

STELLAR ATMOSPHERE AND HYDRODYNAMIC MODELING: **ISOSCELES V2.0**

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In collaboration with

Michel Curé (Universidad de Valparaíso)

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Catalina Arcos (Universidad de Valparaíso)

and many others...



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Physics of Extreme
Massive Stars

Marie-Curie-RISE project
funded by the European Union



Physics of Extreme Massive Stars
25 June, 2024
Rio de Janeiro, Brazil

A quick introduction

Michel Curé's talk...

Momentum Equation

Radial Coordinate: r Time: t Density: ρ Velocity: v

$$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial r} = -\frac{a^2}{\rho} \frac{\partial \rho}{\partial r} - \frac{G M (1 - \Gamma_E)}{r^2} + \frac{v_\phi^2}{r} + g_{\text{rad}}^{\text{line}}$$

Inertia (points to $\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial r}$)

Gas Pressure (points to $-\frac{a^2}{\rho} \frac{\partial \rho}{\partial r}$)

Gravity (points to $-\frac{G M (1 - \Gamma_E)}{r^2}$)

Centrifugal Force (points to $\frac{v_\phi^2}{r}$)

Line Force (points to $g_{\text{rad}}^{\text{line}}$)

$$v_\phi = v_{\text{rot}}(\theta) R_* / r$$

$a = \text{sound speed}$

Line-Force Parameters

M-CAK

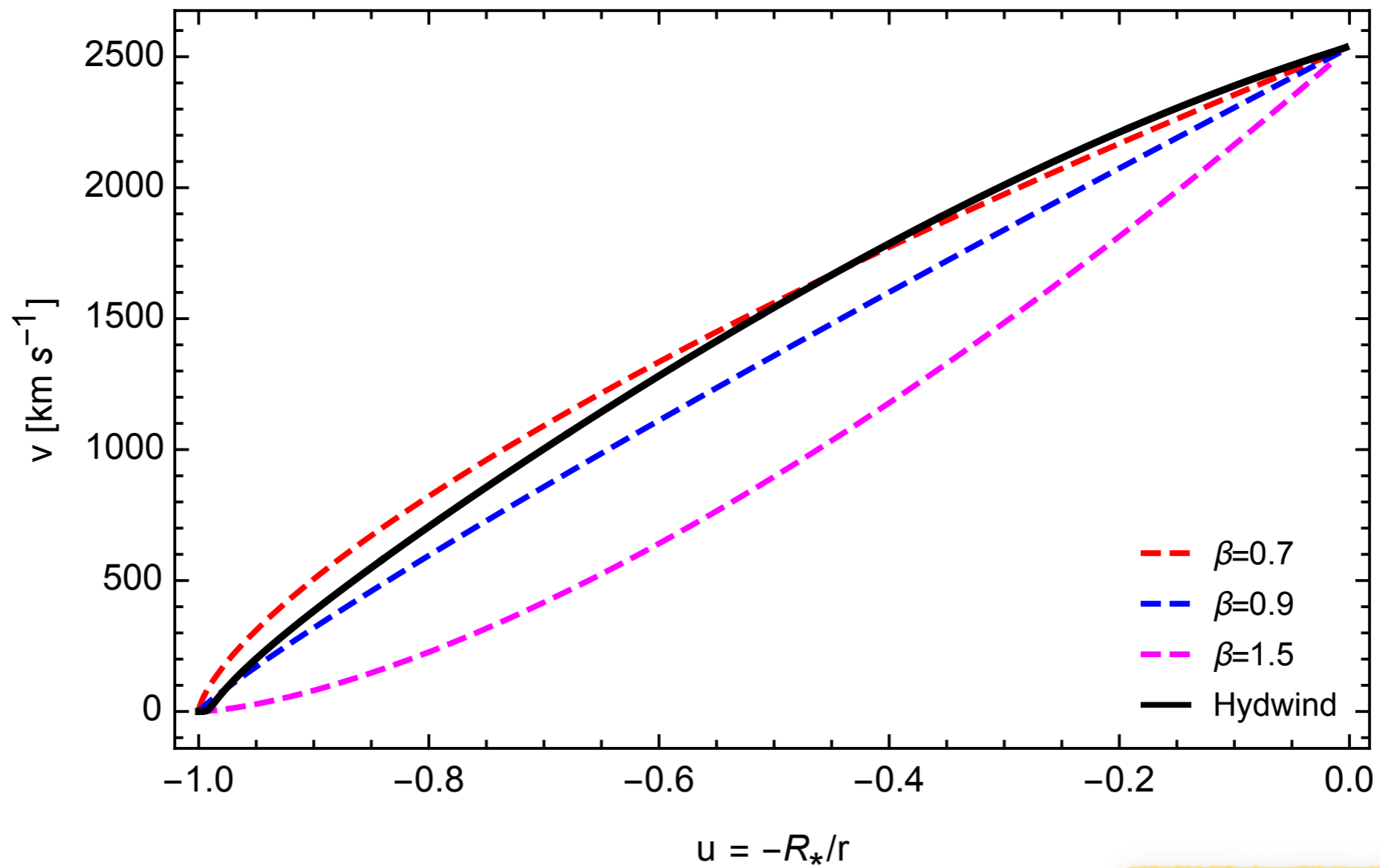
$$g_{\text{rad}}^{\text{line}} = \frac{\Gamma_{\text{E}} G M k}{r^2} \left(\frac{1}{\sigma_{\text{E}} v_{\text{th}}} \right)^{\alpha} \left(\frac{1}{\rho} \frac{\partial v}{\partial r} \right)^{\alpha} \left(\frac{n_{\text{E11}}}{W(r)} \right)^{\delta} f_{\text{CF}} \left(r, v, \frac{\partial v}{\partial r} \right)$$

δ : changes in the ionization throughout the wind

k : related to the number of lines effectively contributing to the driving of the wind

α : ratio between the line-force from optically thick lines and the total line force

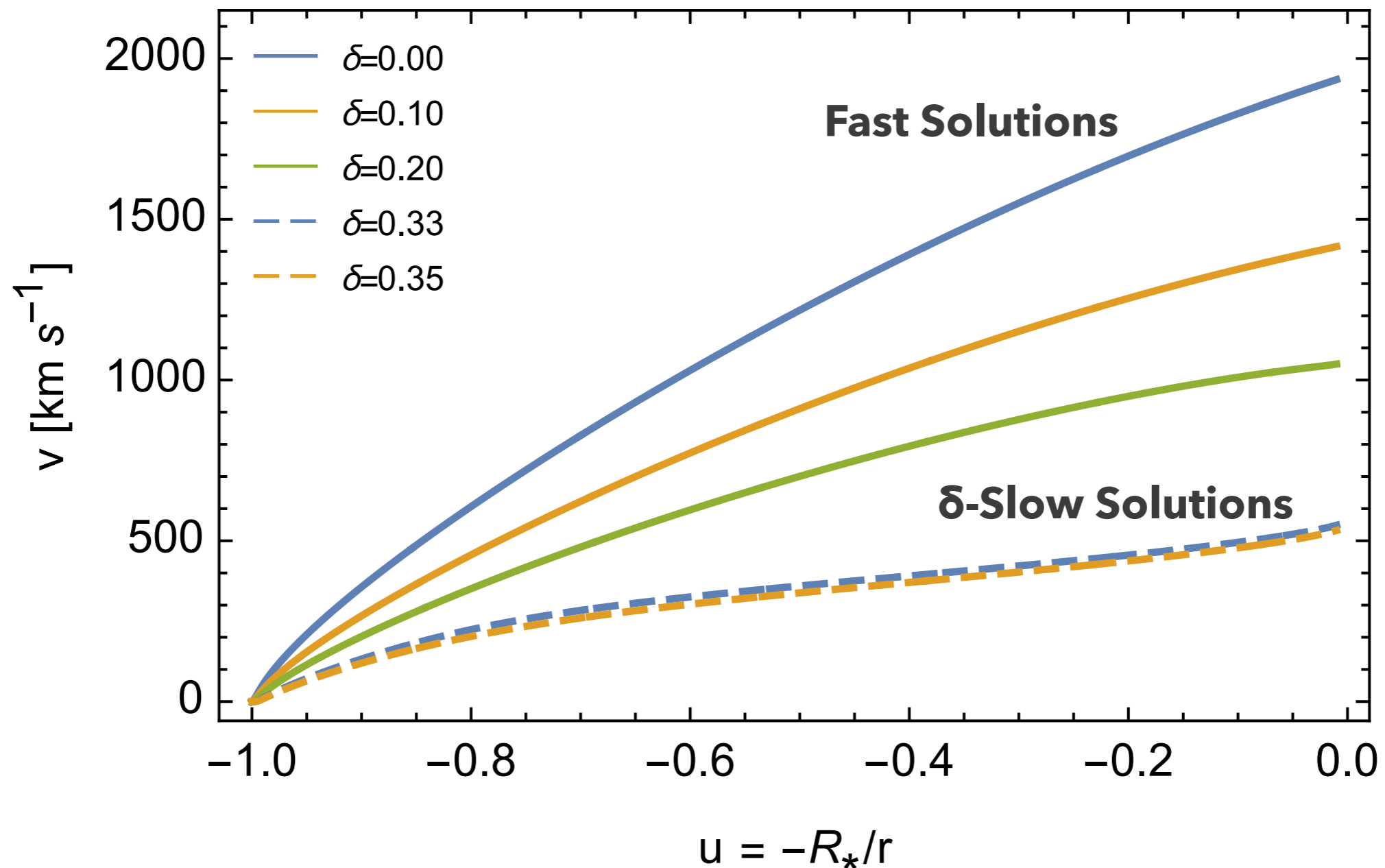
Fast Solution (Standard m-CAK)



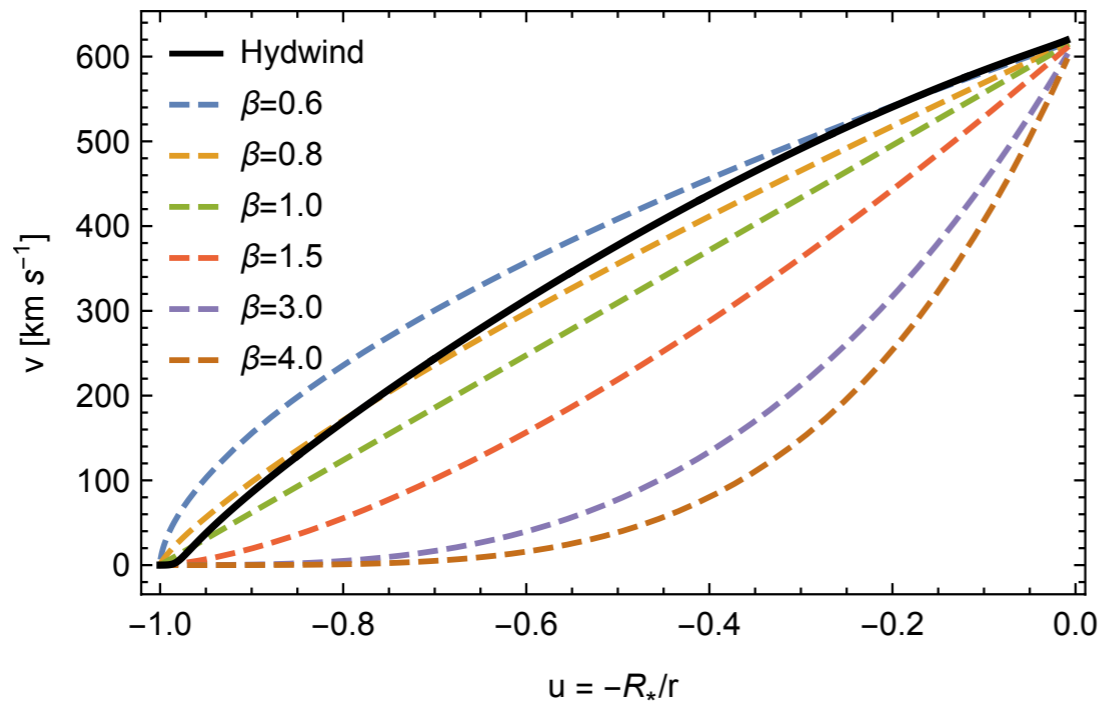
β -law
$$v(r) = v_\infty (1 - R_*/r)^\beta$$

δ -Slow Solutions (Curé et al. 2011) $\delta \gtrsim 0.3$

$$g_{\text{rad}}^{\text{line}} = \frac{\Gamma_{\text{E}} G M k}{r^2} \left(\frac{1}{\sigma_{\text{E}} v_{\text{th}}} \right)^{\alpha} \left(\frac{1}{\rho} \frac{\partial v}{\partial r} \right)^{\alpha} \left(\frac{n_{\text{E11}}}{W(r)} \right)^{\delta} f_{\text{CF}} \left(r, v, \frac{\partial v}{\partial r} \right)$$



Fast Solution



β -law

$$v(r) = v_{\infty} (1 - R_*/r)^{\beta}$$

Typical Values:

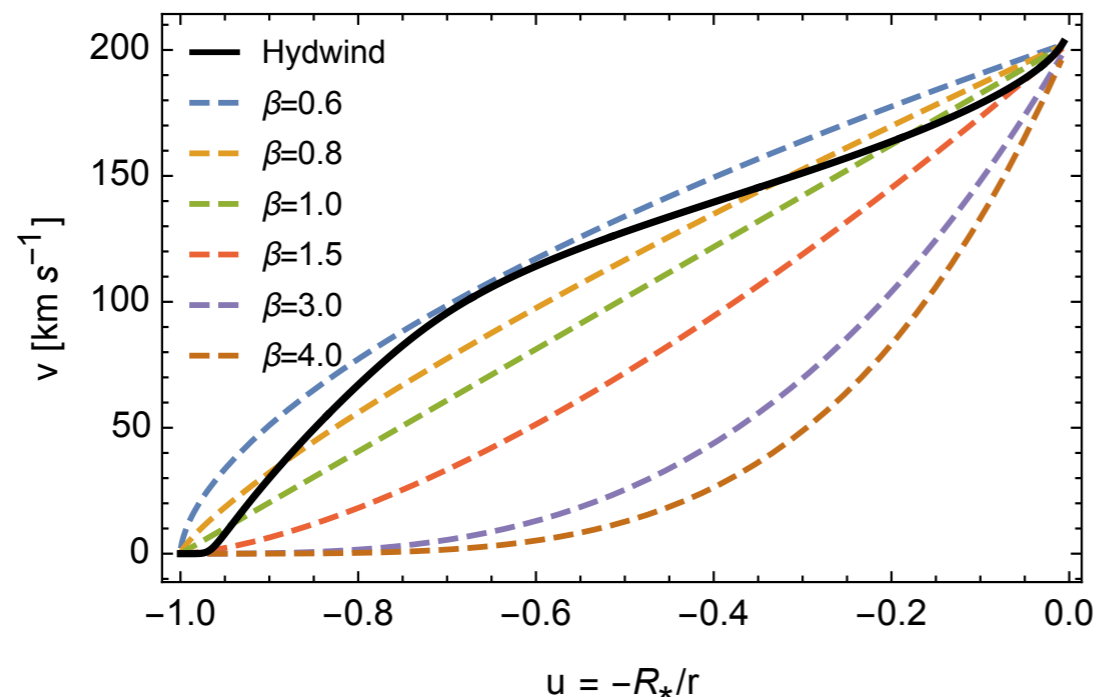
**O and B stars $\rightarrow \beta=0.7$
to 1.5**

Puls et al. 1996, Kudritzki & Puls
2000

**Late B and A supergiants
 $\rightarrow \beta > 1.5$**

(Stahl et al. 1991, Lefever et al. 2007,
Markova & Puls 2008)

δ -Slow Solution



See also Venero et al. 2024

ISOSCELES

Grid of Stellar atmosphere and hydrodynamic models of massive Stars

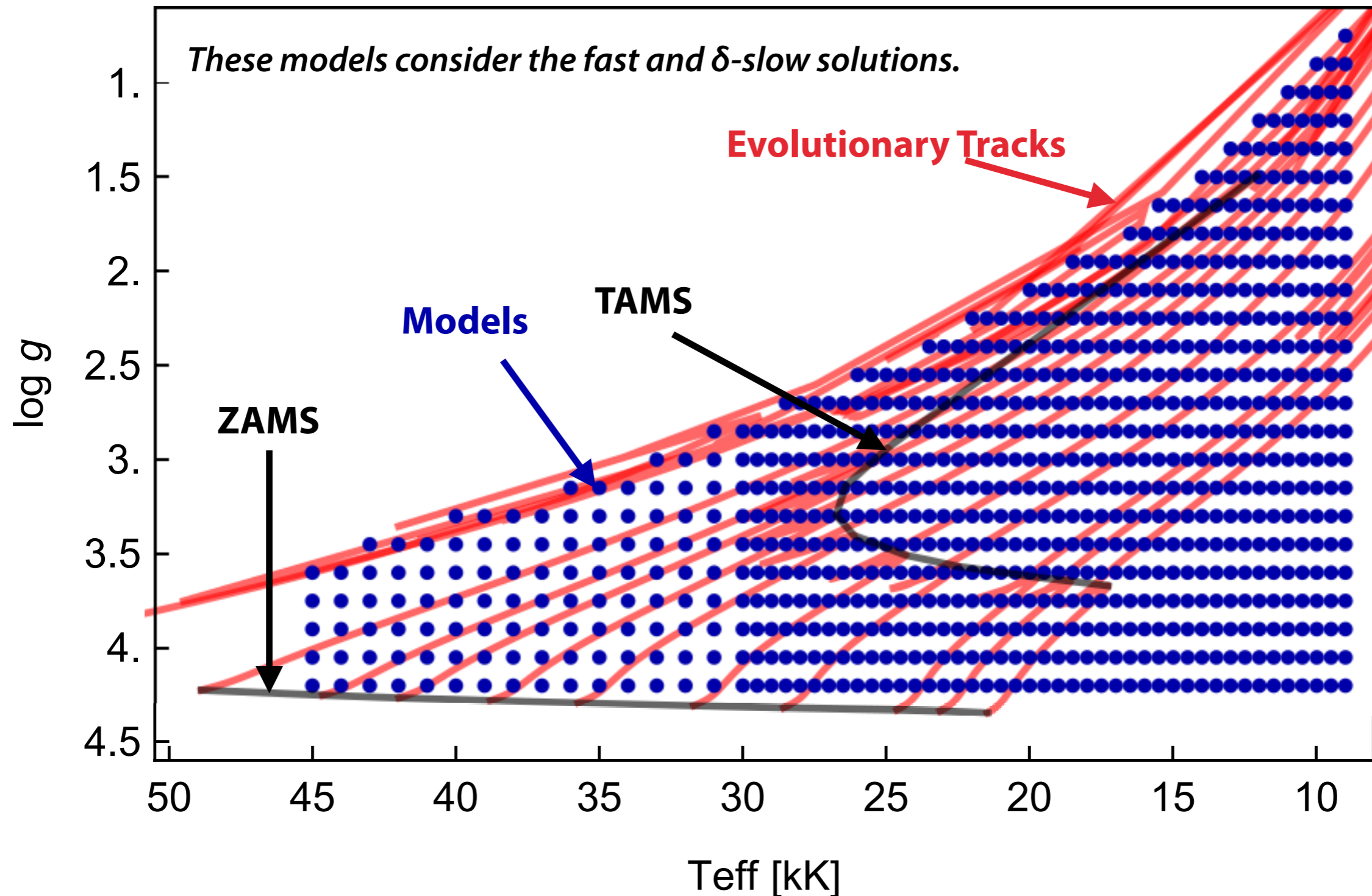
See proceeding Araya et al. 2023

Synthetic data grid for massive stars, integrating m -CAK hydrodynamics and NLTE radiative transport.

Step 1

Hydwind grid - without rotation

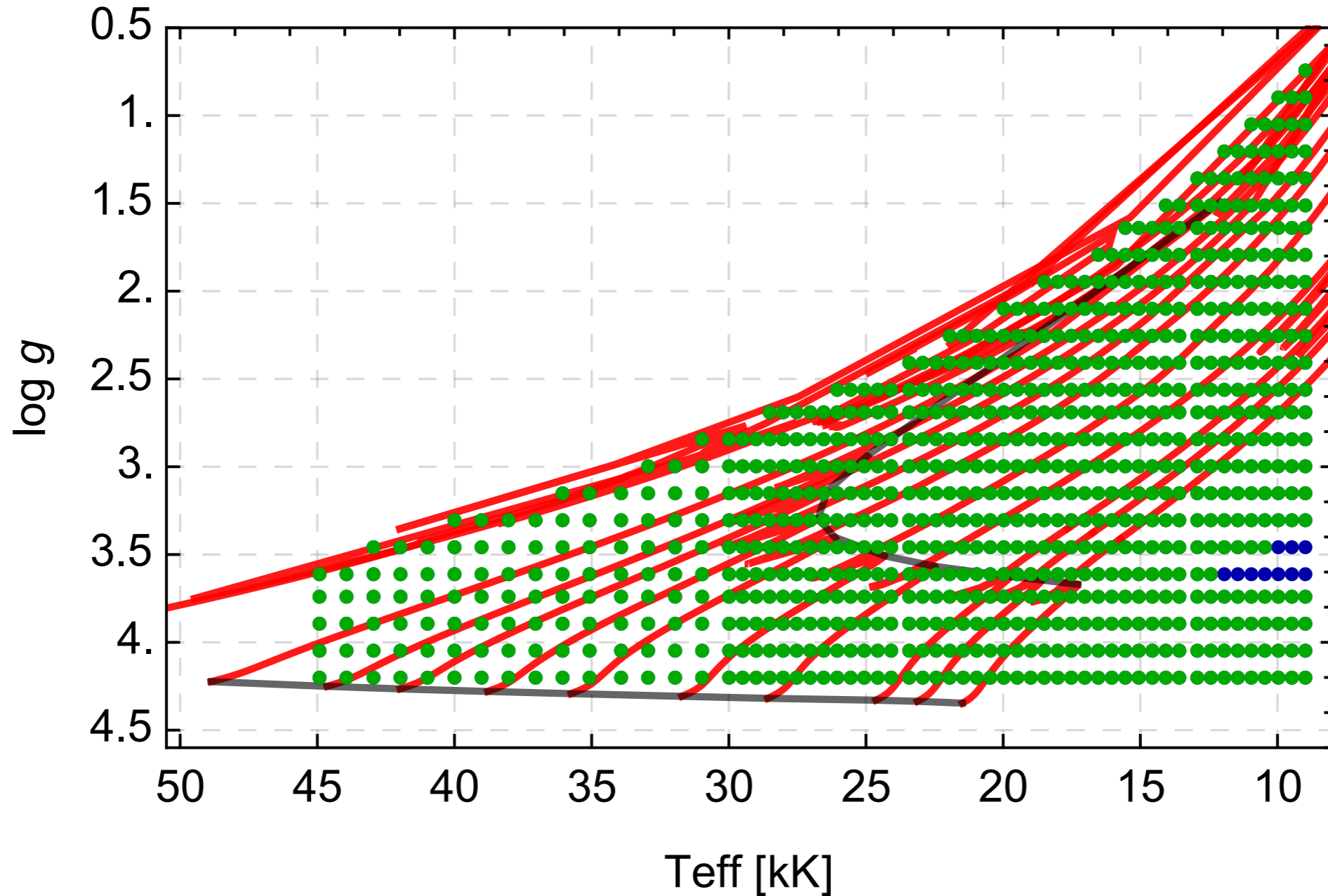
Hydwind (stationary hydrodynamic code, Curé 2004)



Step 2

Fastwind grid (without rotation)

FASTWIND (Fast Analysis of STellar Atmospheres with WINDs, Puls et al. 2005)



ISOSCELES Grid v1.0

Temperature:

9 kK - 30 kK (steps of 500 k)

31 kK - 45 kK (steps of 1000 k)

log g:

4.2 - 0.75 (steps of 0.15)

Line force parameters

α	0.45	0.47	0.51	0.53	0.55	0.57	0.61	0.65				
k	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5	0.55	0.6
δ	0.	0.04	0.1	0.14	0.2	0.24	0.3	0.31	0.32	0.33	0.34	0.35

Si abundance log ϵ_{Si} :

7.21, 7.36, 7.51 (solar), 7.66, and 7.81 dex.

Micro-turbulent velocity

1, 5, 10, 15, 20, 25 km/s

Lines H He Si:

IR - Optical

Total = 573 423 converged models

ISOSCELES Explorer

<https://ifa.uv.cl/grid>

Log g/Temp Graph

Select a Log g/Temp pair by clicking on any point in the graph, or by selecting in the selection box

Temperature (K)
45000

Log g

Temperature (°K)

Models list

First, select a model from the chosen Log g/Temp

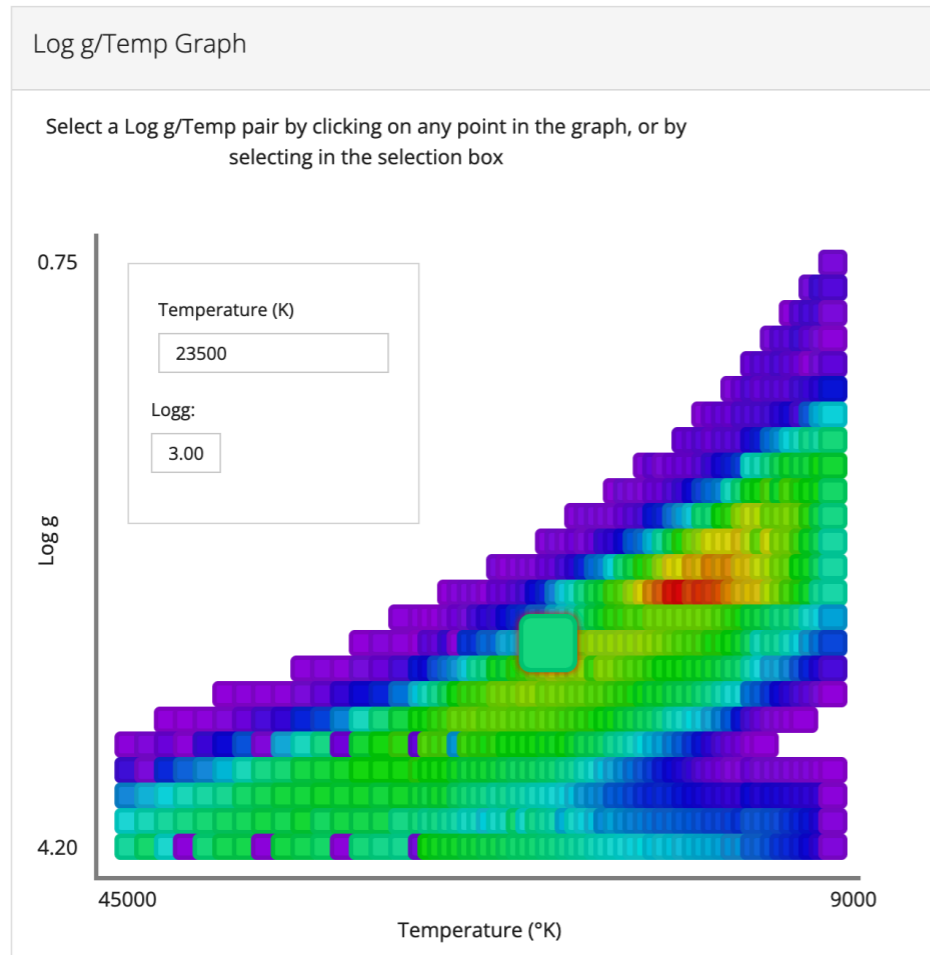
Parameter selection

[Click here to select the parameter\(s\) of interest. None selected means all selected.](#)

Get

ISOSCELES Explorer

<https://ifa.uv.cl/grid>



Models list

Temperature 23500 °K
Log g 3.00
Total of models 949

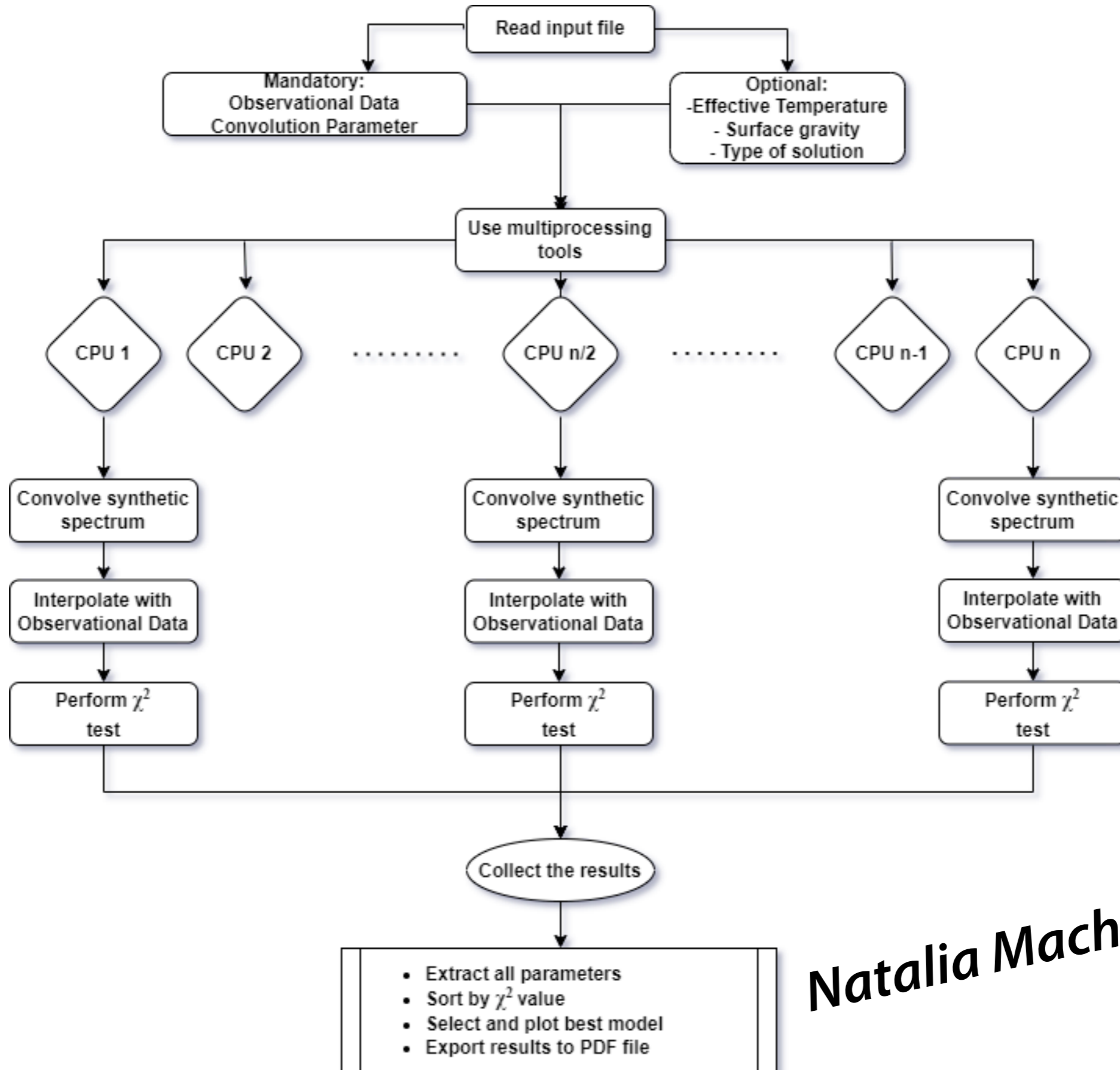
The table below shows a sample of these models

	Temp (°K)	Log g	k	alpha	delta	si	mdot	vinf
<input type="radio"/>	23500	3.00	0.25	0.61	0.10	7.81	1.3710222e-6	1.1007462e+3
<input checked="" type="radio"/>	23500	3.00	0.15	0.55	0.10	7.66	2.0969853e-7	8.8840028e+2
<input type="radio"/>	23500	3.00	0.25	0.45	0.32	7.66	2.6928484e-8	3.0495954e+2
<input type="radio"/>	23500	3.00	0.25	0.55	0.24	7.66	9.5403302e-7	5.9674206e+2
<input type="radio"/>	23500	3.00	0.25	0.61	0.14	7.51	1.5671467e-6	9.7650579e+2
<input type="radio"/>	23500	3.00	0.25	0.61	0.14	7.66	1.5671467e-6	9.7650579e+2
<input type="radio"/>	23500	3.00	0.25	0.61	0.20	7.81	1.9966341e-6	8.2119768e+2
<input type="radio"/>	23500	3.00	0.30	0.45	0.10	7.36	1.9203121e-7	6.4988458e+2
<input type="radio"/>	23500	3.00	0.30	0.65	0.24	7.36	6.1899429e-6	8.4175889e+2
<input type="radio"/>	23500	3.00	0.60	0.65	0.14	7.81	1.3285612e-5	1.1509216e+3

Parameter selection Click here to select the parameter(s) of interest. None selected means all selected.

<input type="checkbox"/> BR10	<input type="checkbox"/> HEI4471	<input type="checkbox"/> HEI712	<input type="checkbox"/> SIIII4552
<input type="checkbox"/> BR11	<input type="checkbox"/> HEI4713	<input type="checkbox"/> HEI713	<input type="checkbox"/> SIIII4567
<input type="checkbox"/> BR12	<input type="checkbox"/> HEI4922	<input type="checkbox"/> HEPS	<input type="checkbox"/> SIIII4574
<input type="checkbox"/> BRALPHA	<input type="checkbox"/> HEI6678	<input type="checkbox"/> HGAMMA	<input type="checkbox"/> SIIII4716
<input type="checkbox"/> BRBETA	<input type="checkbox"/> HEI1218	<input type="checkbox"/> PALPHA	<input type="checkbox"/> SIIII4813
<input type="checkbox"/> BRGAMMA	<input type="checkbox"/> HEI14200	<input type="checkbox"/> PBETA	<input type="checkbox"/> SIIII4819
<input checked="" type="checkbox"/> HALPHA	<input type="checkbox"/> HEI14541	<input type="checkbox"/> PF10	<input type="checkbox"/> SIIII4829
<input type="checkbox"/> HBETA	<input type="checkbox"/> HEI14686	<input type="checkbox"/> PF9	<input type="checkbox"/> SIIII5739
<input type="checkbox"/> HDELTA	<input type="checkbox"/> HEI157	<input type="checkbox"/> PFGAMMA	<input type="checkbox"/> SIIIV4089
<input type="checkbox"/> HEI170	<input type="checkbox"/> HEI1611	<input type="checkbox"/> PGAMMA	<input type="checkbox"/> SIIIV4116
<input type="checkbox"/> HEI205	<input type="checkbox"/> HEI16406	<input type="checkbox"/> SIIII4128	<input type="checkbox"/> SIIIV4212
<input type="checkbox"/> HEI211	<input type="checkbox"/> HEI16527	<input type="checkbox"/> SIIII4130	<input type="checkbox"/> SIIIV4950
<input type="checkbox"/> HEI4026	<input type="checkbox"/> HEI16683	<input type="checkbox"/> SIIII5041	<input type="checkbox"/> SIIIV6667
<input type="checkbox"/> HEI4387	<input type="checkbox"/> HEI167	<input type="checkbox"/> SIIII5056	<input type="checkbox"/> SIIIV6701

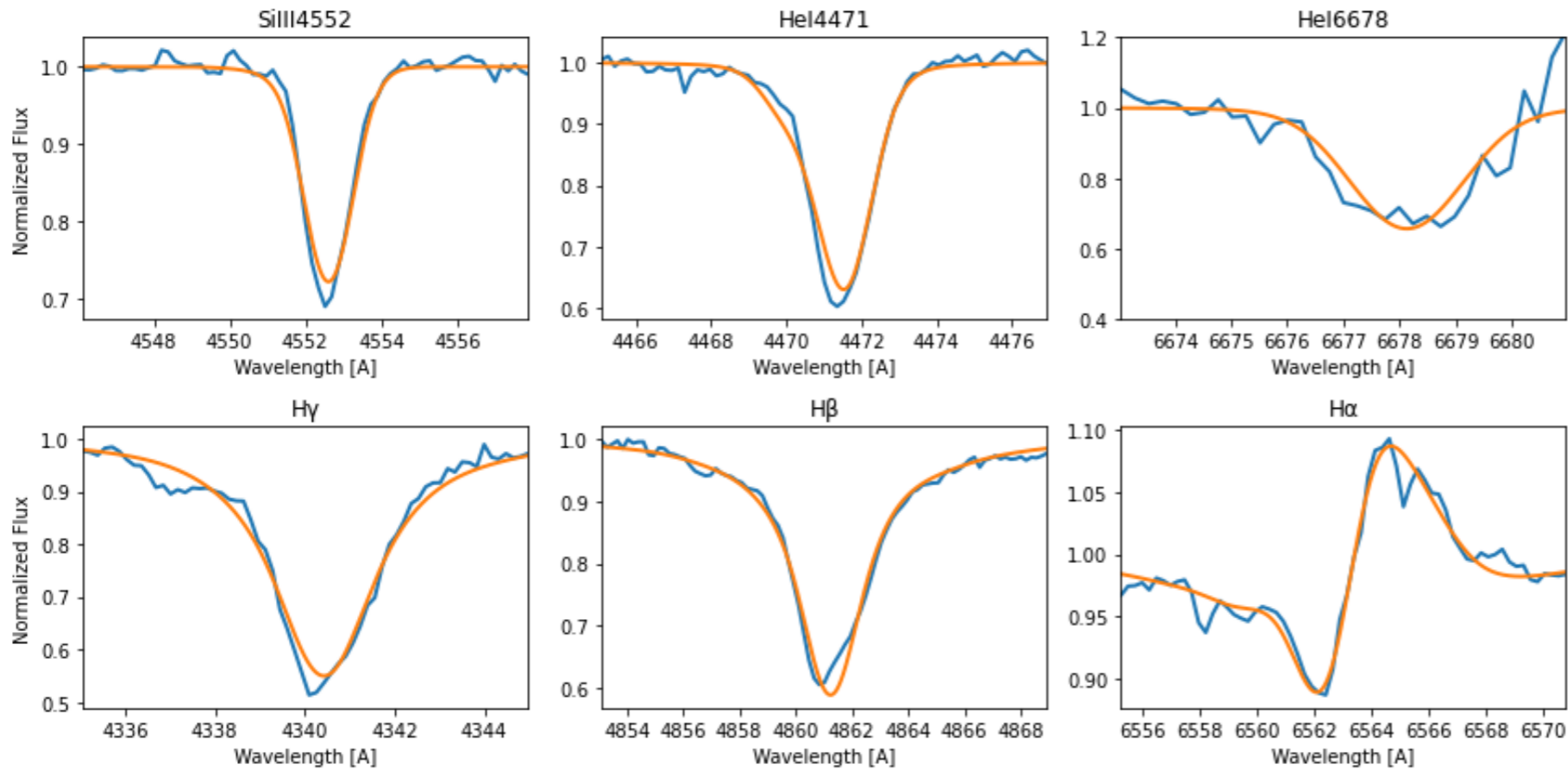
Optimization problem of spectral line fitting



Natalia Machuca's work

Some Results

HD 99953

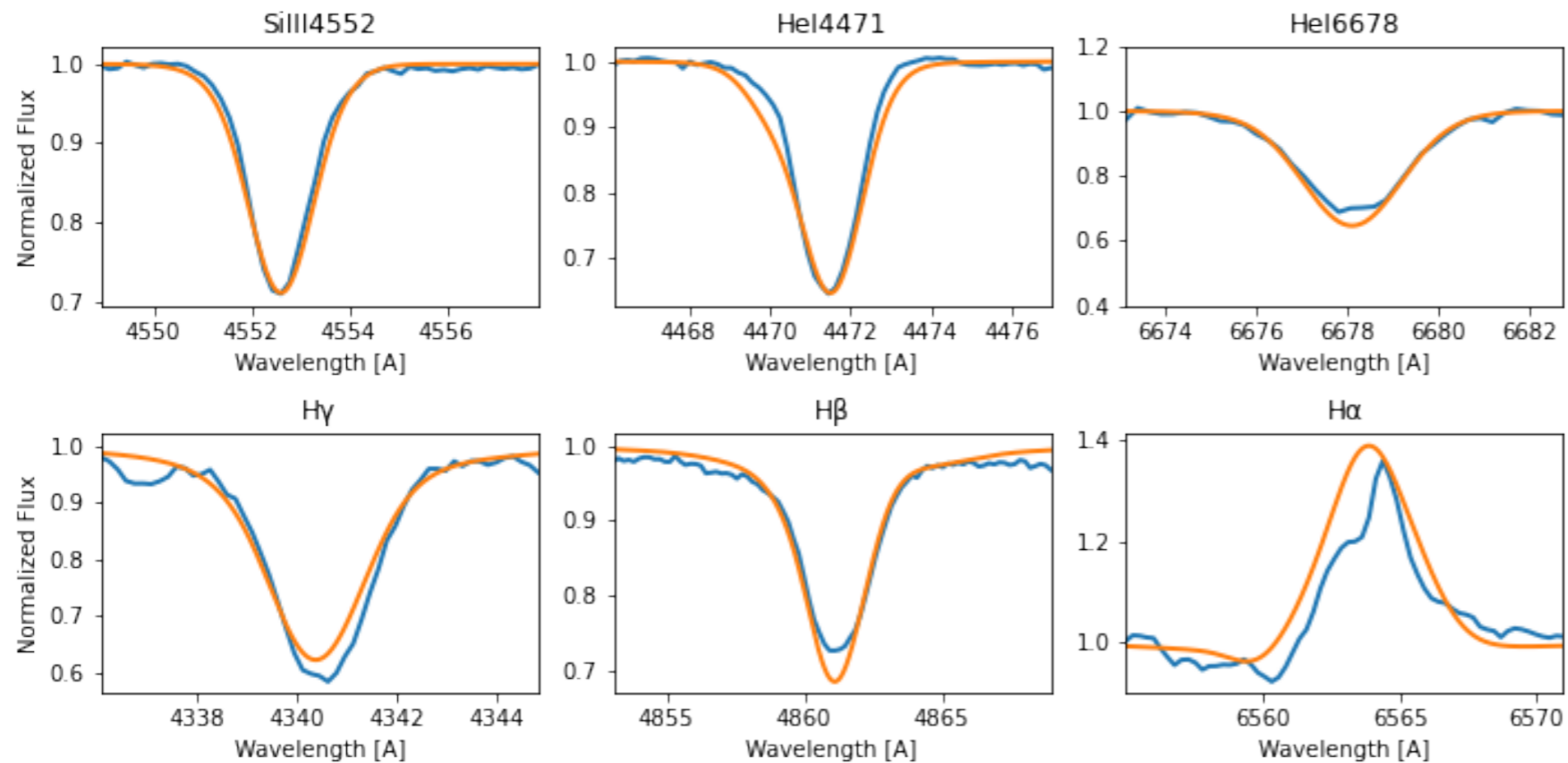


Observations from Haucke et al. 2018

	Haucke et al. 2018	This work
T_{eff} [K]	19000	18500
$\log g$	2.30	2.40
α	—	0.53
k	—	0.15
δ	—	0.34
β	2.0	—
\dot{M} [$10^{-6} M_{\odot} / \text{yr}$]	0.13	0.24
v_{∞} [km/s]	500	254

Some Results

HD 41117

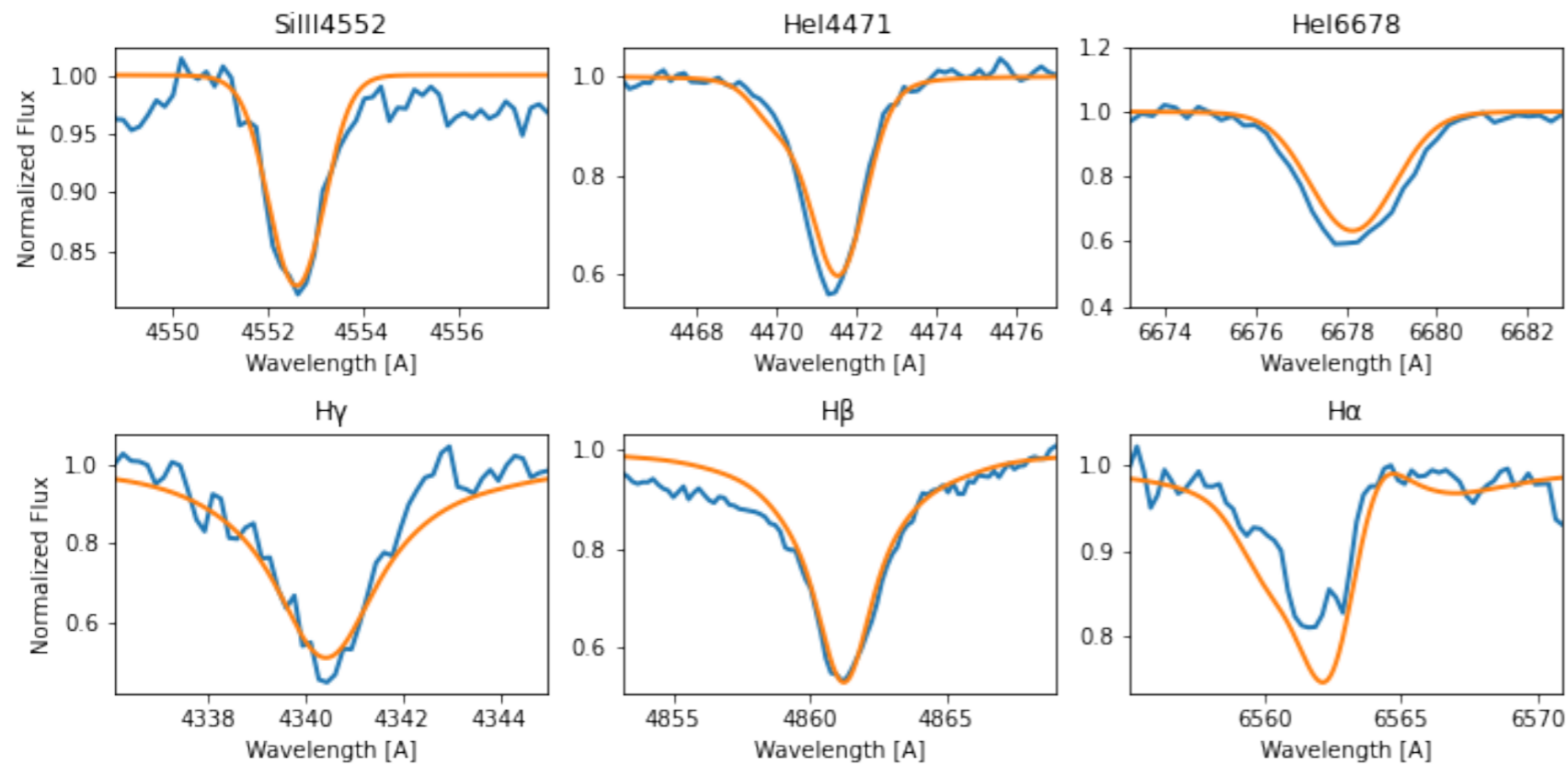


Observations from Haucke et al. 2018

	Haucke et al. 2018	This work
T_{eff} [K]	19000	19000
$\log g$	2.30	2.25
α	—	0.53
k	—	0.1
δ	—	0.33
β	2.0	—
\dot{M} [$10^{-6} M_{\odot} / \text{yr}$]	0.17	0.55
v_{∞} [km/s]	510	223

Some Results

HD 75149



Observations from Haucke et al. 2018

	Haucke et al. 2018	This work
T_{eff} [K]	16000	16500
$\log g$	2.10	2.25
α	—	0.51
k	—	0.2
δ	—	0.33
β	2.5	—
\dot{M} [$10^{-6} M_{\odot} / \text{yr}$]	0.16	0.19
v_{∞} [km/s]	400	228

Natalia Machuca's Poster



Spectral modelling of OB-type stars and the Wind momentum Luminosity Relationship

Natalia Machuca¹, Michel Curé¹ and Ignacio Araya²

¹Universidad de Valparaíso, ²Universidad Mayor



Results

Wind momentum depends on the mass-loss rates, terminal velocity and radius of the star as shown in the y-axis. With this, we defined the WLR as $\log(D_{\text{mom}}) = x \log(L/L_{\odot}) + D_0$.

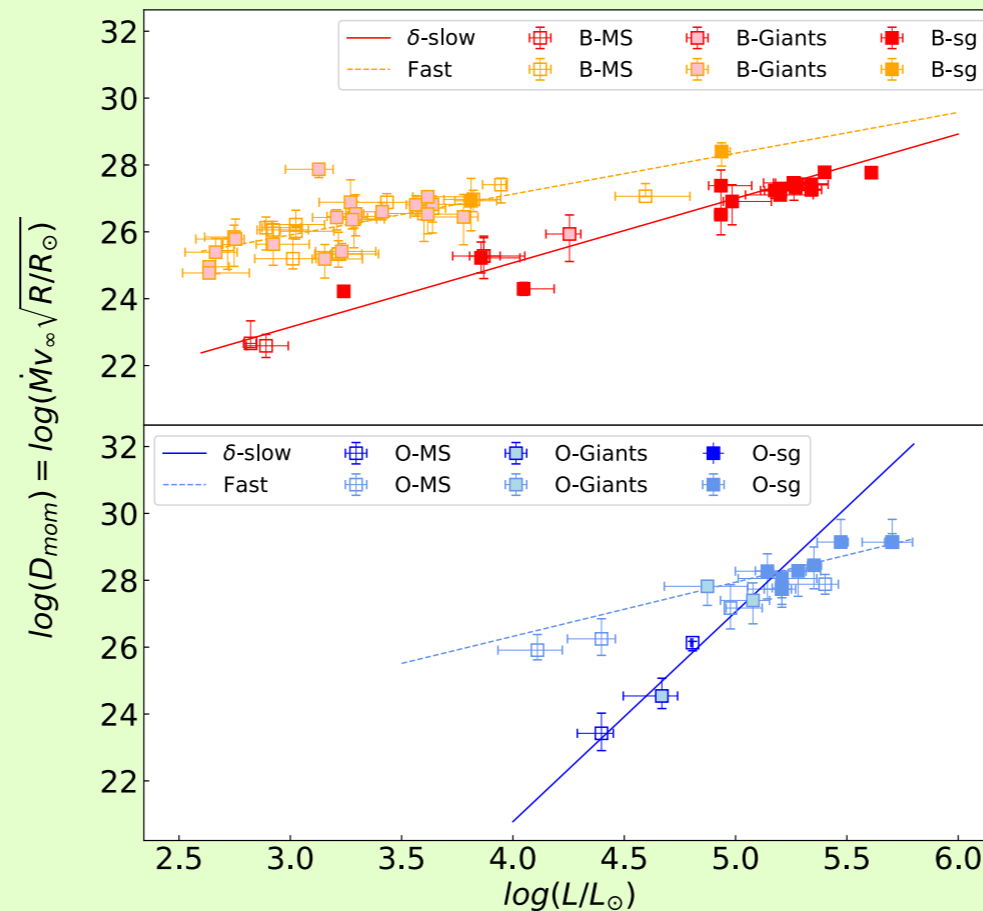


Figure 2. WLR for O and B-type stars. Dashed lines are linear fits for both hydrodynamical solutions. Filling styles represent different luminosity classes. Values of the WLR found for B-type stars are $x = 1.92^{+0.14}$ and $D_0 = 17.37^{+0.65}$ for δ -slow solutions and $x = 1.22^{+0.17}$ and $D_0 = 22.23^{+0.58}$ for fast solutions. For O-type stars, these values are $x = 6.27^{+1.85}$ and $D_0 = -4.31^{+8.57}$ for δ -slow solutions and $x = 2.07^{+0.20}$ and $D_0 = 17.23^{+1.07}$ for fast solutions.

Felipe Ortiz's Poster

Classification of spectral H α lines from massive stars using machine learning methods

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¹ Instituto de Física y Astronomía, Universidad de Valparaíso.

² Escuela de Informática, Universidad Técnica Federico Santa María, CCTVal-UTFSM.

³ Centro Multidisciplinario de Física, Universidad Mayor.



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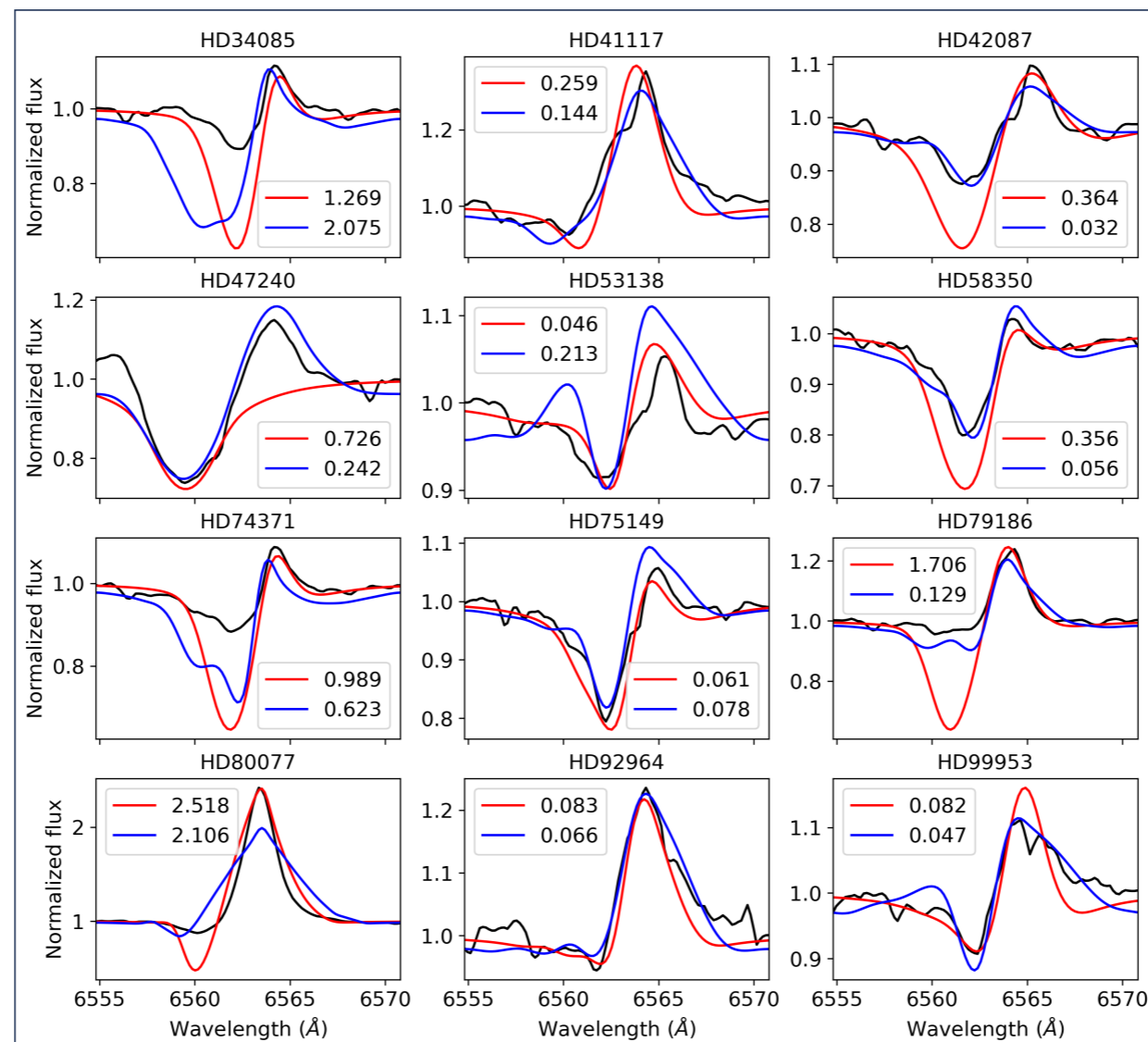


Fig. 3: H α lines for 12 stars studied in [6]. In blue there are our fits, and in red the fits from [6]. The labels show the χ^2 values.

ISOSCELES Grid v2.0

Temperature:

10 kK - 30 kK (steps of 500 k)

31 kK - 45 kK (steps of 1000 k)

log g:

4.2 - 0.75 (steps of 0.15)

Micro-turbulent velocity

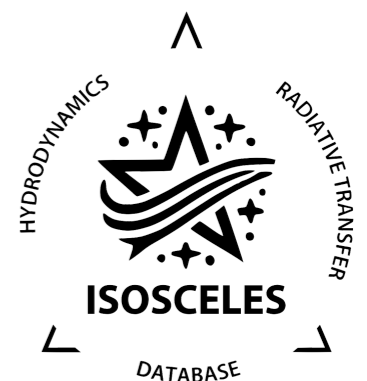
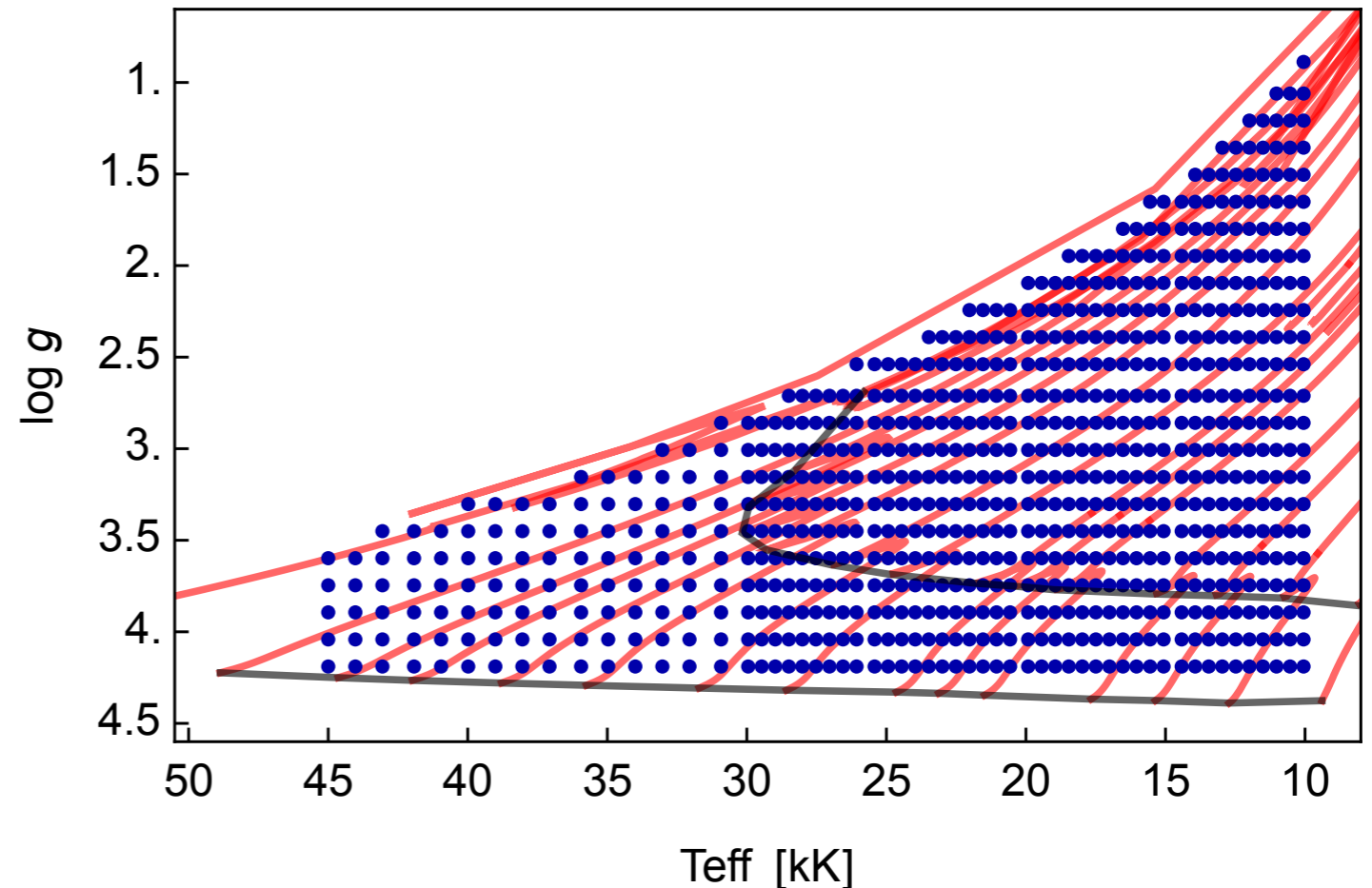
1, 5, 10, 15, 20, 25 km/s

Line force parameters

α	0.4	0.43	0.46	0.49	0.52	0.55	0.58	0.61	0.64	0.67	0.7		
k	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5	0.55	0.6	0.65
δ	0.	0.04	0.1	0.14	0.2	0.24	0.29	0.3	0.31	0.32	0.33	0.34	0.35

Lines profiles - H He Si C N O

IR - Optical - UV



ISOSCELES Grid - Differences

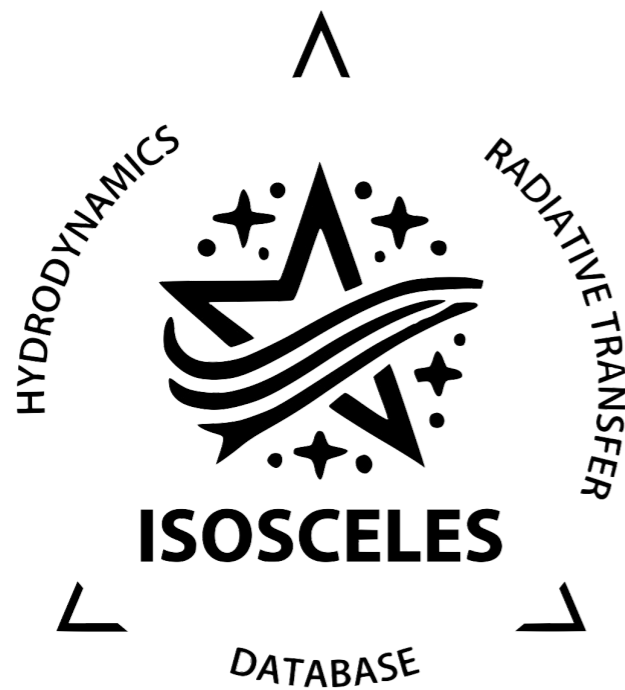
	ISOSCELES v1.0	ISOSCELES v2.0
<i>Wavelength Range</i>	<i>IR, Optical</i>	<i>IR, Optical, UV</i>
<i>Explicit Elements</i>	<i>H, He, Si</i>	<i>H, He, Si, C, N, O</i>
<i># Line profiles</i>	<i>57</i>	<i>167</i>
<i># Models</i>	<i>~ 0.5 M</i>	<i>~ 2.5 M</i>
<i>CAK parameters</i>	<i>k: 12 values α: 8 values δ: 12 values</i>	<i>k: 13 values α: 11 values δ: 13 values</i>
<i>Size (binary format)</i>	<i>~300 Gb</i>	<i>~1.4 Tb</i>

Final Remarks and Future Work

- ISOSCELES is the first grid of synthetic data for massive stars that involves both, the **m-CAK** hydrodynamics and the NLTE radiative transport.
- The results obtained from ISOSCELES should have a better justification than the currently and widely calculated models with a **β -law** in quantitative spectroscopic analyses, **especially for high values of β**
- ISOSCELES v2.0 will cover the **UV** region
- We are implementing **Machine-learning methods** for the spectral line fitting.
- The next steps are new grids with other **metallicities**.

If anyone wants to use ISOSCELES, please feel free to contact me (ignacio.araya@umayor.cl)!

Thanks!



QUESTIONS?

STELLAR ATMOSPHERE AND HYDRODYNAMIC MODELING: ISOSCELES V2.0

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