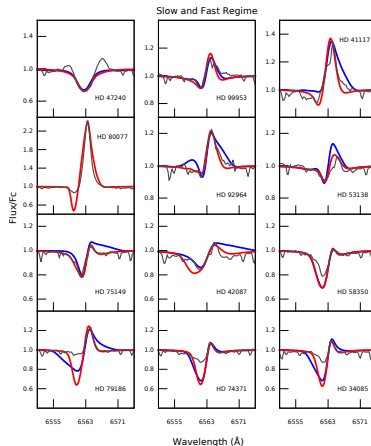


## Comparison with observations

### H $\alpha$ line profiles

There are no significant differences between the H $\alpha$  fittings for both the *fast* and  $\delta_{\text{slow}}$  regimes.

H $\alpha$   
dichotomy



# Wind parameters from fittings

## Fast regime

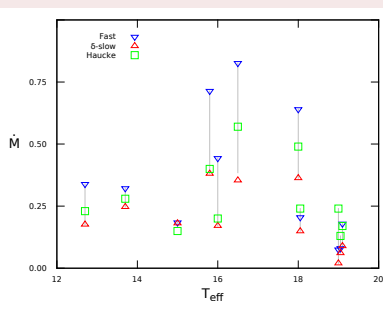
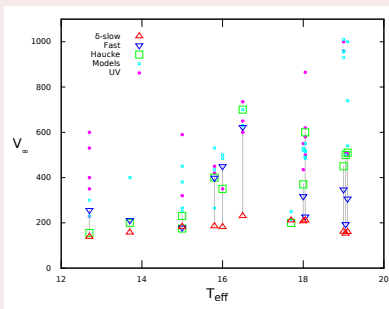
Star	$\Omega$	$v_{\text{crit}}$	$v_{\infty}$	$\dot{M}$	$k$	$\alpha$	$\delta$	$\log D_{\text{mom}}$
HD 47240	0.55	222.5	347.2	0.075	0.070	0.500	0.000	26.96
HD 99953	0.33	191.7	193.8	0.080	0.090	0.494	0.150	26.69
HD 41117	0.27	183.9	306.9	0.179	0.113	0.520	0.000	27.22
HD 80077	0.03	470.0	—	—	—	—	—	—
HD 92964	0.20	287.1	317.5	0.640	0.120	0.500	0.200	28.03
HD 53138	0.21	238.8	227.5	0.205	0.190	0.420	0.170	27.30
HD 75149	0.23	224.8	450.1	0.443	0.155	0.480	0.000	27.99
HD 42087	0.35	290.7	622.8	0.826	0.530	0.420	0.000	28.38
HD 58350	0.27	187.5	179.0	0.184	0.240	0.420	0.170	27.18
HD 79186	0.24	209.2	399.1	0.714	0.140	0.510	0.000	28.15
HD 74371	0.22	176.8	211.9	0.323	0.190	0.450	0.120	27.57
HD 34085	0.25	154.0	256.3	0.339	0.150	0.500	0.050	27.67

## $\delta_{\text{slow}}$ regime

Star	$\Omega$	$v_{\text{crit}}$	$v_{\infty}$	$\dot{M}$	$k$	$\alpha$	$\delta$	$\log D_{\text{mom}}$	$v_{\infty}^{\text{Hal}^{\text{B}}}$	$\dot{M}^{\text{Hal}^{\text{B}}}$	$\beta^{\text{Hal}^{\text{B}}}$	$\log D_{\text{mom}}^{\text{Hal}^{\text{B}}}$
HD 47240	0.55	222.5	161.3	0.020	0.090	0.500	0.300	26.04	450	0.24	1	27.57
HD 99953	0.33	191.7	152.5	0.061	0.080	0.530	0.320	26.47	500	0.13	2	27.33
HD 41117	0.27	183.9	160.0	0.089	0.095	0.510	0.240	26.63	510	0.17	2	27.38
HD 80077	0.03	470.0	211.0	6.379	0.606	0.300	0.295	29.07	200	5.4	3.2	28.86
HD 92964	0.20	287.1	207.0	0.363	0.130	0.505	0.350	27.60	370	0.49	2	27.98
HD 53138	0.21	238.8	211.2	0.149	0.090	0.550	0.320	27.13	600	0.24	2	27.79
HD 75149	0.23	224.8	181.6	0.171	0.185	0.480	0.310	27.18	350	0.2	2.5	27.54
HD 42087	0.35	290.7	230.4	0.354	0.452	0.480	0.405	27.58	700	0.57	2	28.27
HD 58350	0.27	187.5	182.5	0.181	0.120	0.550	0.290	27.18	233	0.15	3	27.21
HD 79186	0.24	209.2	185.3	0.381	0.110	0.550	0.300	27.54	400	0.4	3.3	27.90
HD 74371	0.22	176.8	157.6	0.247	0.163	0.501	0.270	27.32	155	0.23	2.6	27.22
HD 34085	0.25	154.0	138.5	0.176	0.180	0.500	0.280	27.11	155	0.23	2.6	27.22

# Comparison with values from previous works

Comparison of terminal velocities and mass loss rates as a function of effective temperature.

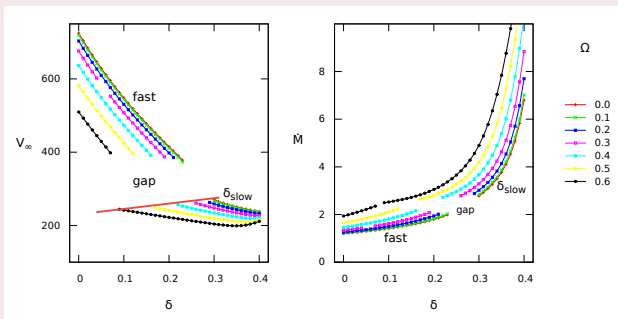


Models & UV points were taken from literature.

- Generally, the  $\delta_{\text{slow}}$  solution yields the lowest values for the wind parameters.
- The *fast* solution provides values greater than those predicted by the  $\beta$  law.
- The measured values of  $v_{\infty}$  (UV) exceed those obtained by all models.

# Solution domains in $\delta$ and $\Omega$ space

## Upper limit for terminal velocities in the $\delta$ -slow solution



The existence of a **gap** between *fast* and  $\delta_{slow}$  solutions, puts an upper limit on the terminal velocities of the  $\delta_{slow}$  solution.



# Conclusions

## Domains of hydrodynamic solutions

- We determined the **domains** of hydrodynamic solutions. The *fast* and  $\delta_{\text{slow}}$  regimes are separated by a **gap** where no stationary solutions were found using the available codes.
- **Rotation** affects the distribution of domains.

## Line profiles

- For the first time, we have **fitted synthetic line profiles** computed with the hydrodynamic solution  $\delta_{\text{slow}}$  to observed ones for B supergiant stars.
- $H\alpha$  line profiles can be fitted with **both** *fast* and  $\delta_{\text{slow}}$  models.
- The  $\delta_{\text{slow}}$  solution could be suitable for modeling the winds of **certain** B supergiants.
- However, this solution is constrained by the **maximum terminal velocity**. Consequently, it cannot account for the measured (or estimated)  $v_{\infty}$  values in the UV for B supergiants.

## Future work

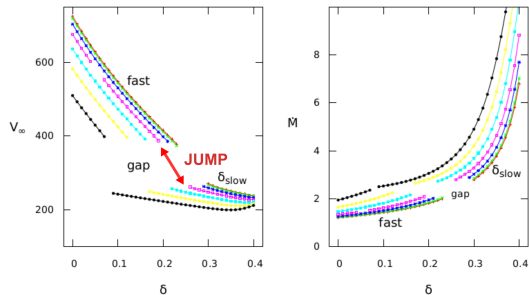
- $H\alpha$  may not be the most suitable line for determining the most appropriate wind regime. A **multiwavelength analysis** is required.
- This study analyzed only 12 stars. A **larger sample** is needed.
- Since the only hypergiant B in the sample was fitted exclusively with the  $\delta_{\text{slow}}$  solution, a sample of **hypergiants B** should be studied.

# Discussion

## The gap and the variability

- A change in wind regime can occur as a result of variations in  $\delta$ .
- A higher rotational rate  $\Omega$  reduces the required change in  $\delta$  to transition between regimes.
- Could these changes in regime be due to binaries or stellar pulsations?

## Jumping the gap



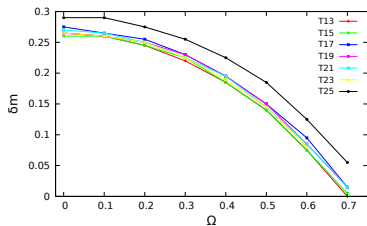


# The End



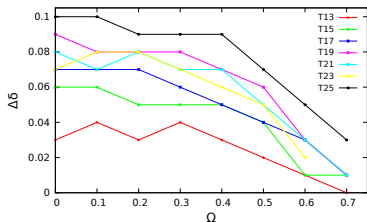
# Gap Properties

## Gap location



- $\delta_m$  represents the average value of  $\delta$  across the edges of the gap.
- The location of the gap is almost independent of  $T_{\text{eff}}$ .
- For B supergiants exhibiting higher rotation rates, the gap is located at small values of  $\delta$ .

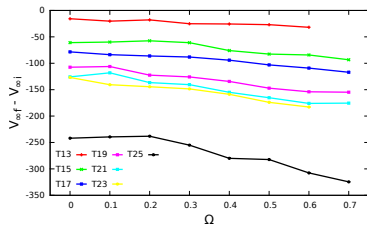
## Gap width



- $\Delta\delta$  is the width of the gap in  $\delta$  values.
- The width decreases as  $\Omega$  increases.
- Gaps are narrower in models with lower  $T_{\text{eff}}$ .

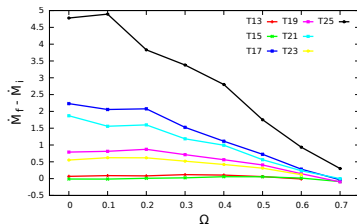
# Gap Properties

## Jump in $v_\infty$



- There is little to no change in  $v_\infty$  for low  $T_{\text{eff}}$ .
- The jump increases in magnitude for faster rotators.

## Jump in $\dot{M}$



- The jump in  $\dot{M}$  is smaller for larger rotators.
- $\dot{M}$  can double its value if changes in  $\delta$  result in crossing the gap.

# Interaction between $k$ and $\delta$ , and the wind parameters

## Model T19

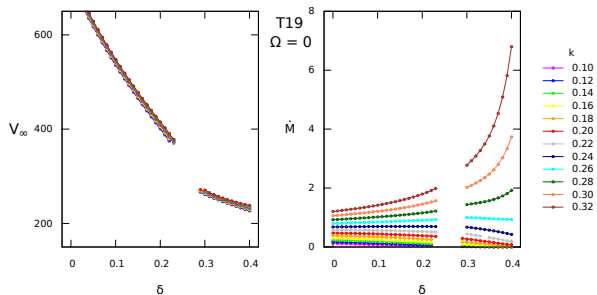
$$\alpha = 0.5$$

$$\Omega = 0$$

The value of  $v_\infty$  remains unchanged when different values of  $k$  are considered.

There is no change in the position or width of the gap (in  $\delta$  space).

## Dependence of solutions on the parameter $k$

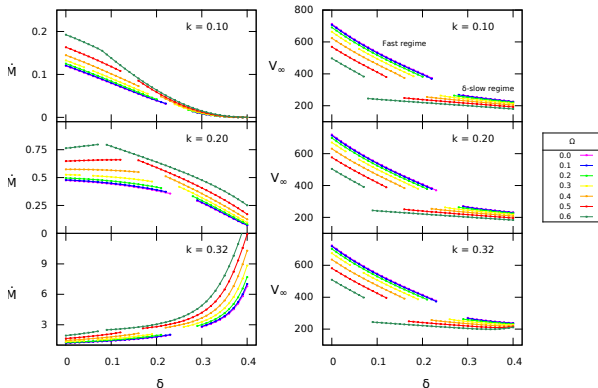


# Interaction between $k$ and $\delta$ , and the wind parameters

## Dependence of solutions on the parameter $k$

### Model T19

The change in the slope of  $\dot{M}$  as a function of  $\delta_{\text{slow}}$  for  $k = 0.1, 0.2, \text{ and } 0.32$ . In contrast, the slope in  $v_\infty$  does not change.





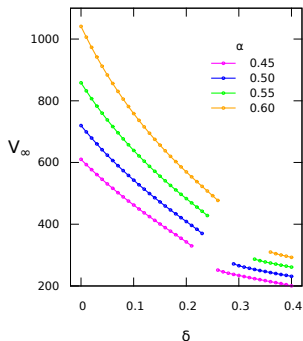
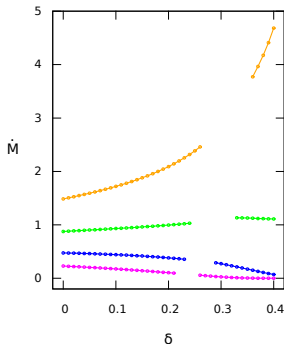
## Interaction between $\alpha$ and $\delta$ , and the wind parameters

### Model T19

In contrast to the parameter  $k$ ,  $\alpha$  completely modifies the terminal velocities.

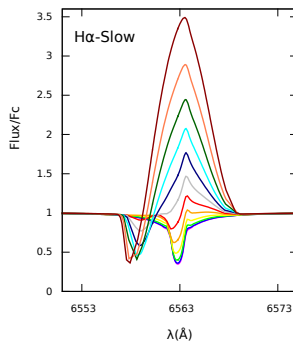
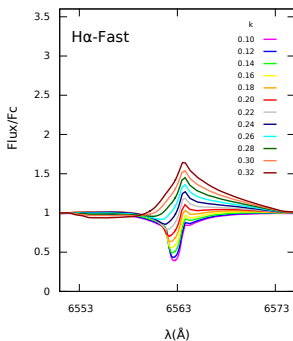
$\dot{M}$  is also highly sensitive to this parameter.

Changing the value of  $\alpha$  also alters the gap in  $\delta$ .



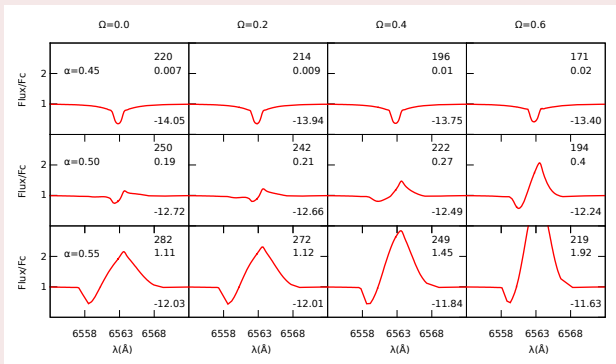
# H $\alpha$ line profiles

## H $\alpha$ line dependence on the parameter $k$



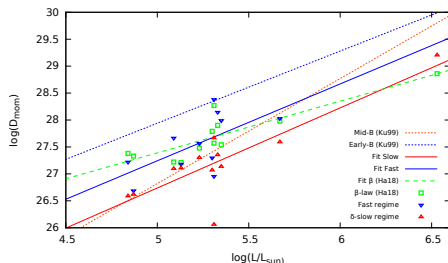
# H $\alpha$ line profiles

H $\alpha$  line dependence on the parameter  $\alpha$



# Discussion

## Wind momentum - Luminosity relation



- The WLR based on the  $\delta_{\text{slow}}$  solution models is close to the empirical behaviour of the mid-B supergiants (Kudritzki+,1999).
- The WLR based on the *fast* solution is in better agreement with the results from Haucke+(2018) using a  $\beta$ -law.
- Both relations show a considerable dispersion.

## Linear regressions

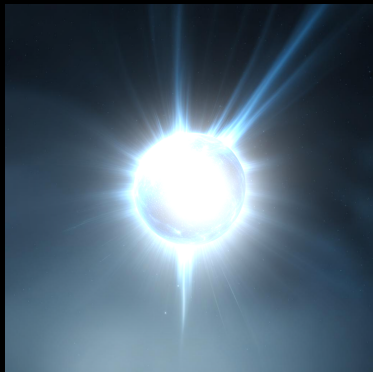
$\delta_{\text{slow}}$  regime

$$\log D_{\text{mom}} = 1,48 \log L/L_{\odot} + 19,30$$

*fast* regime

$$\log D_{\text{mom}} = 1,43 \log L/L_{\odot} + 20,11$$

# Stellar winds from B supergiant stars: Exploring the $\delta$ -slow hydrodynamic solution



**Roberto O. J. Venero**

IALP (CONICET-UNLP) - FCAG (UNLP) - Argentina

B-type supergiant stars are a heterogeneous group of objects with strong stellar winds. The hydrodynamic equations for rotating radiation-driven winds predict three kinds of solutions. In this presentation, we evaluate the “ $\delta$ -slow” solution for the first time, in predicting the  $H\alpha$  line profile for B supergiants.

The observed  $H\alpha$  line can be reproduced by both “fast” and “ $\delta$ -slow” hydrodynamic wind regimes with similar precision. These findings raise a dichotomy, because mass-loss rates and terminal velocities for each solution are quite different.

However, the “ $\delta$ -slow” solution predicts maximum values for  $v_\infty$  that are systematically lower than those measured in the ultraviolet. Multiwavelength analyses and a larger sample of stars are needed to reach a definitive conclusion.