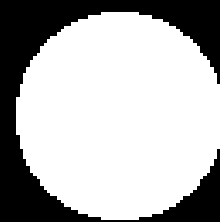
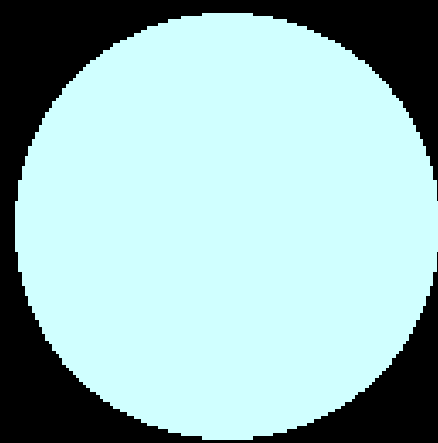

Strong Winds of Magnetic Massive Stars

Asif ud-Doula
Penn State Scranton

Introduction

- Line-driven winds
- Magnetism in stars
- Numerical simulations/models
- Results, implications

Main Sequence Stars



Spectral Type:	O	B	A	F	G	K	M
Temperature:	40 000K	20 000K	8500K	6500K	5700K	4500K	3200K
Radius (Sun=1):	10	5	1.7	1.3	1.0	0.8	0.3
Mass (Sun=1):	50	10	2.0	1.5	1.0	0.7	0.2
Luminosity (Sun=1):	100 000	1000	20	4	1.0	0.2	0.01
Lifetime (million yrs):	10	100	1000	5000	10 000	50 000	100 000
Abundance:	0.00001%	0.05%	0.3%	1.5%	4%	9%	80%

Giant Stars

Low mass stars near the end of their life.

Spectral Type:	G, K or M
Temperature:	4000K
Radius (Sun=1):	20
Mass (Sun=1):	1.2
Luminosity (Sun=1):	200
Lifetime (million yrs):	10
Abundance:	0.5%

White Dwarfs

Dying remnant of an imploded star.

Spectral Type:	D
Temperature:	Under 50 000K
Radius (Sun=1):	Under 0.01
Mass (Sun=1):	Under 1.4
Luminosity (Sun=1):	Under 0.01
Lifetime (million yrs):	–
Abundance:	5%

Supergiant Stars

High mass stars near the end of their life.

Spectral Type:	B, A, F, G, K or M
Temperature:	4000 to 40 000K
Radius (Sun=1):	30 to 500
Mass (Sun=1):	10 to 70
Luminosity (Sun=1):	30 000 to 1 000 000
Lifetime (million yrs):	10
Abundance:	0.0001%

Mass Loss from Stars

- Stars like the sun lose very little mass $\sim 10^{-14}$ MSun/yr
- Solar wind is driven by gas pressure gradient
- Hot/massive stars (O and B type) lose $10^{-9}\sim 10^{-5}$ MSun/yr
- Hot star winds are driven by scattering of radiation by resonance lines of heavy ions.

Sound speed; thermal pressure has little significance.

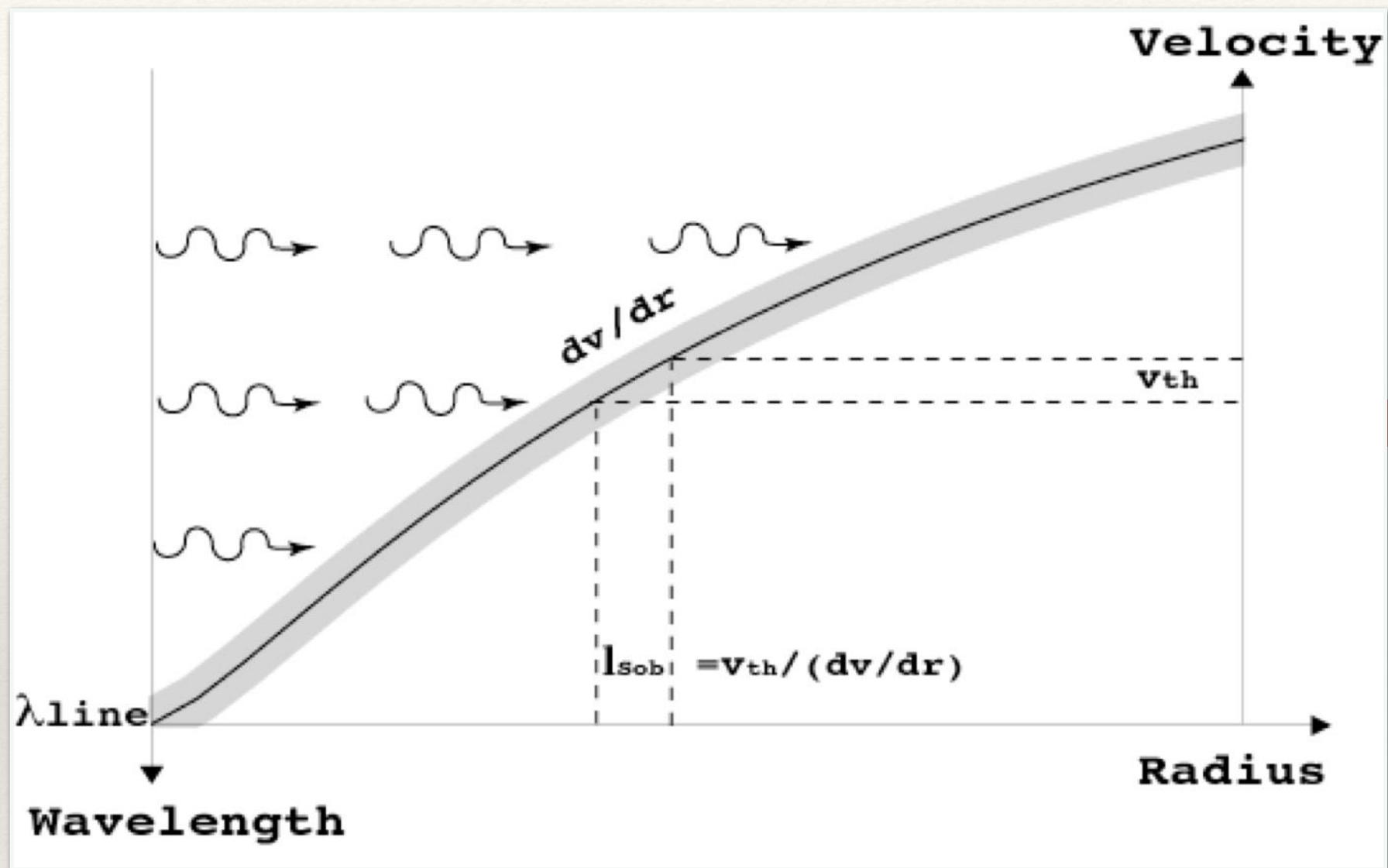
Light's Momentum

- Light has momentum, $p=E/c$
- Usually neglected, because c is so high
- But becomes significant for very bright stars
- Key question: how big is this force vs. gravity?

Light As a Driving Mechanism

- Free Electron (continuum) Scattering
- Bound Electron (line) Scattering
 - Can be much stronger than free electron scattering

Light As a Driving Mechanism



$$L_{sob} \ll R_*$$

For strong,

optically thick lines

$$g_{thick} \sim \frac{g_{thin}}{\tau} \sim \frac{1}{\rho} \frac{dv}{dr} \tau \equiv \kappa \rho \frac{v_{th}}{dv/dr}$$

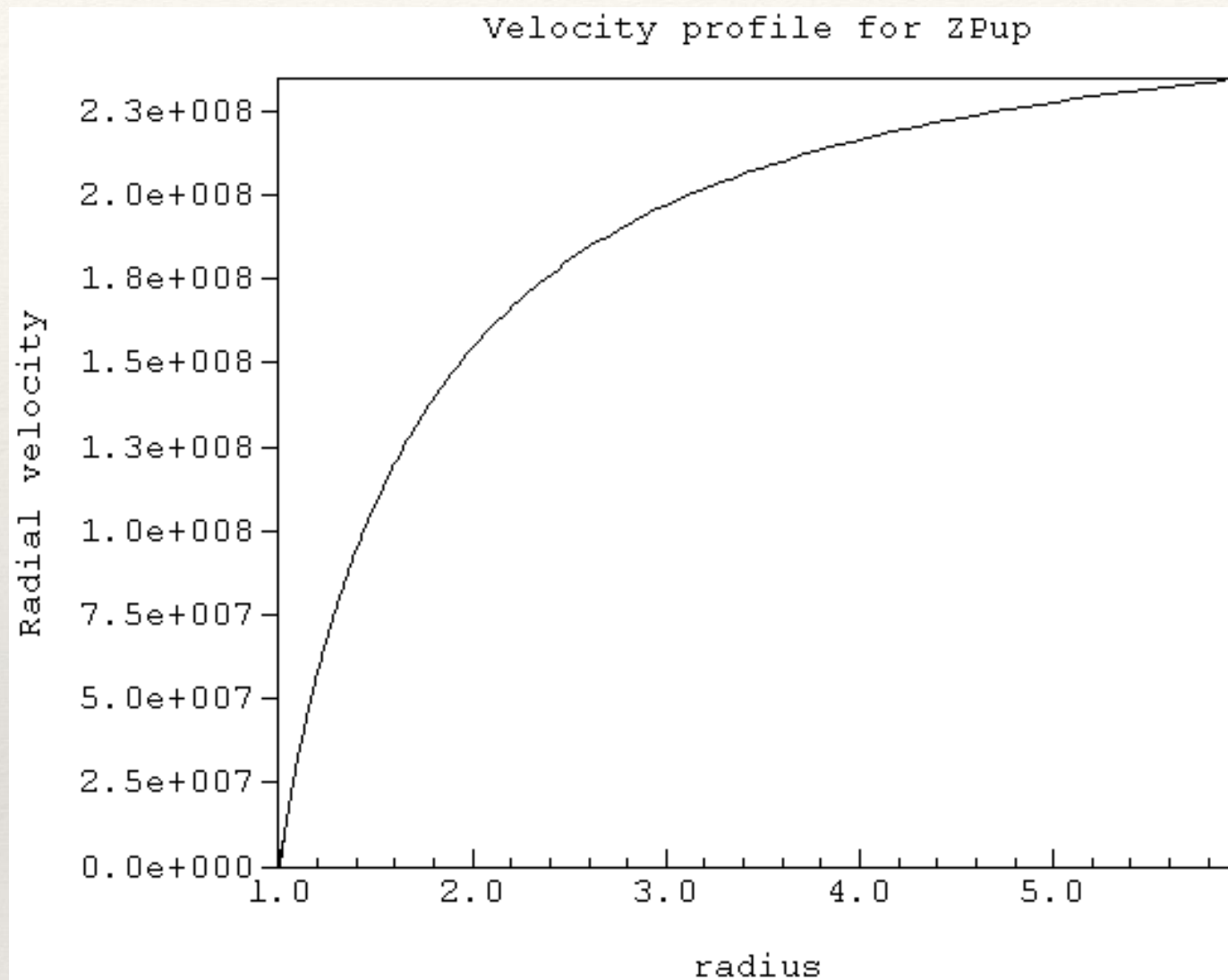
Line Force From an Ensemble of Lines in CAK theory

If we take into account all available thick and thin lines, the line force is:

$$g_{lines} \approx \bar{Q} \frac{\kappa_e L}{4\pi r^2 c} \left(\frac{dv/dr}{\rho c \bar{Q} \kappa_e} \right)^\alpha$$

Free e- scattering

1D CAK Model of ZPup



Steady & spherically
symmetric

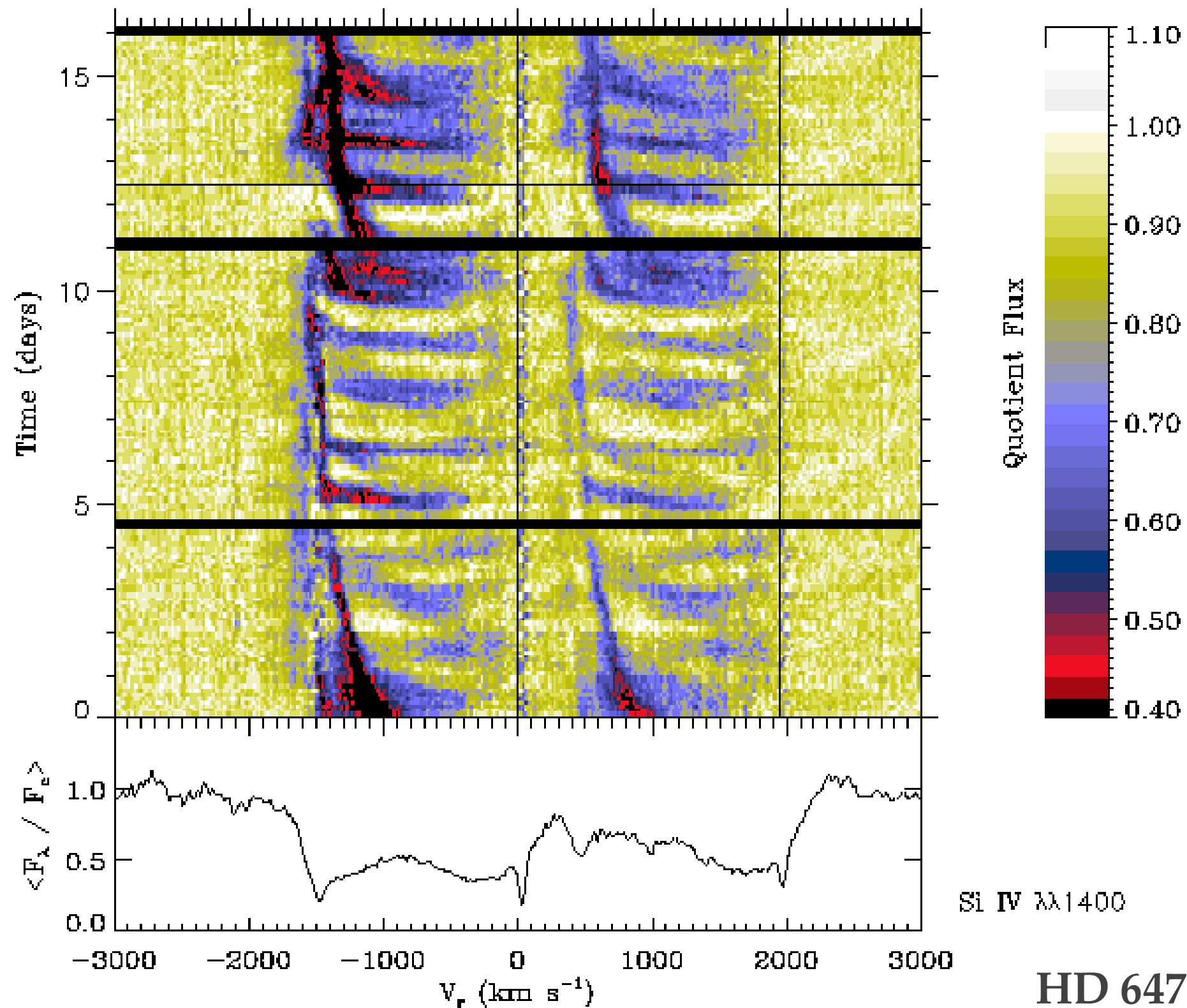
well characterized by

$$v(r) = v_{\infty} (1 - R_* / r)^{\beta}$$

Observational evidence:

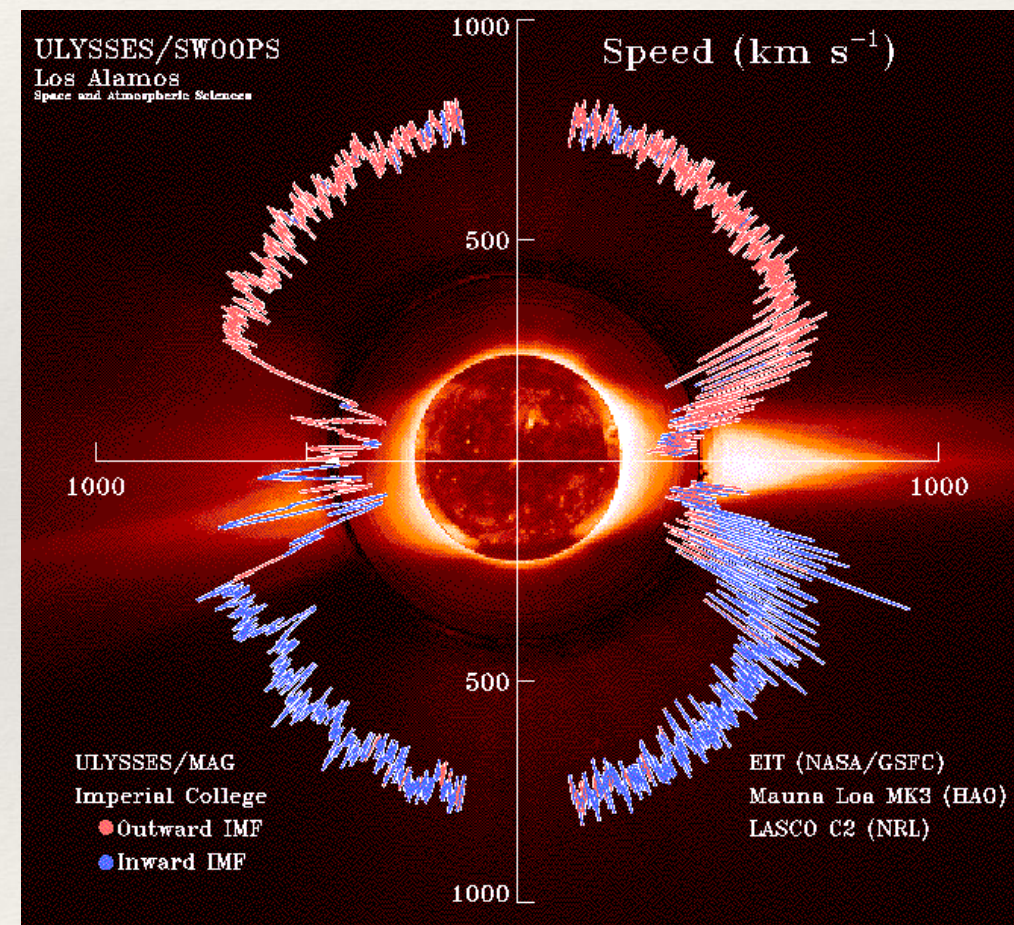
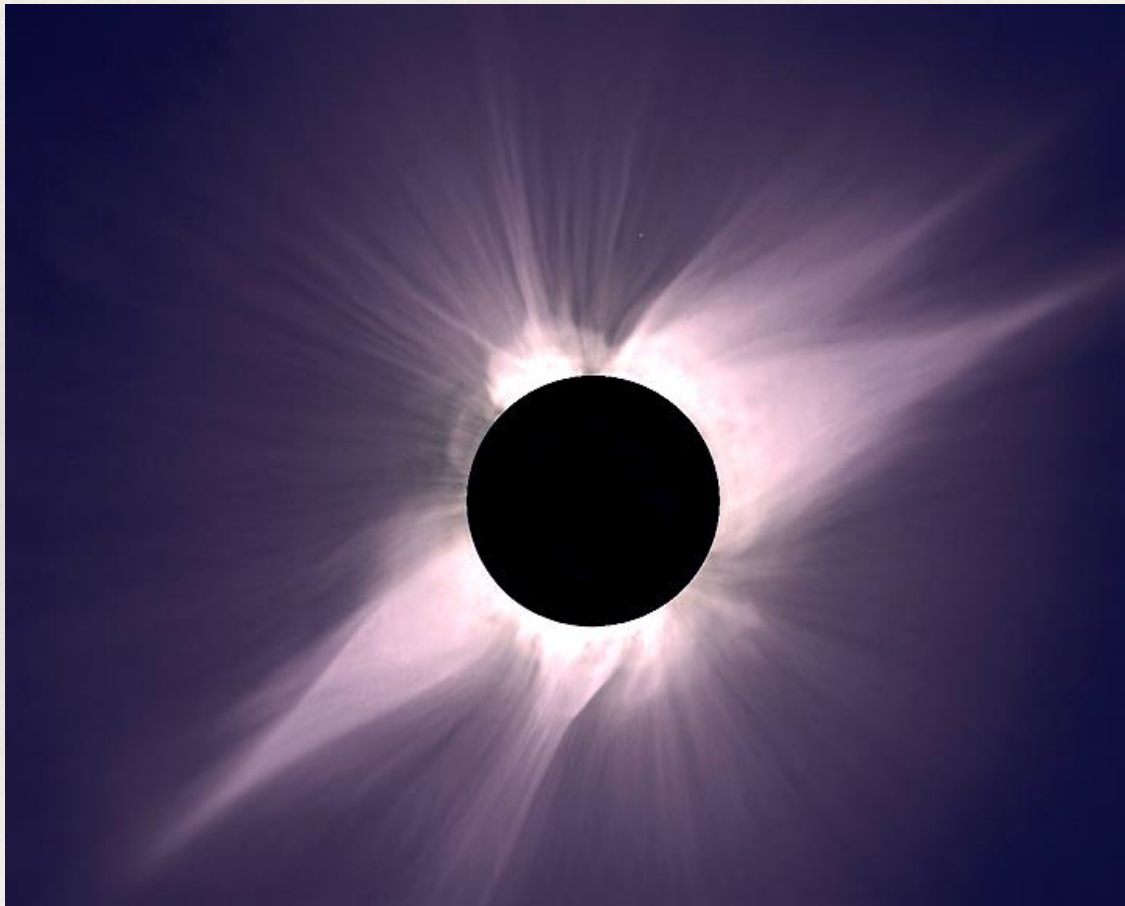
unsteady, spherically non-symmetric.

Discrete Absorption Features



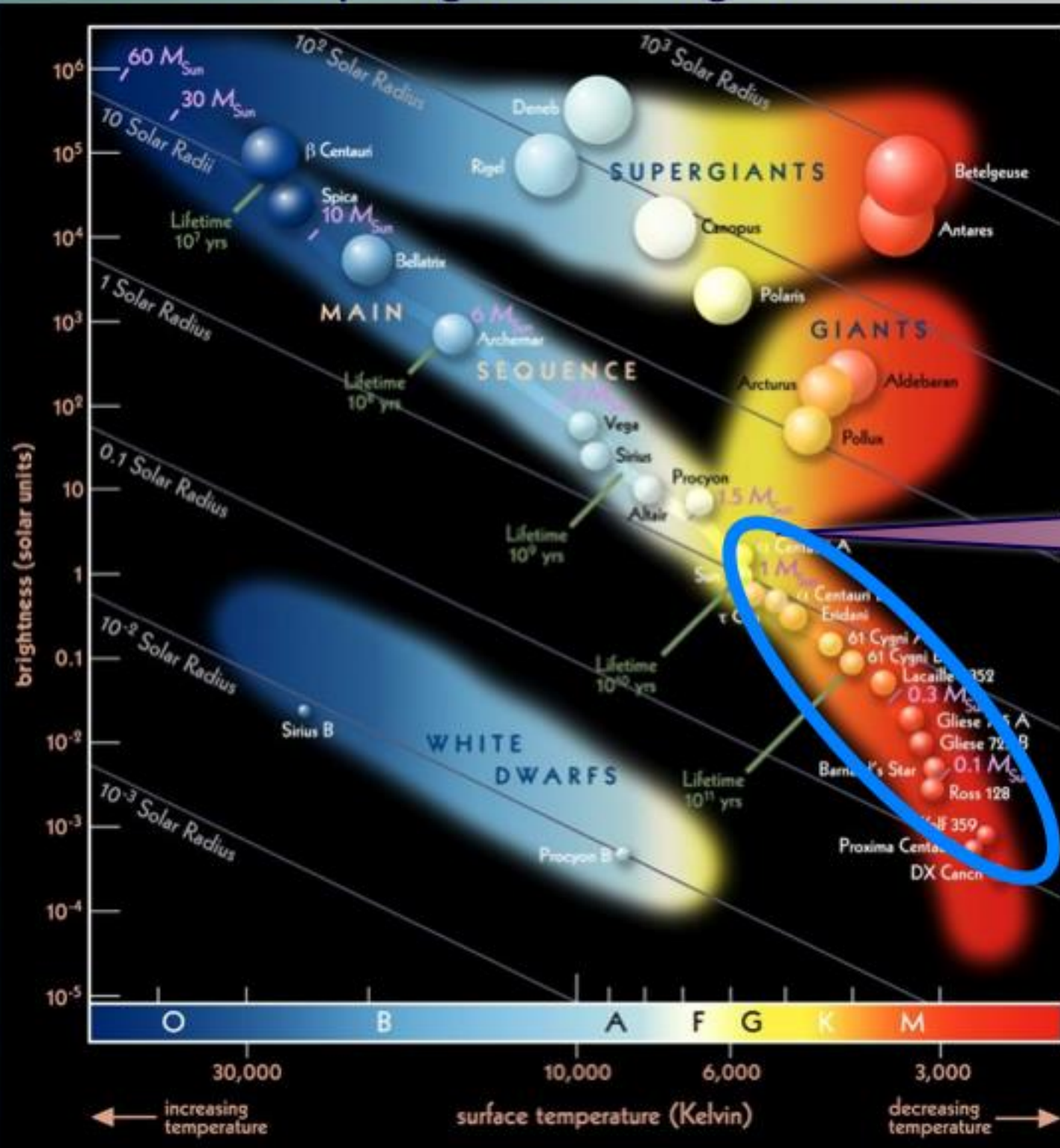
Magnetic Effects on Solar Coronal Expansion

1991 Solar Eclipse



Where do we find stellar magnetism?

The Hertzsprung-Russell diagram of stars



Our Sun

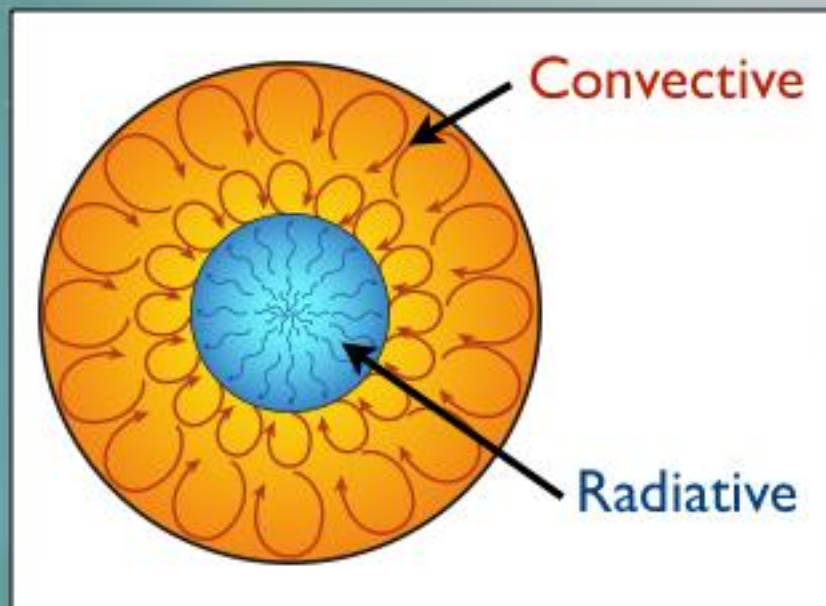


1 kGauss = 0.1 Tesla

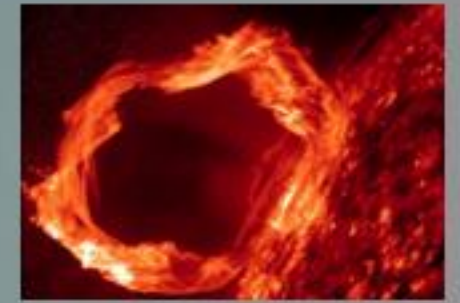
Courtesy: V. Petit

The Sun and its fellow low-mass stars

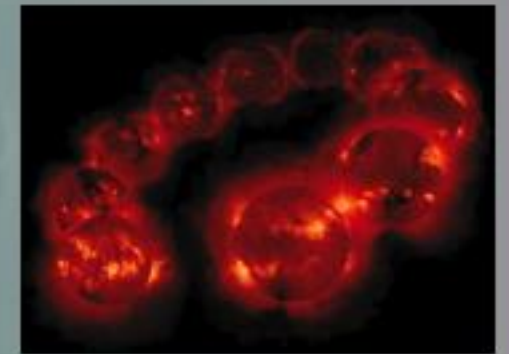
Cool stars with convective envelopes



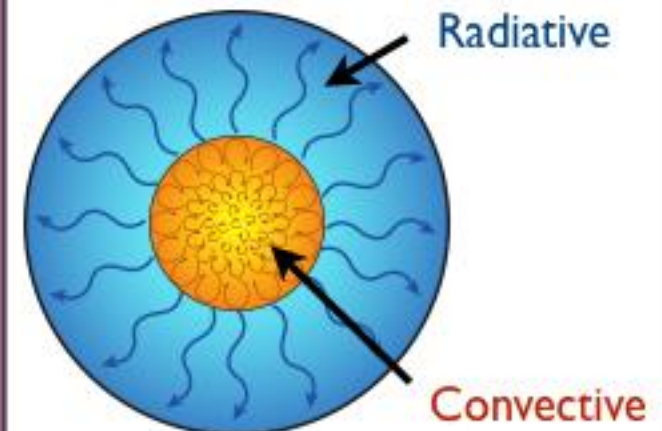
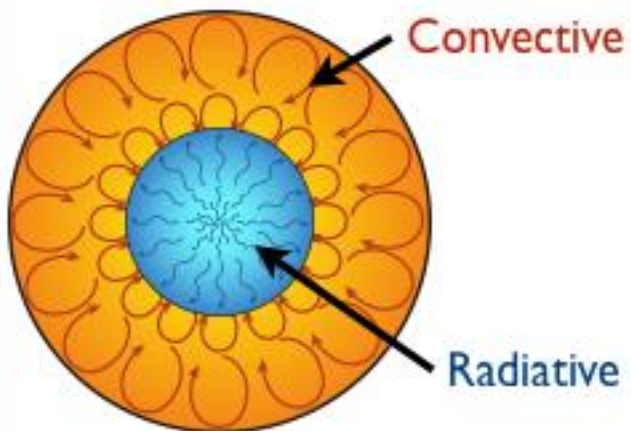
Topologically complex



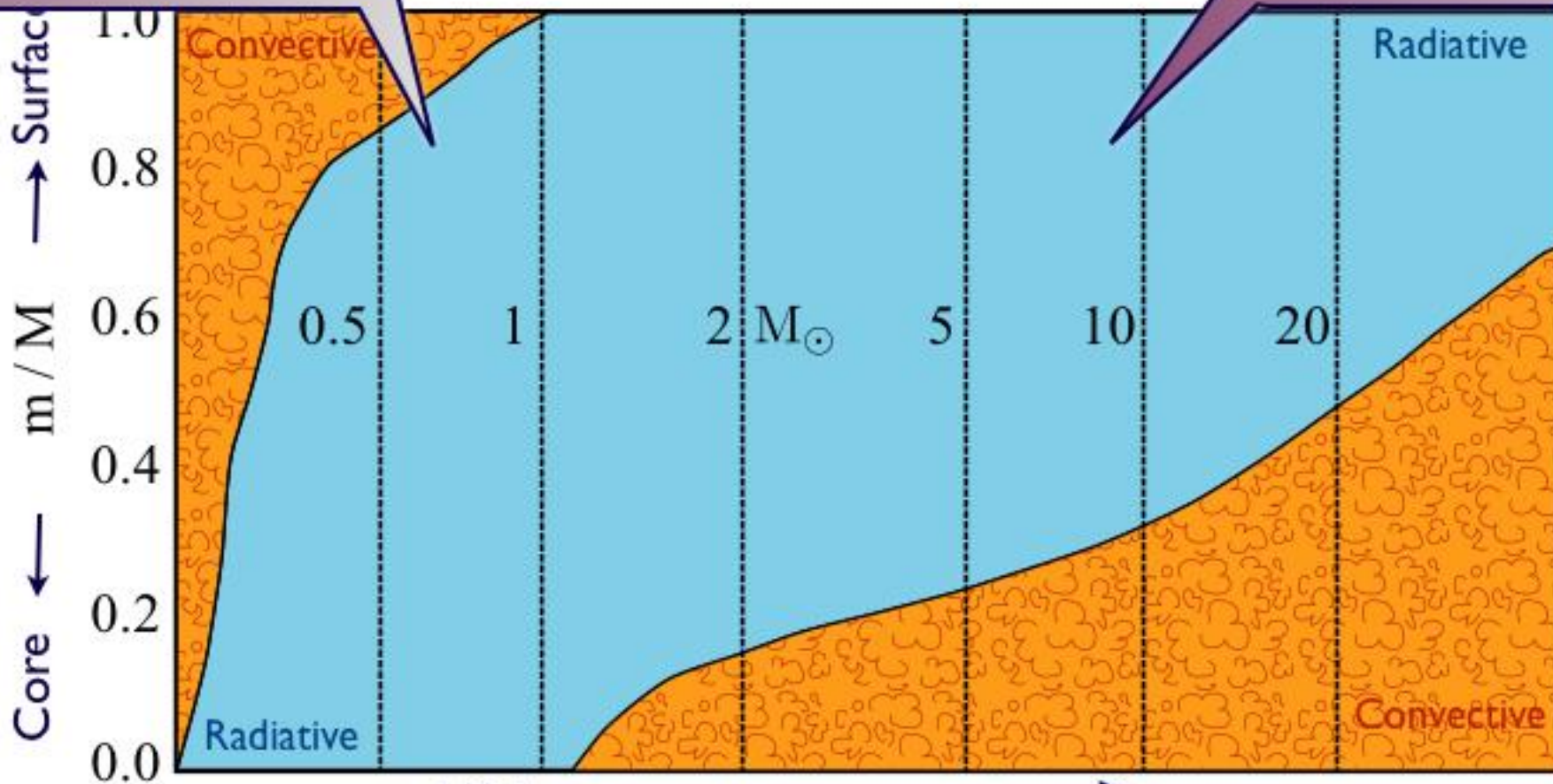
Dynamic on various timescales (hh, dd, yy)



Where do we find stellar magnetism?



Stellar interiors

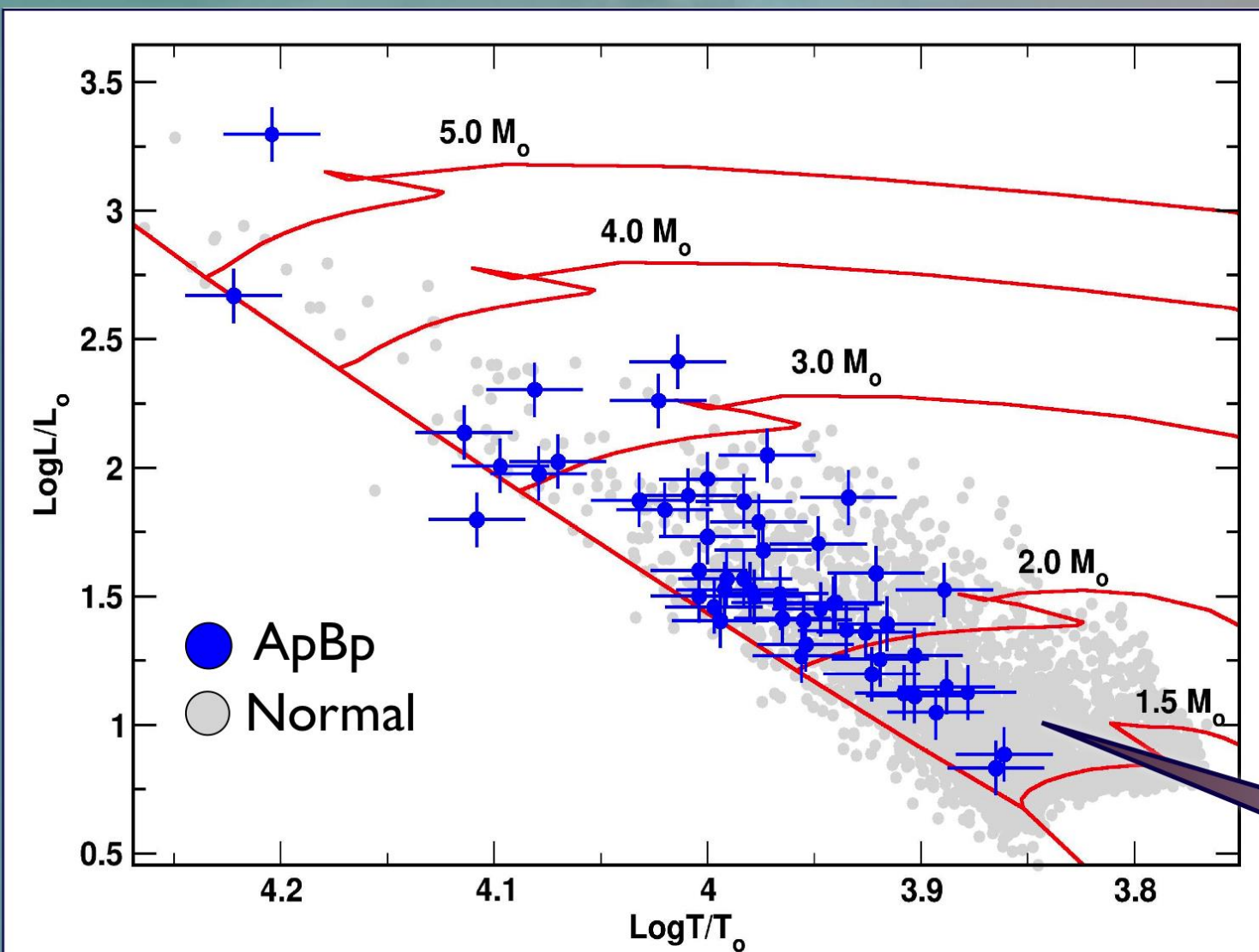


Higher mass stars →

Kippenhahn & Weigert 1990

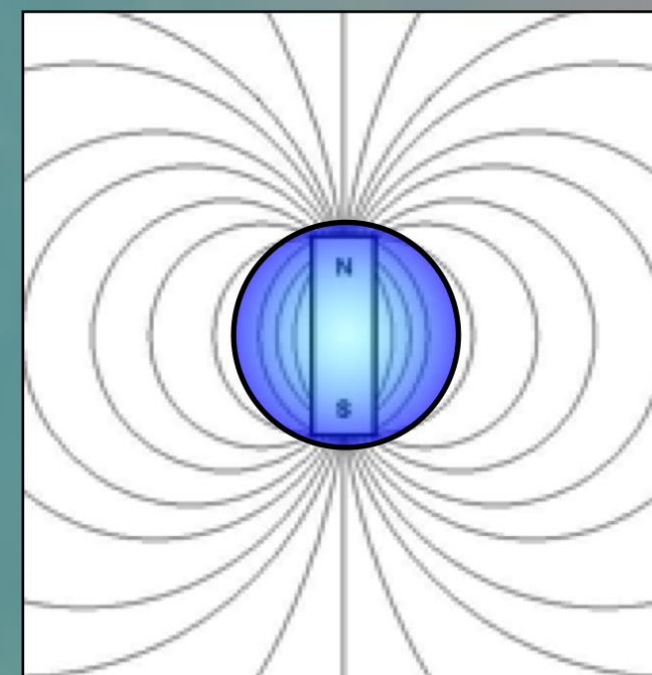
Chemically Peculiar Magnetic ApBp Stars

Volume limited (100pc) sample of A- and late-B stars



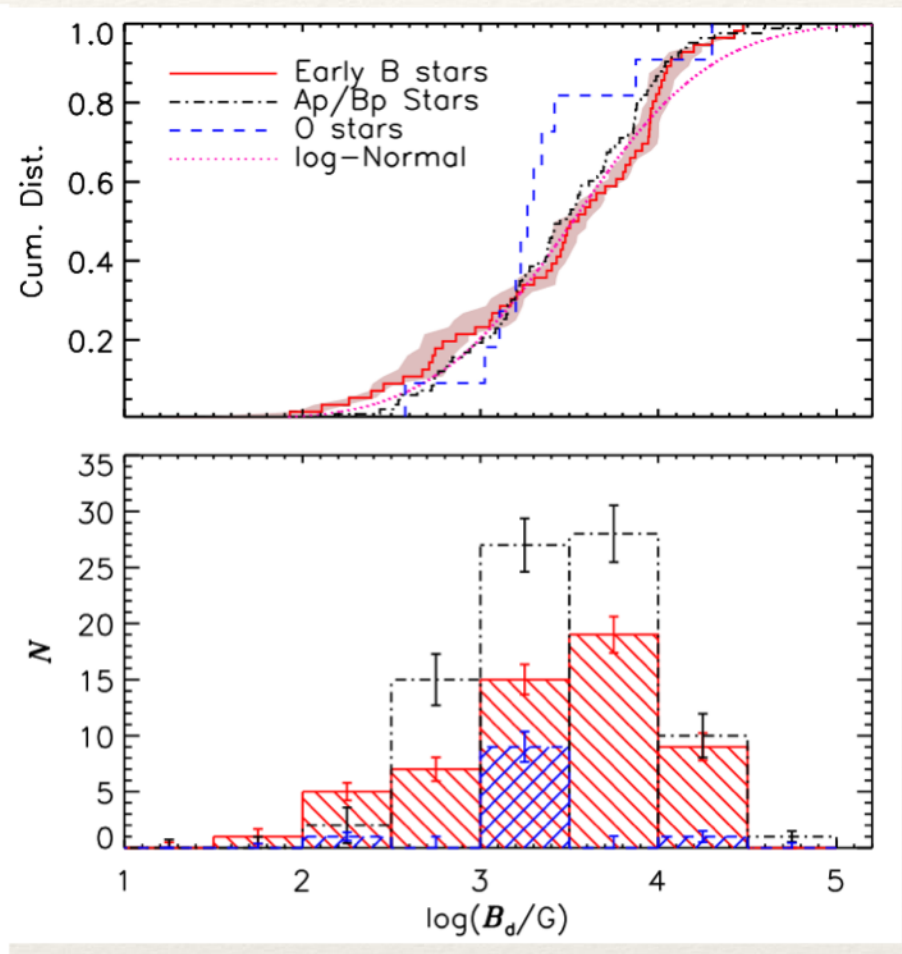
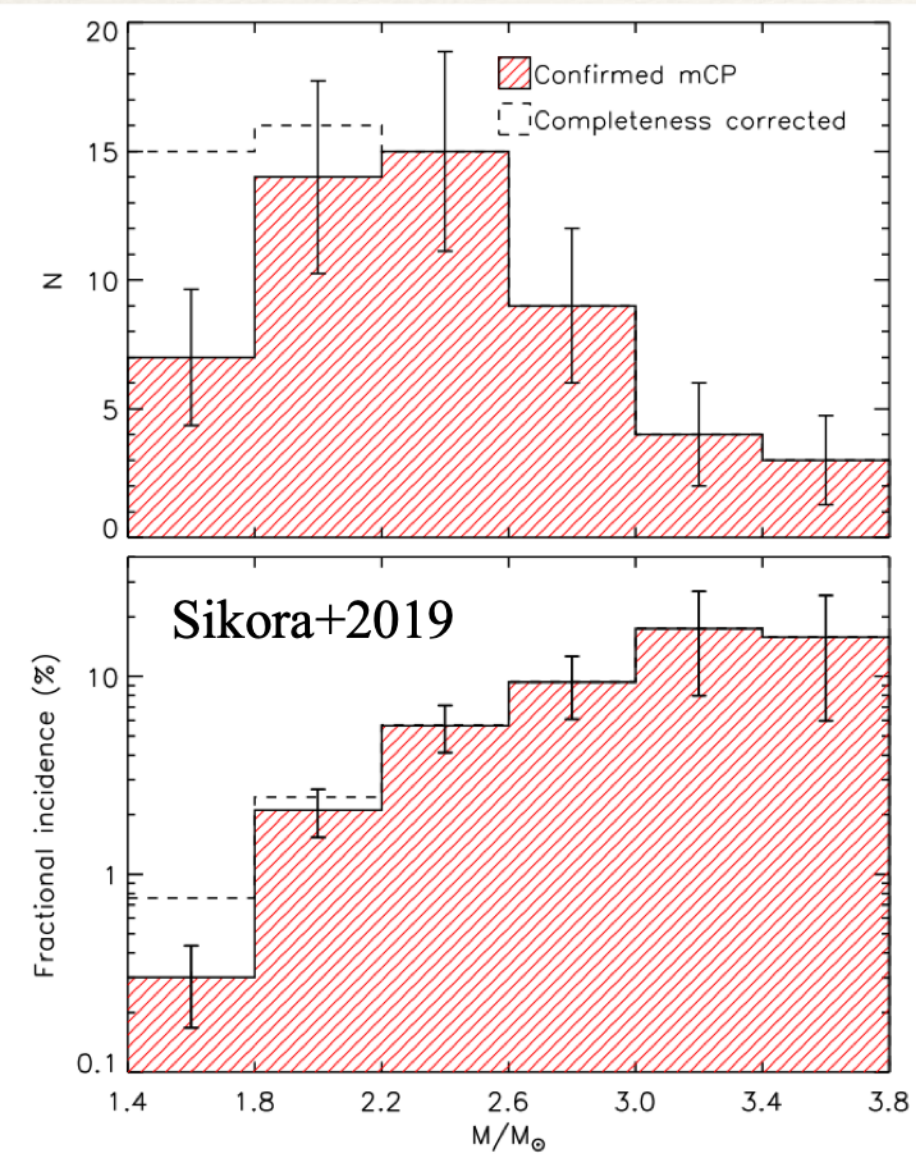
Power et al. (2007)

- ▶ Strong (kG)
- ▶ Large-scale

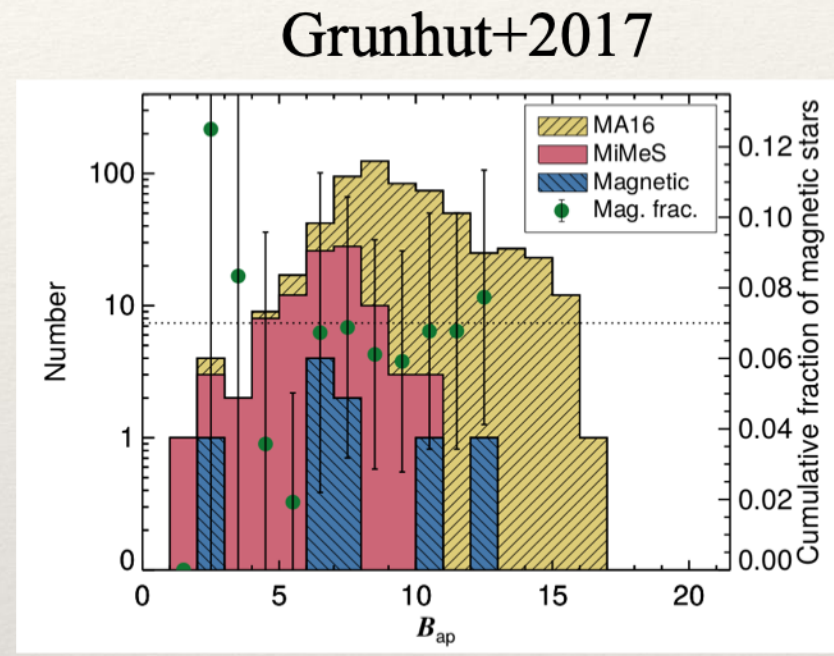


Incidence: 10%

About 10% of massive stars are magnetic.

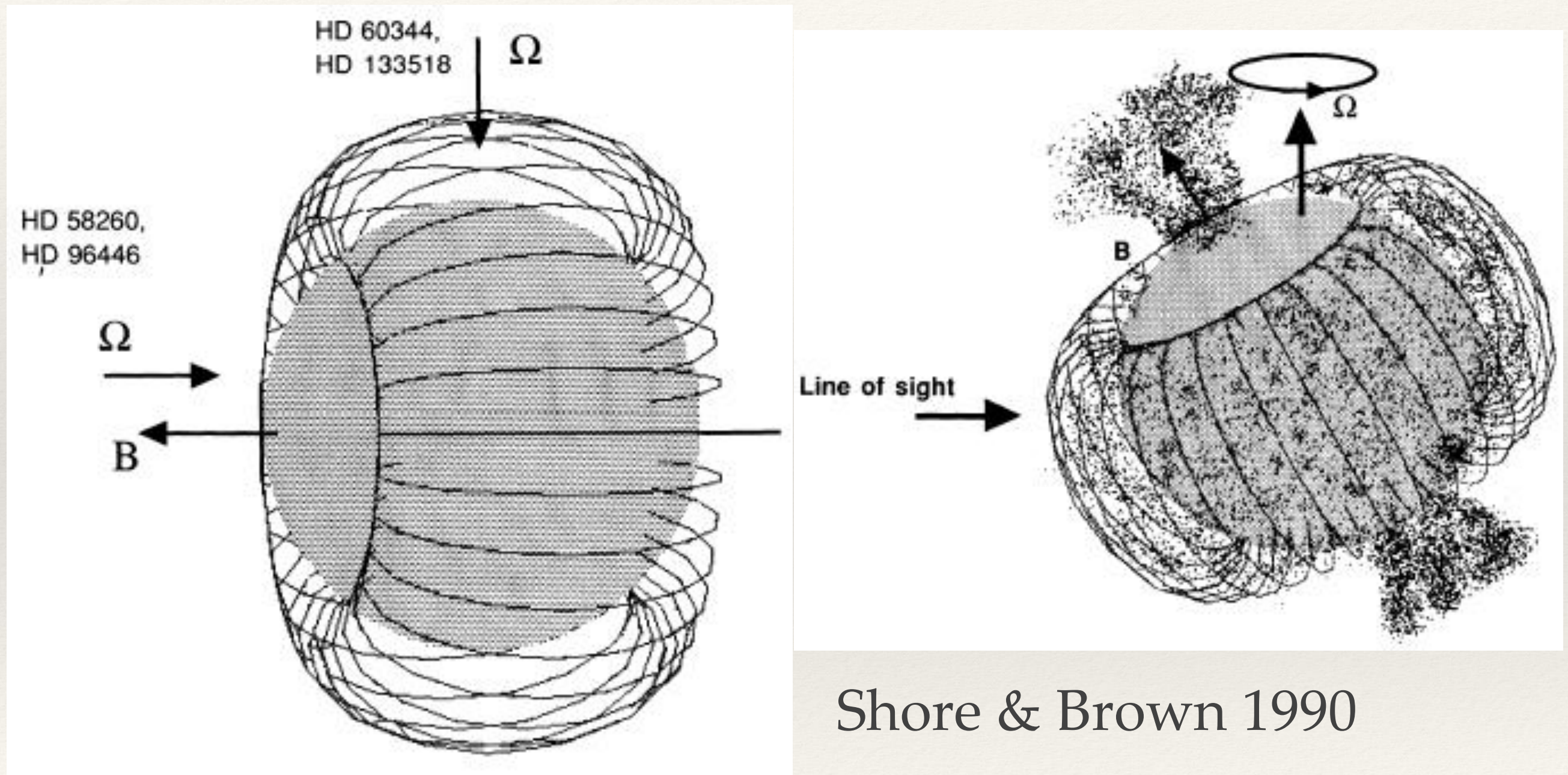


Shultz+2019a



How do we model these
magnetic winds?

Wind confinement in magnetic B-stars



Shore & Brown 1990

Wind confinement in magnetic B-stars



Magnetically Confined Wind-Shocks

Magnetic Ap-Bp stars

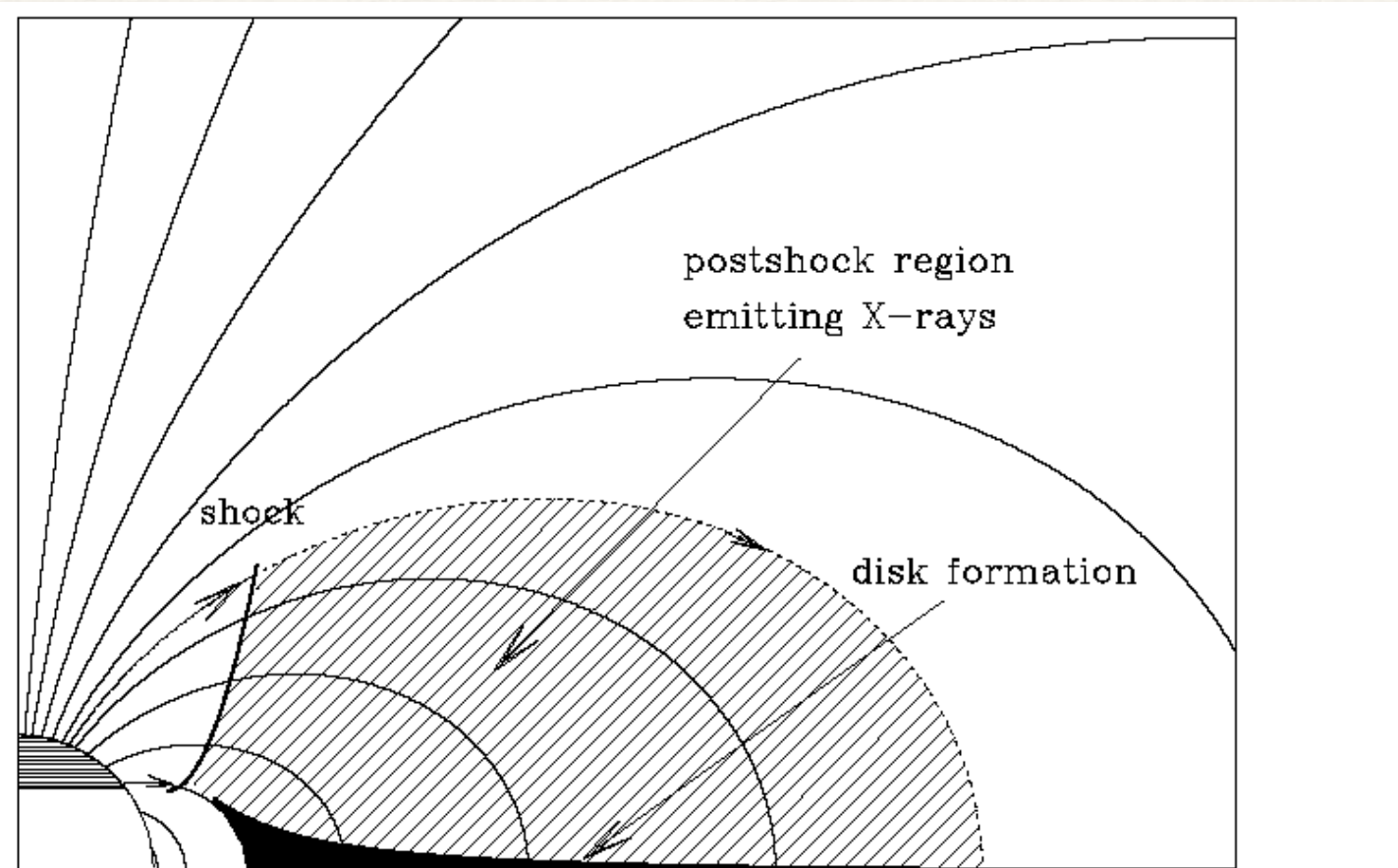


Fig. 7. Schematic view of the model proposed for the X-ray emission from IQ Aur (see text).

Babel & Montmerle 1997

Magnetic Confinement Parameter

$$\frac{\text{magnetic energy density}}{\text{kinetic energy density}} \equiv \eta(r) \equiv \frac{B^2/8\pi}{\rho v^2/2}$$

$$\eta(r) = \frac{B^2 r^2}{M v} = \left[\frac{B_*^2 R_*^2}{M v_\infty} \right] \left[\frac{(r/R_*)^{-2n}}{(1 - (R_*/r))^\beta} \right]$$

η^*

$$\eta_* = \frac{B_0^2 R_*^2}{M v_\infty} = 0.4 \times \frac{B_{100}^2 R_{12}^2}{M_{-6} v_8}$$

for solar wind, $\eta^* \sim 40$

but for O-stars, to get $\eta^* \sim 1$, need: $B^* \sim 300$ G for ζ Pup

Computing Alfven Radius

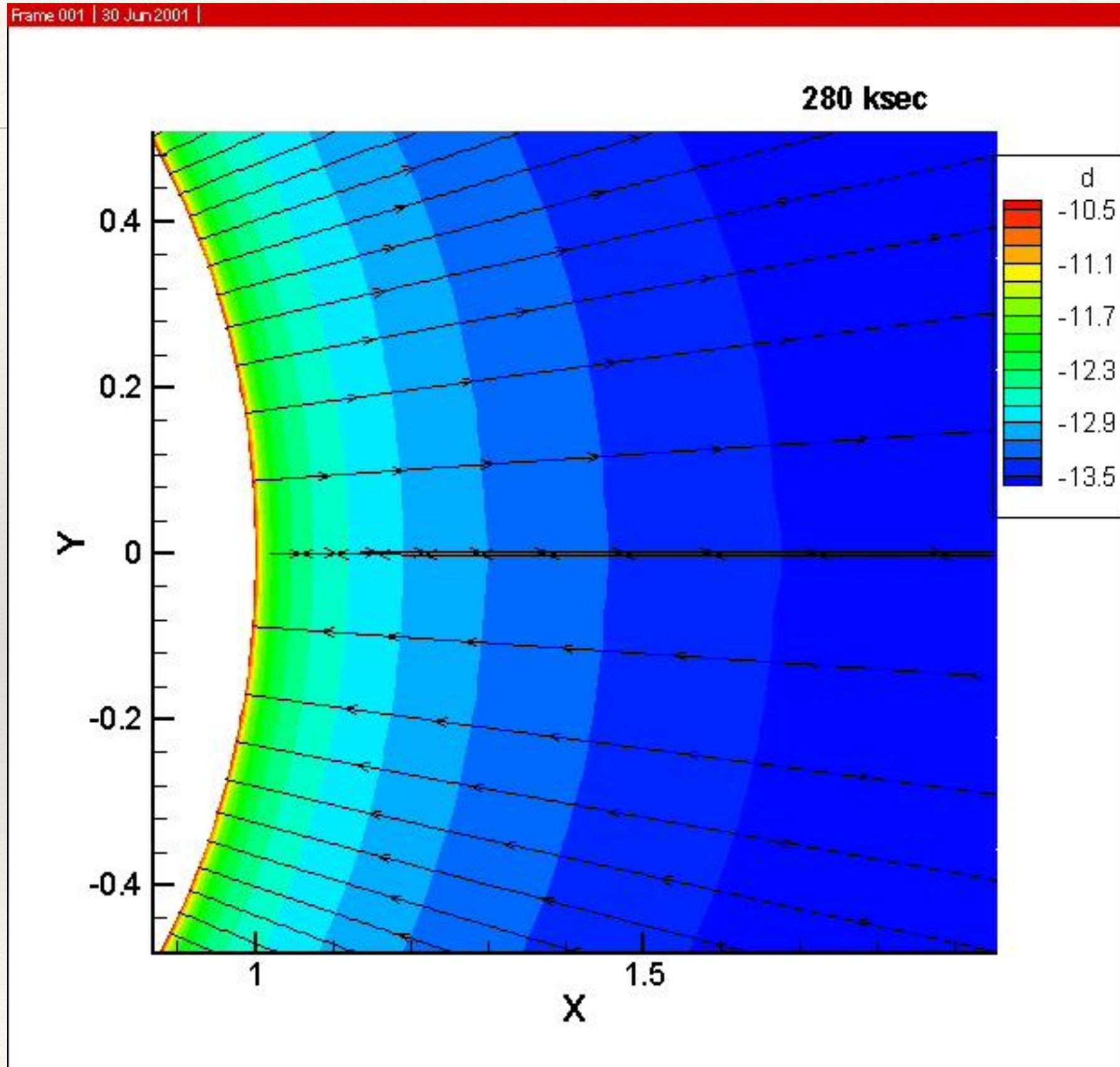
$$\eta(r) = \eta_* \left[\frac{(r/R_*)^{-2n}}{(1 - (R_*/r))^\beta} \right]^{\beta \sim 1} \text{ For hot stars,}$$

For a dipole $n=2$

$$\frac{R_A}{R_*} \approx \eta_*^{1/4}$$

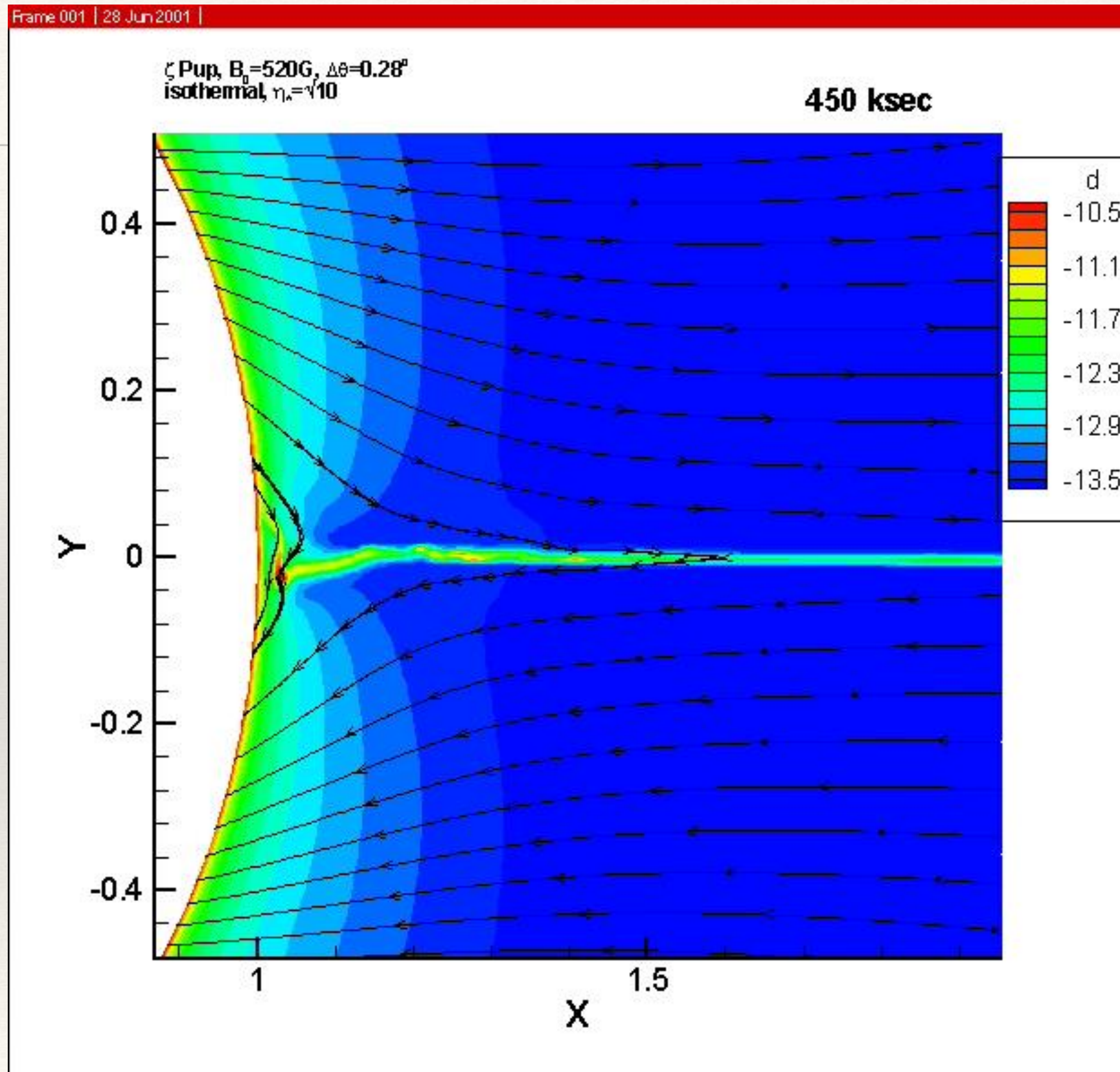
For Moderate Confinement Cases:
MHD

93 G ; $\eta^* = 0.1$

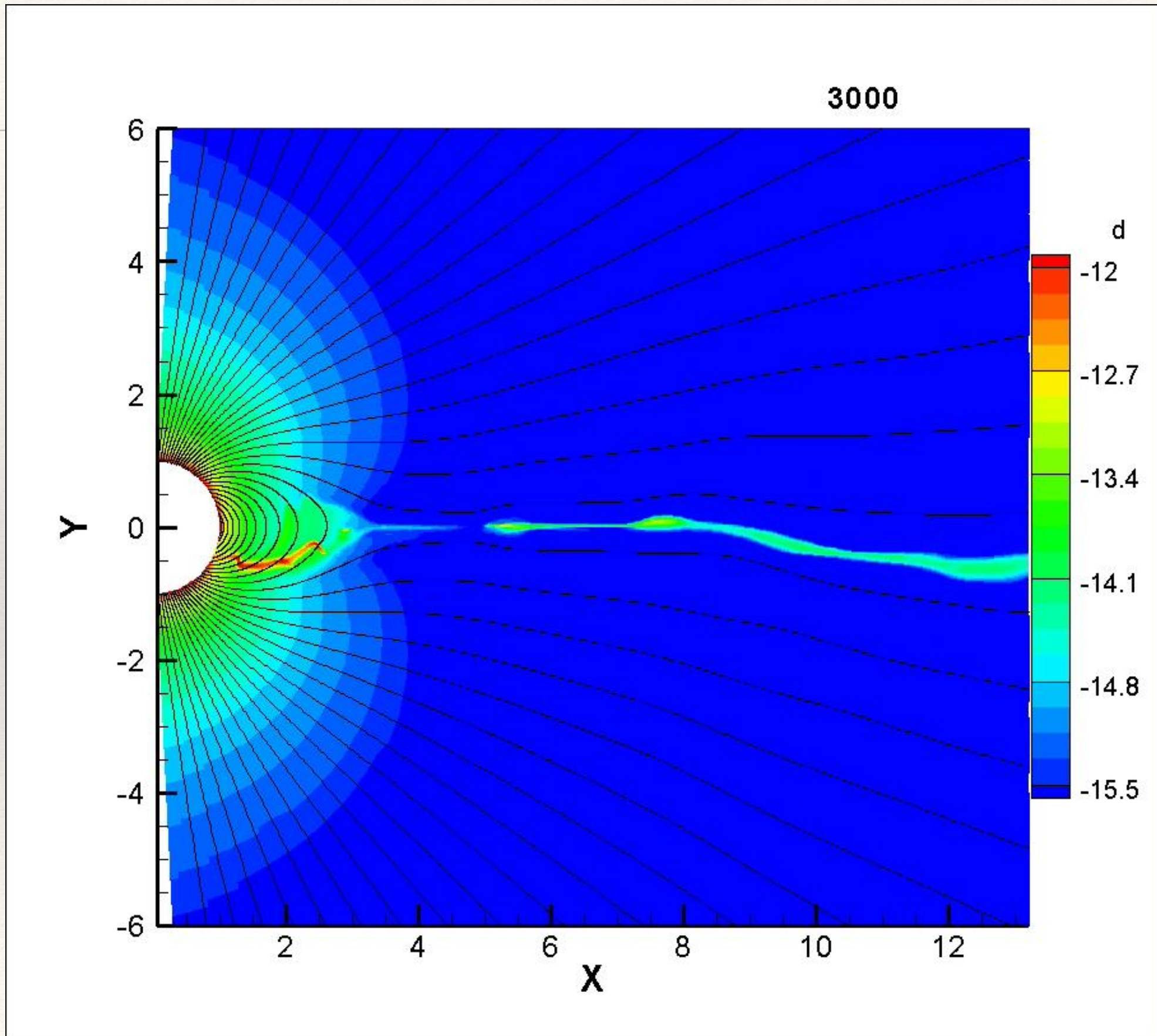


Zeus Code

520 G ; $\eta^* = 3.2$



2950 G ; $\eta^* = 100$



Magnetic confinement vs. Wind + Rotation

Wind mag. confinement

$$\eta_* = \frac{B_*^2 R_*^2}{\dot{M} v_\infty}$$

Alfven radius

$$R_A = \eta_*^{1/4} R_*$$

Rotation vs. critical

$$W = \frac{V_{rot}}{\sqrt{GM/R_*}}$$

Kepler radius

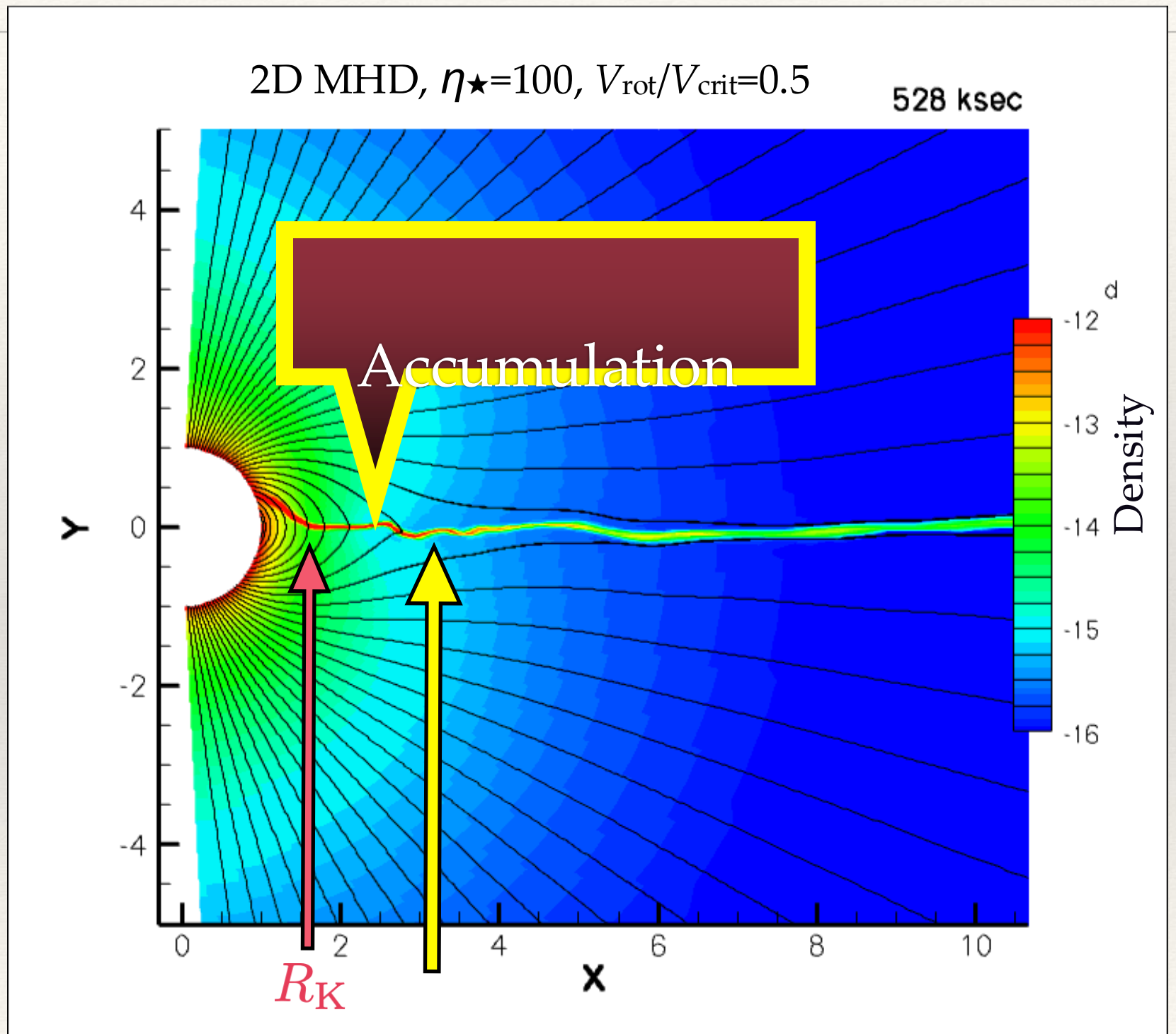
$$R_K = W^{-2/3} R_*$$

Centrifugal support

$$W = \frac{V_{rot}}{V_{crit}}$$

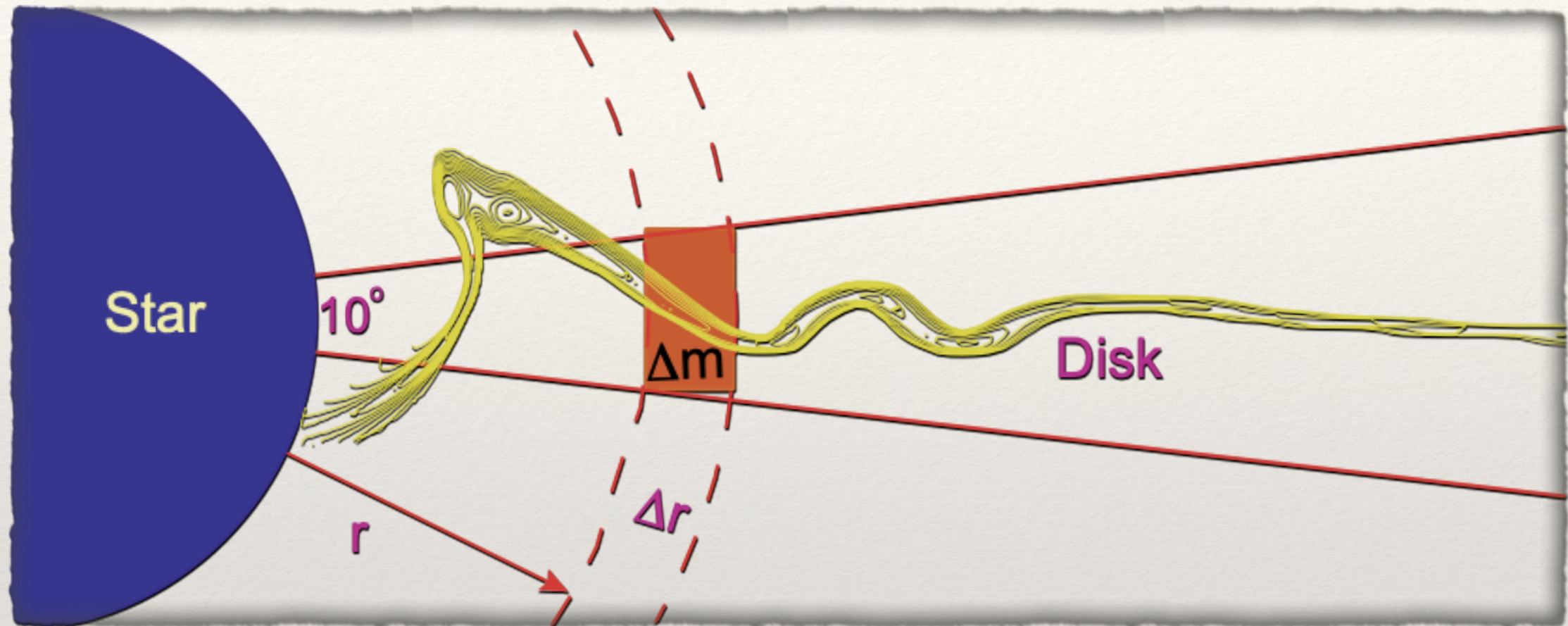
$$\frac{R_K}{R_*} \equiv W^{-2/3}$$

Kepler radius



$$R_A \propto \eta_{\star}^{1/4}$$

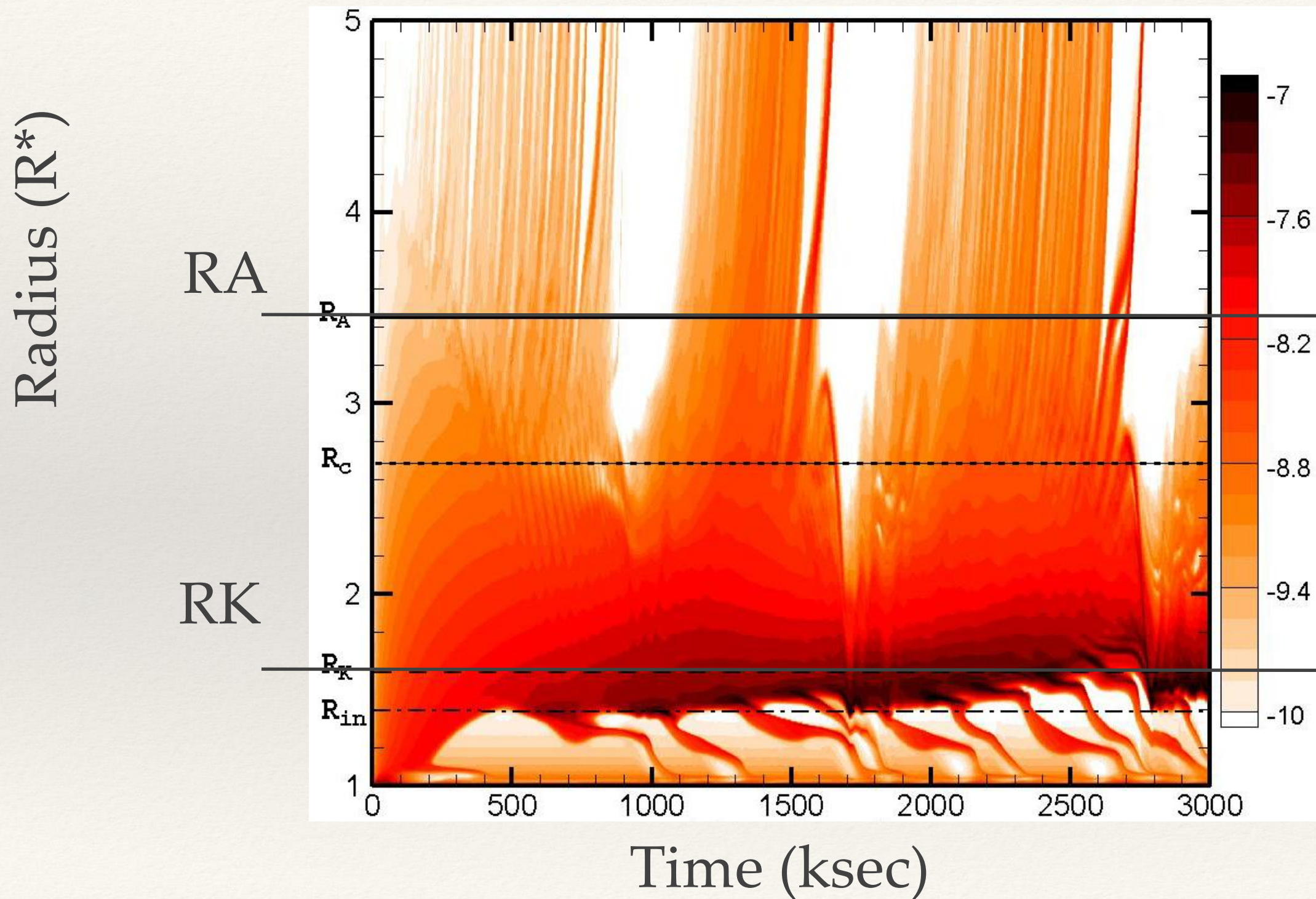
Radial Mass Distribution



$$\frac{dm_e(r, t)}{dr} \equiv 2\pi r^2 \int_{\pi/2 - \Delta\theta/2}^{\pi/2 + \Delta\theta/2} \rho(r, \theta, t) \sin \theta d\theta$$

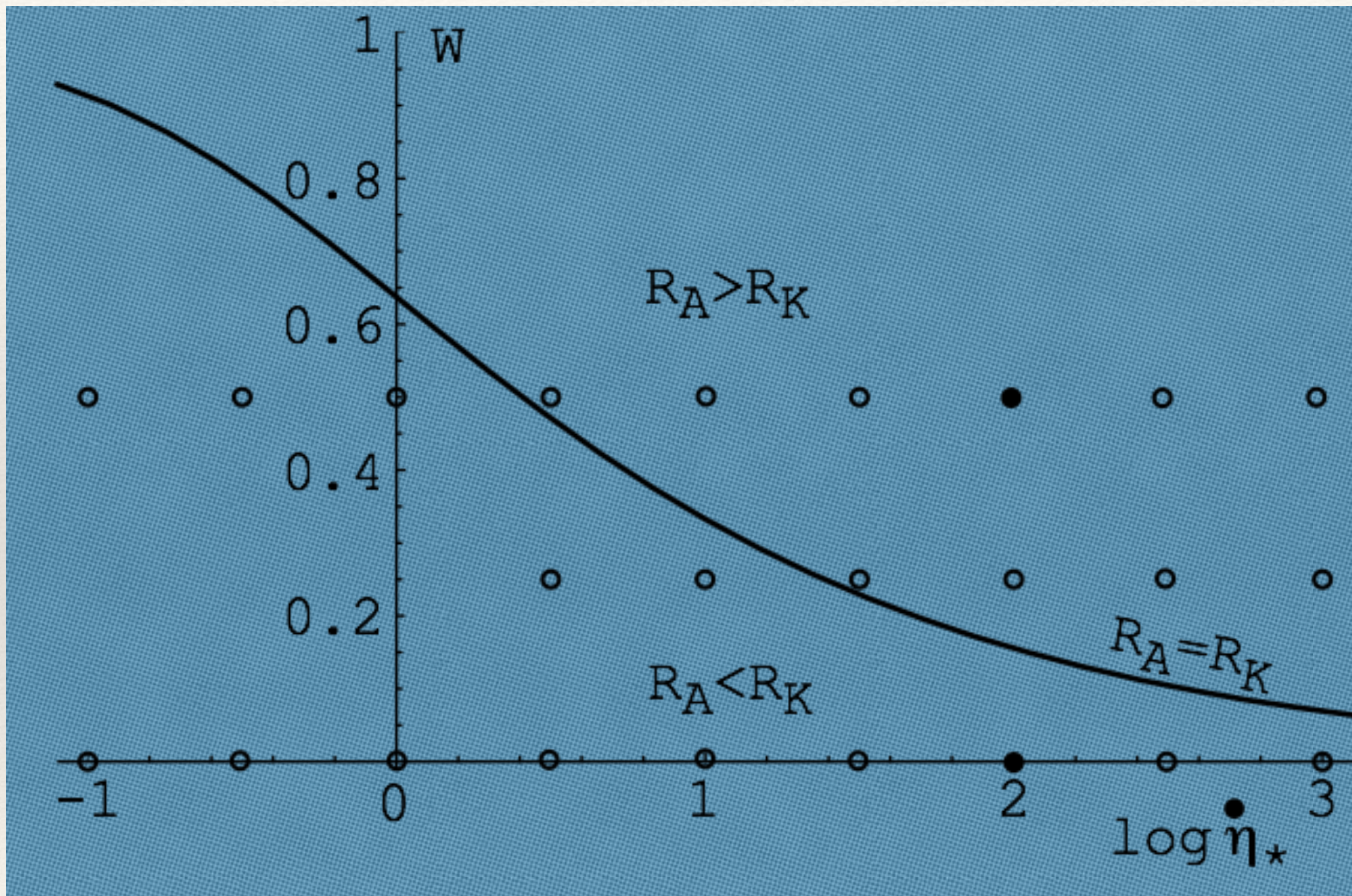
Time evolution of Radial distribution of equatorial disk mass

$$\eta^* = 100 \quad \& \quad V_{\text{rot}}/V_{\text{crit}} = 1/2$$



Two Parameter Study

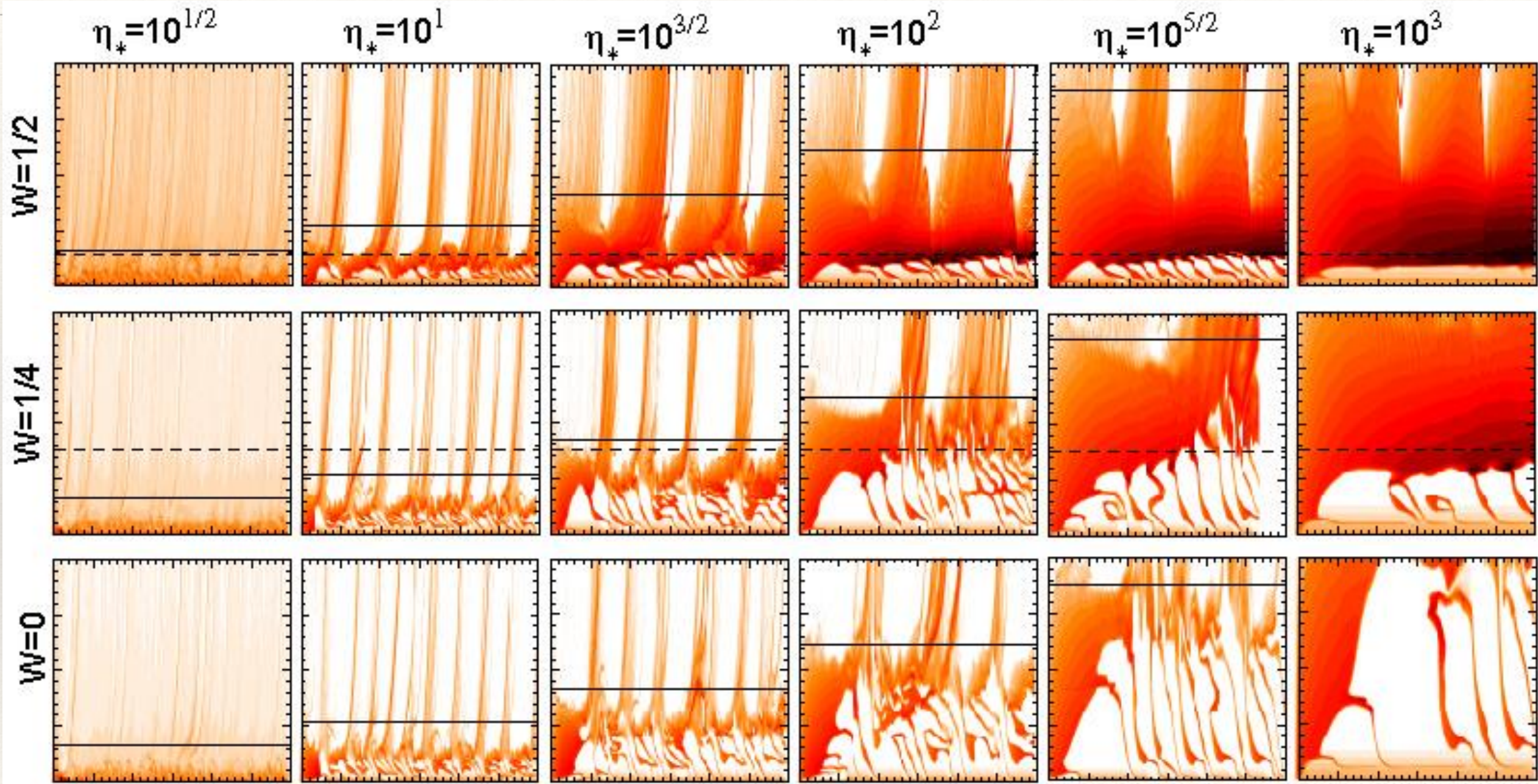
More Rapid Rotation \dashrightarrow



Stronger Magnetic Confinement \dashrightarrow

Radial Distribution of equatorial disk mass

More Rapid Rotation \dashrightarrow



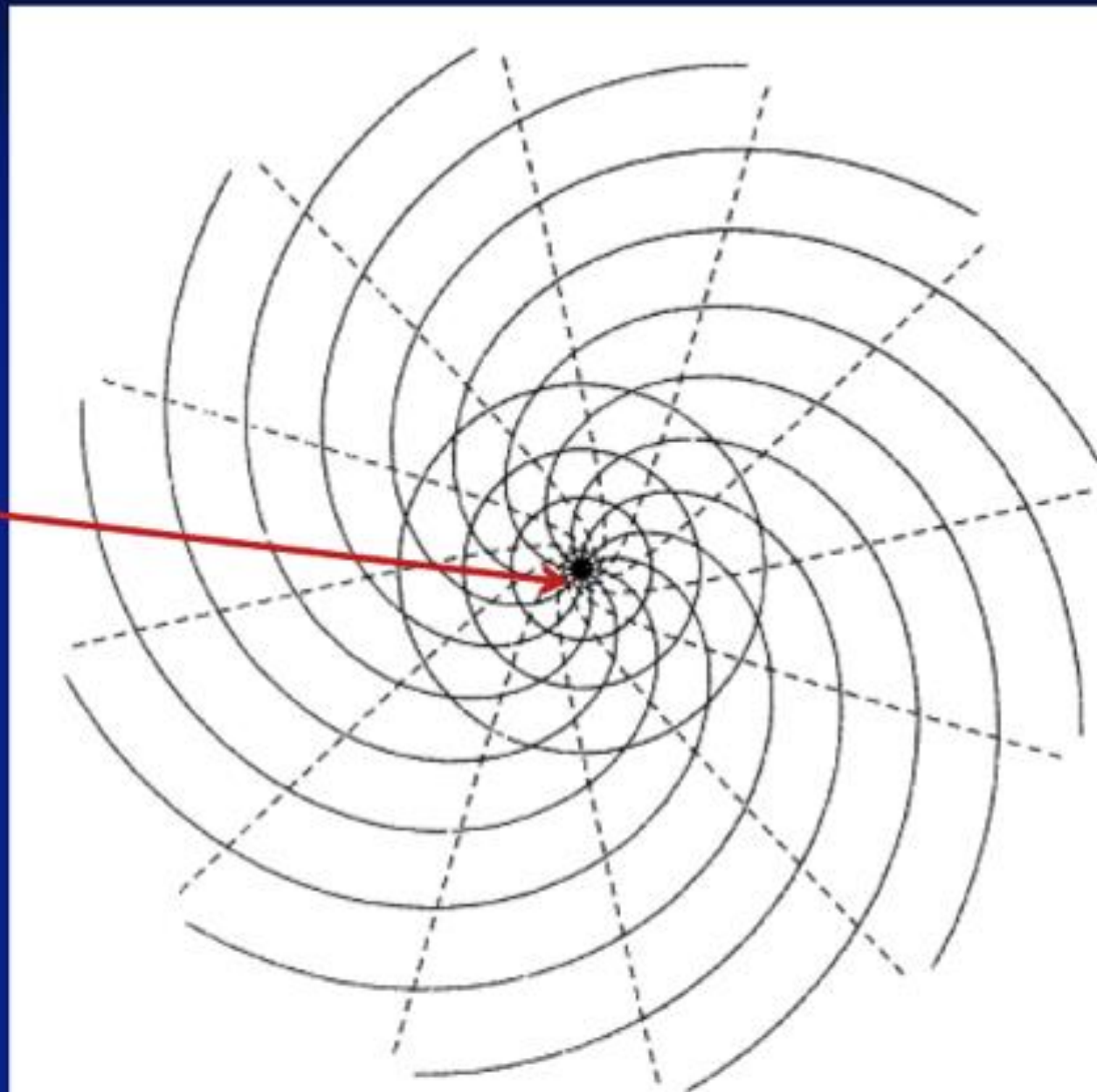
Stronger Magnetic Confinement \dashrightarrow

What are the implications?

Angular Momentum Loss

Weber and Davis (1967)

Monopole field at
solar surface



Spindown

contribution from both field and gas

$$\dot{J} = \frac{2}{3} \dot{M} \Omega R_A^2$$

For Dipole

$$\tau_{spin} \equiv \frac{J}{\dot{J}} \approx \frac{\frac{3}{2} I}{M R_*^2} \frac{M}{\dot{M}} \frac{1}{\sqrt{\eta_*}} = \tau_{mass} \frac{\frac{3}{2} k}{\sqrt{\eta_*}}$$

$$\frac{\tau_{spin}}{\tau_{mass}} = \frac{0.15}{\sqrt{\eta_*}}$$

Spindown Time

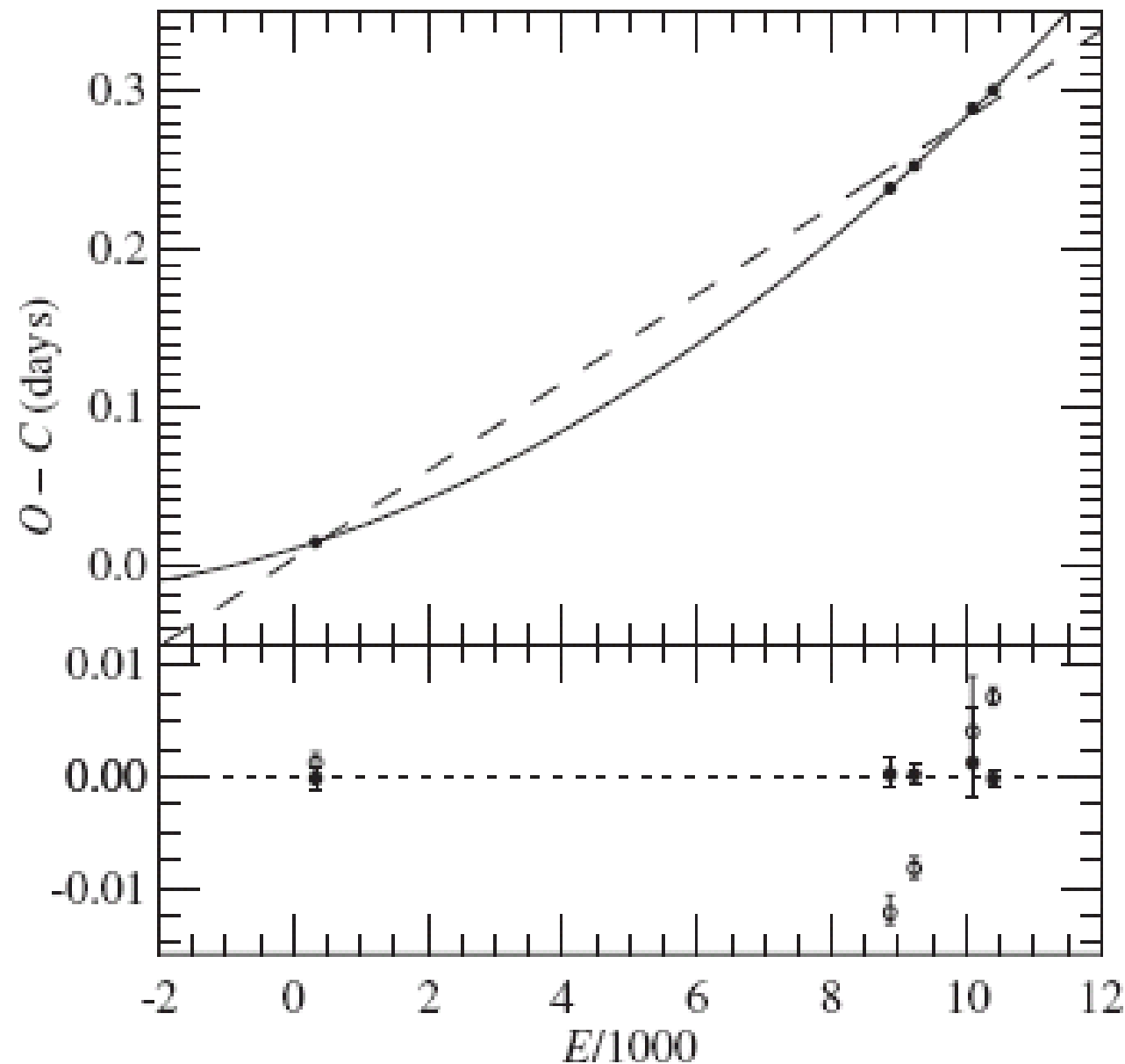
Table 1. Estimated spin-down time for selected known magnetic stars.

Star ^a	M/M_{\odot}	R_{*}/R_{\odot}	P (d)	k	\dot{M} ($10^{-9} M_{\odot} \text{ yr}^{-1}$)	v_{∞} (1000 km s^{-1})	B_p (kG)	η_{*}	τ_{spin} (Myr)
θ^1 Ori C ¹	40	8	15.4	0.28	400	2.5	1.1	15.7	8
HD191612 ²	40	18	538	0.17	6100	2.5	1.6	7.6	0.4
ζ Cas ³	8	5.9	5.37	0.1	0.3	0.8	0.34	3200	65.2
σ Ori E ⁴	8.9	5.3	1.2	0.1	2.4	1.46	9.6	1.4×10^5	1.4
ρ Leo ⁵	22	35	7-47	0.12	630	1.1	0.24	20	1.1

^aReferences: ¹Donati et al. (2002); ²Donati et al. (2006); ³Neiner et al. (2003) and Smith & Bohlender (2007); ⁴Krtićka, Kubát & Groote (2006) and ⁵Kholtygin et al. (2007).

ud-Doula et al. 2009

Rotational Braking of σ Ori E



Predicted

$\tau_{\text{spin}}=1.40$ Myr

Measured

$\tau_{\text{spin}}=1.34$ Myr

Figure 3. Observed-minus-corrected diagram for the primary minimum measurements. The solid (dashed) lines indicate the best-fit quadratic (linear) models; the residuals relative to these models are shown below the $O - C$ diagram as filled (open) symbols.

Non-isothermal 2D models: X-ray

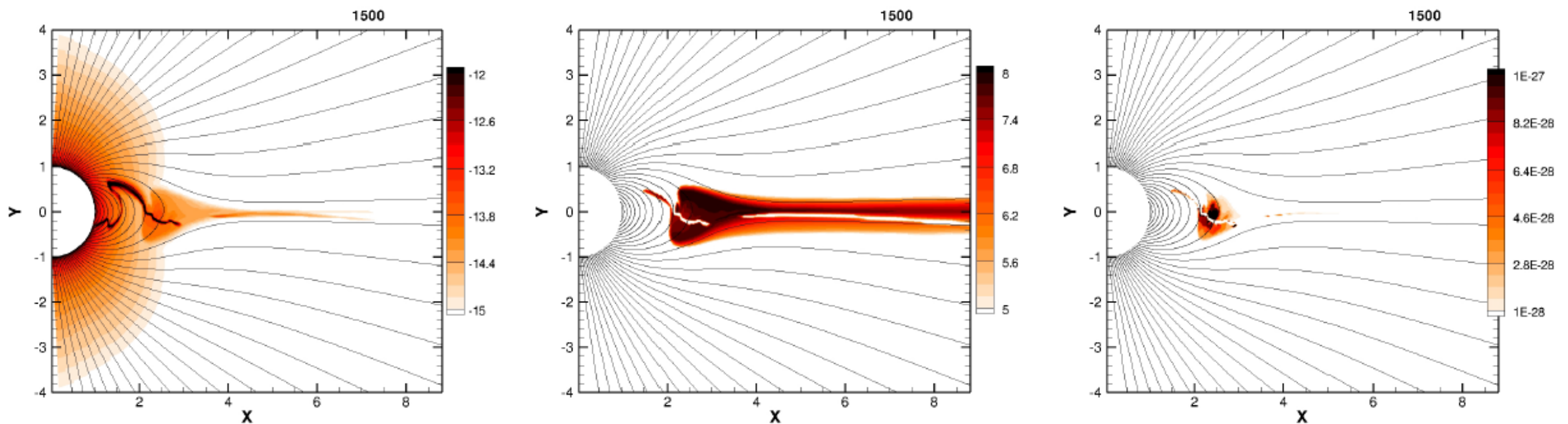
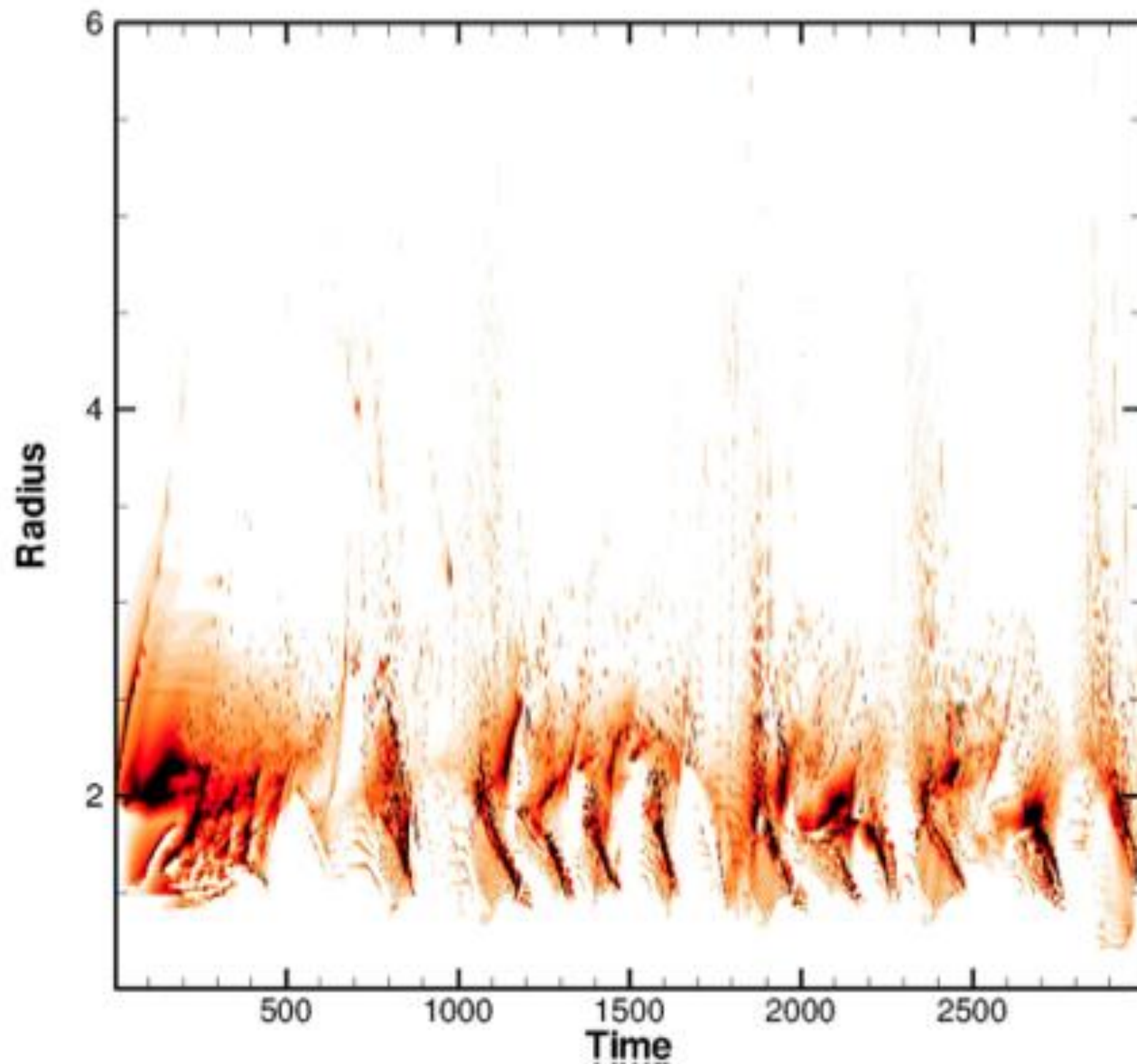


Figure 4. Color plots of log density (left) and log temperature (middle) for arbitrary snapshot of structure in the standard model with $\eta_* = 100$ and no IC cooling. The right panel plots the proxy X-ray emission XEM_{T_x} (weighted by the radius r) from (26), on a *linear* scale for a threshold X-ray temperature $T_x = 1.5$ MK.

X-ray Emission Measure



ud-Doula et al. 2014

X-ray from magnetic stars

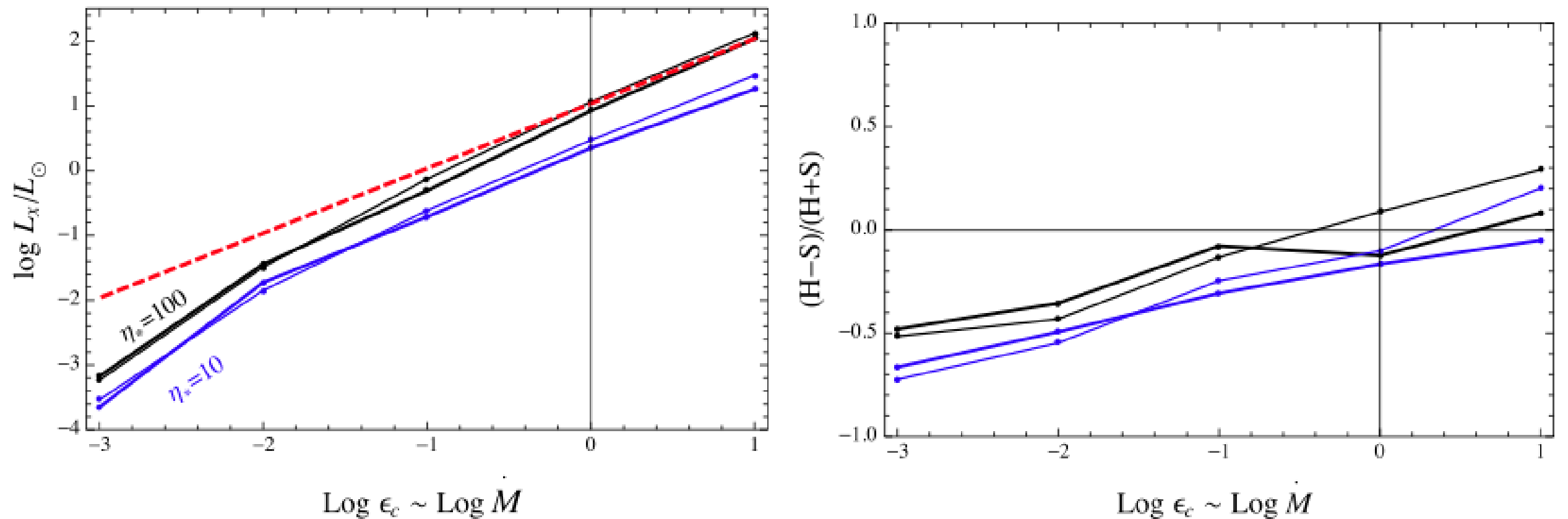
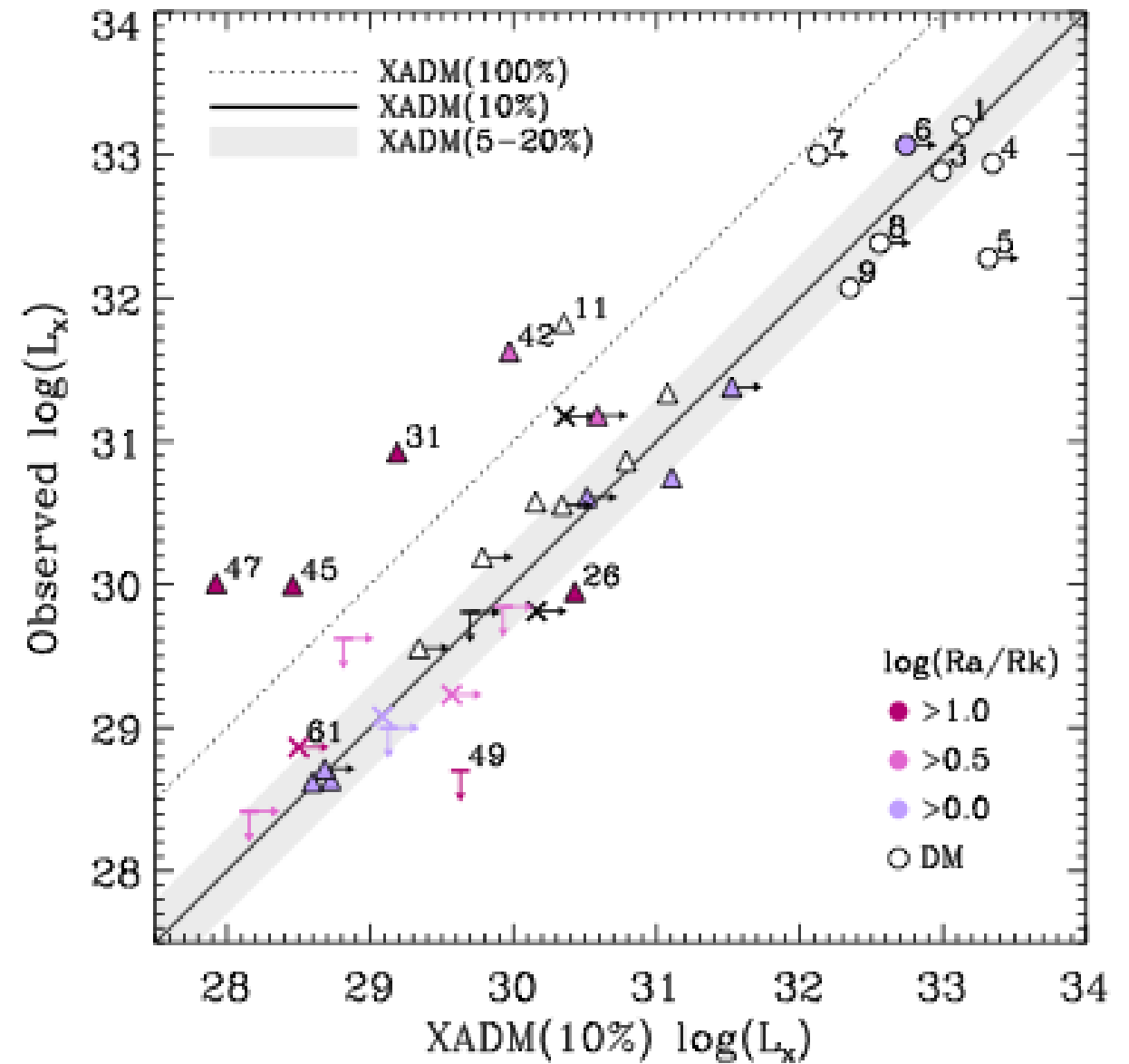
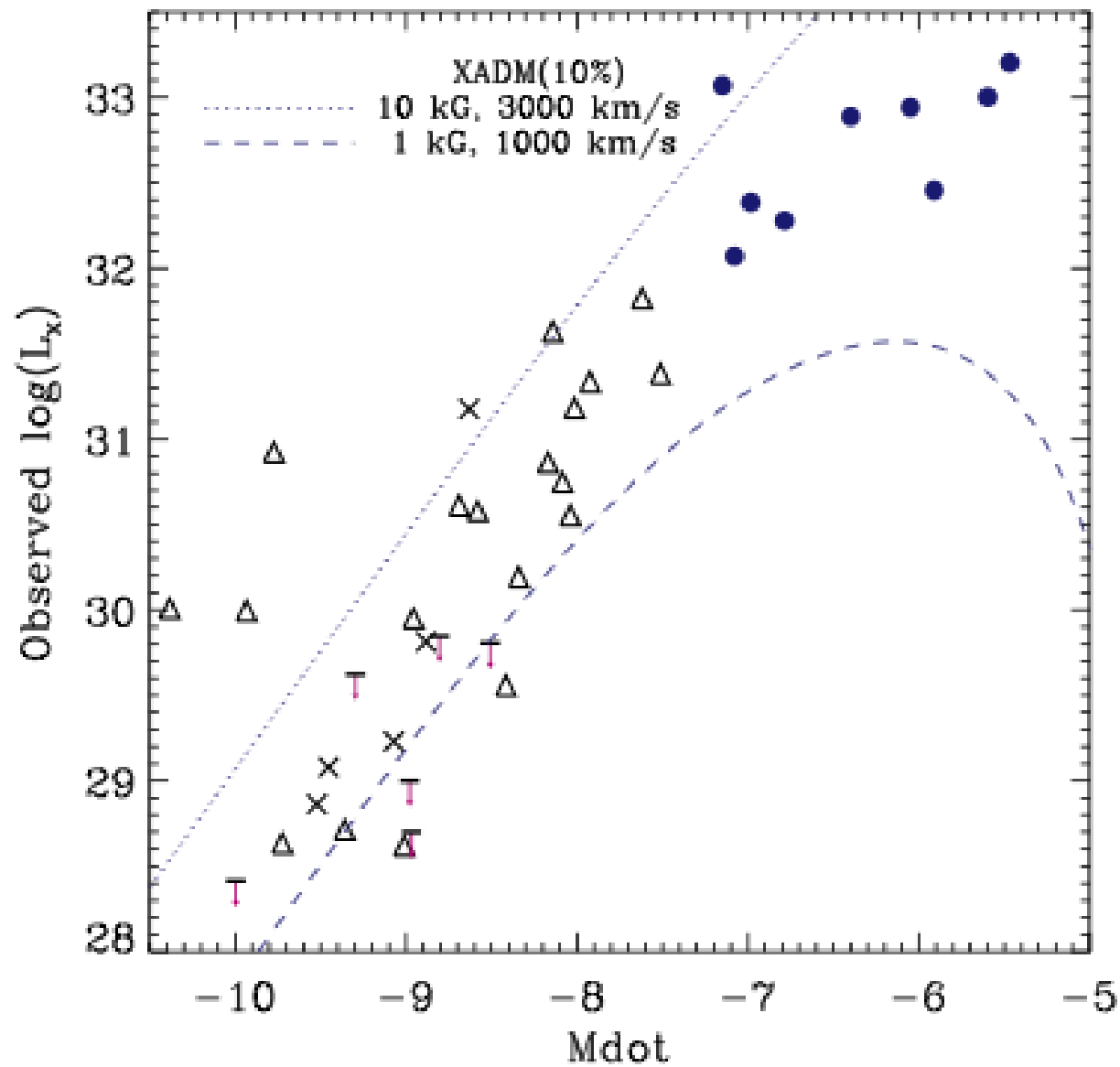


Figure 9. Left: log of time-averaged X-ray luminosity, $\log L_x$, for X-rays above $E_x = 0.3$ keV, plotted versus log of cooling efficiency $\log \epsilon_c$, which acts as a proxy for mass-loss rate \dot{M} . The upper (black) and lower (blue) curves are, respectively, for $\eta_* = 100$ and $\eta_* = 10$, and the thick and normal thickness lines represent models with and without IC cooling. The dashed red line shows a linear relation normalized to values for the $\eta_* = 100$ model with the strongest cooling $\epsilon_c = 10$. Right: analogous plots of hardness ratio $(H-S)/(H+S)$ versus $\log \epsilon_c$, where H represents emission from 1 to 10 keV, and S represents emission from 0.3 to 1 keV.

Observed X-ray

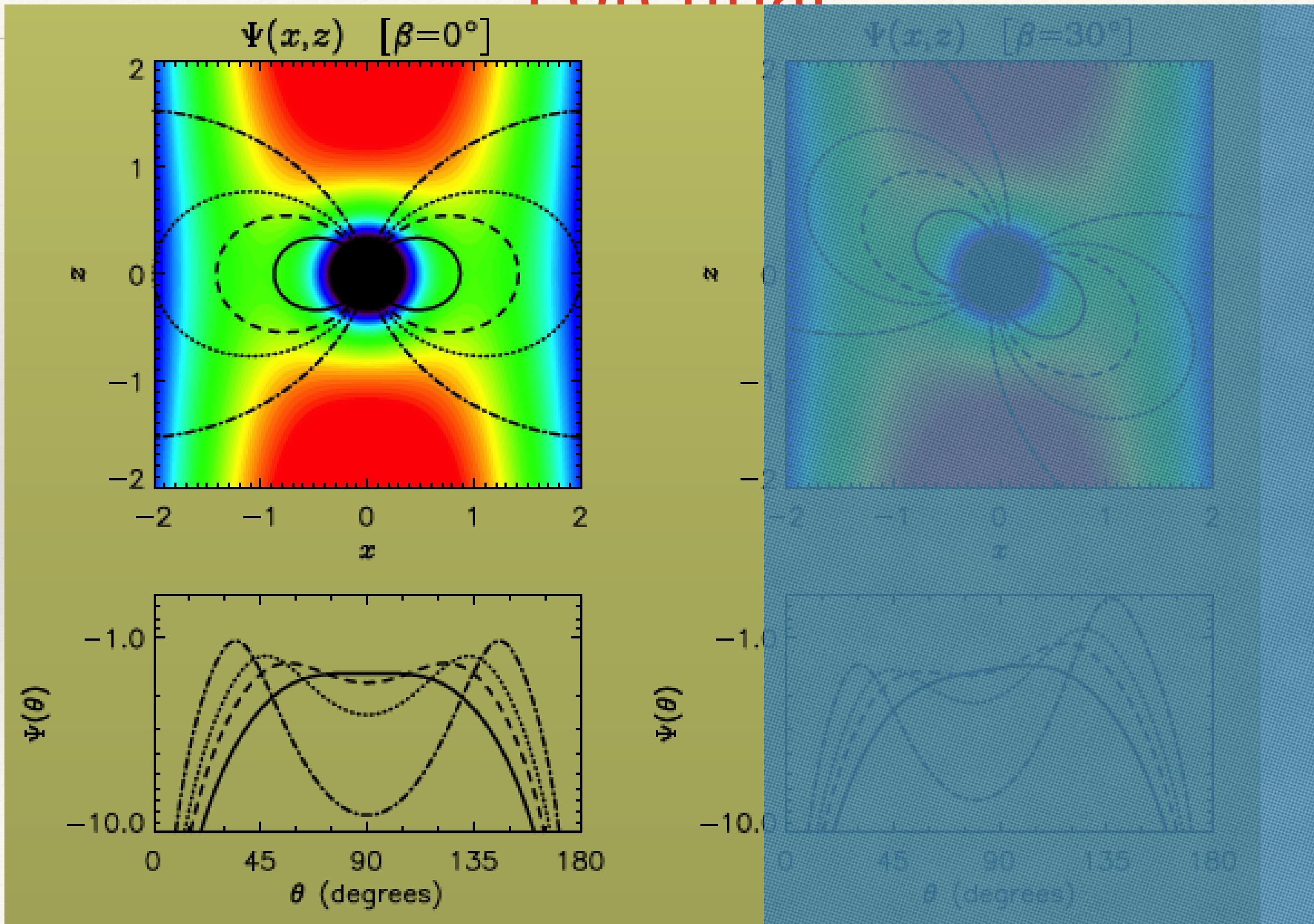


Nazé et al. 2014

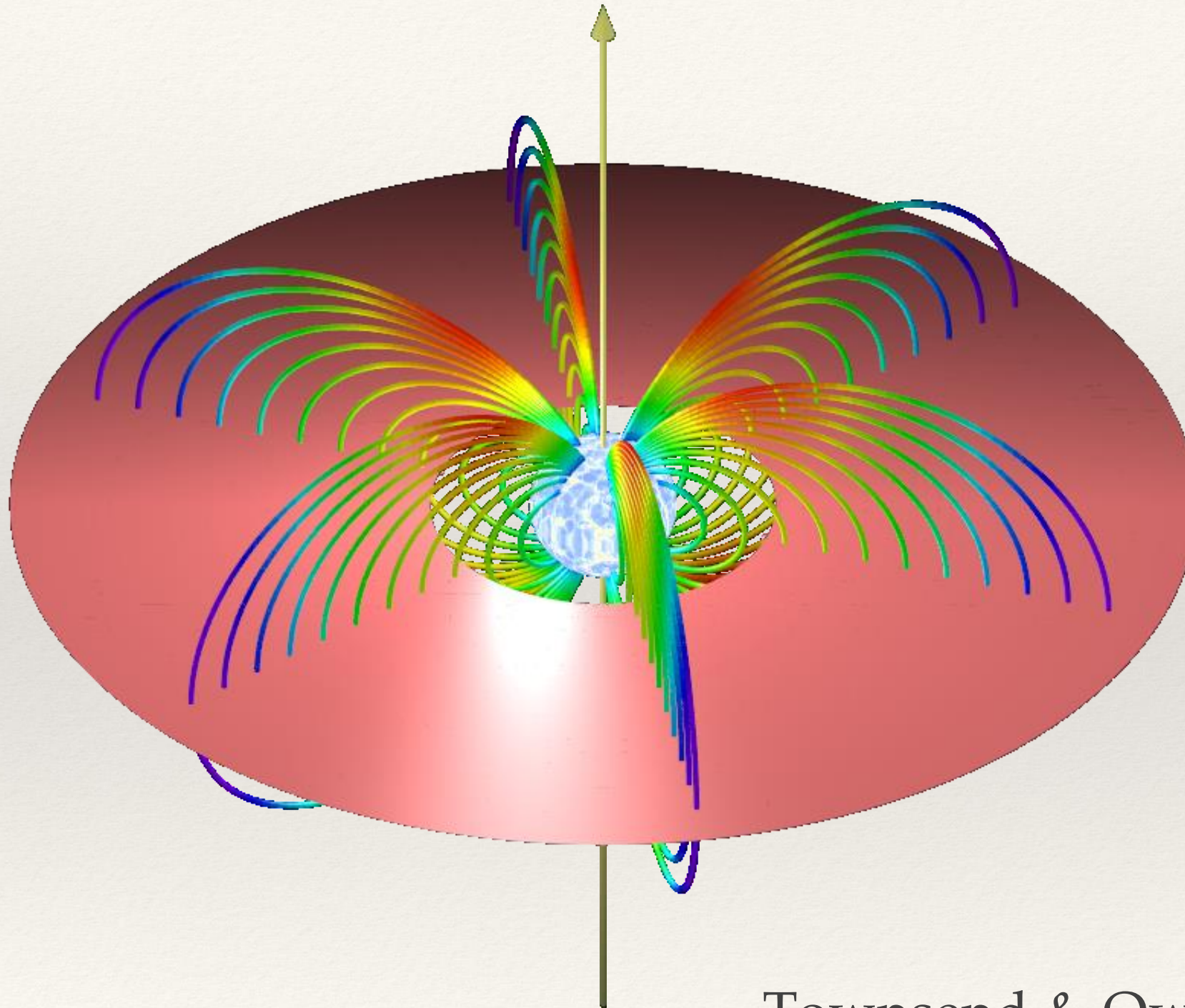
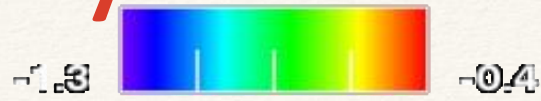
For Strong Confinement Cases

$(\eta^* \gg 1 \rightarrow \infty) : \text{RRM, RFHD, ARFHD}$

Effective Gravitational+Centrifugal Potential



Rigidly Rotating Magnetosphere



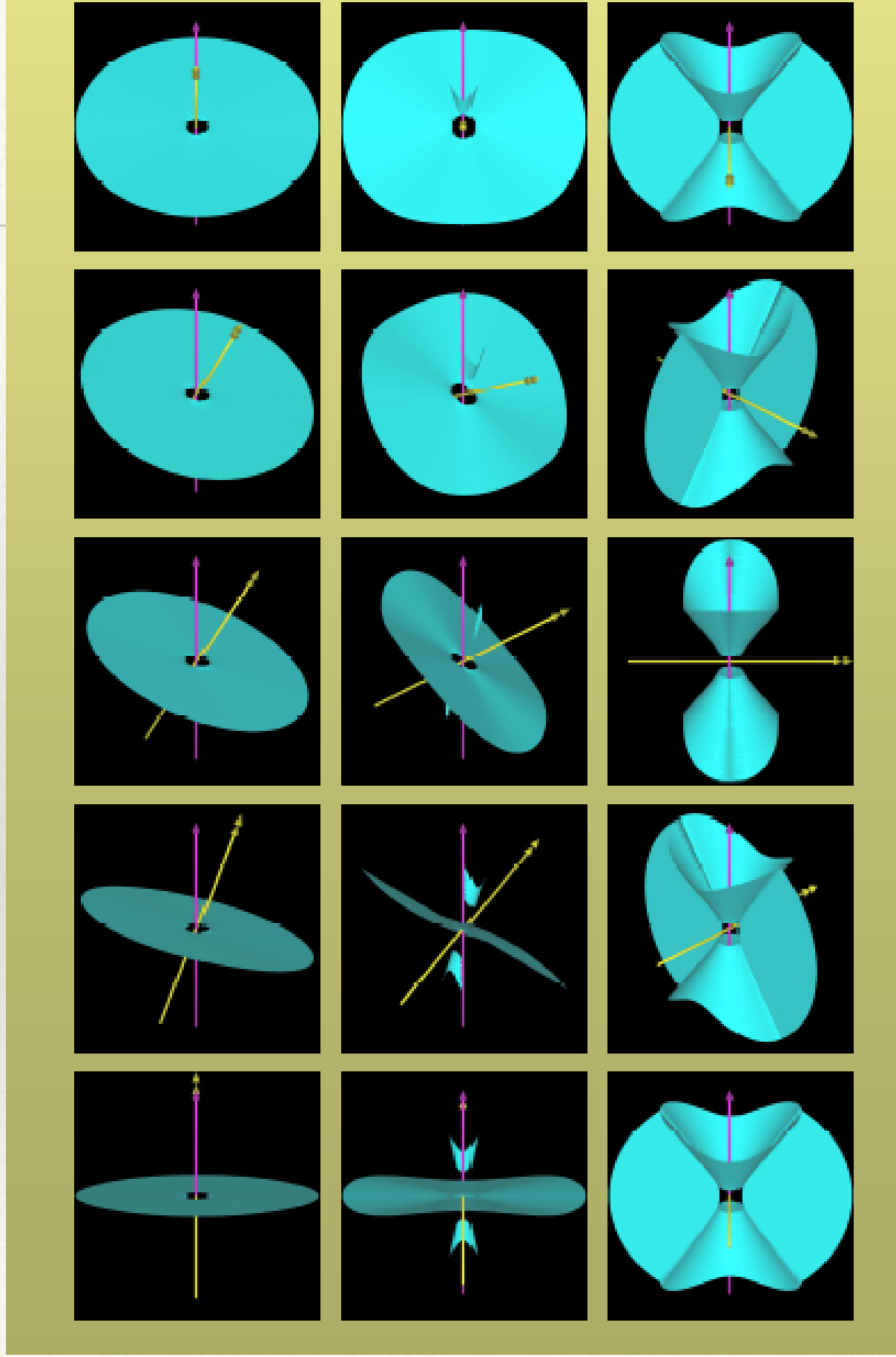
Townsend & Owocki (2005)

$\beta=30^\circ$

$\beta=60^\circ$

$\beta=90^\circ$

Rotational phase \rightarrow



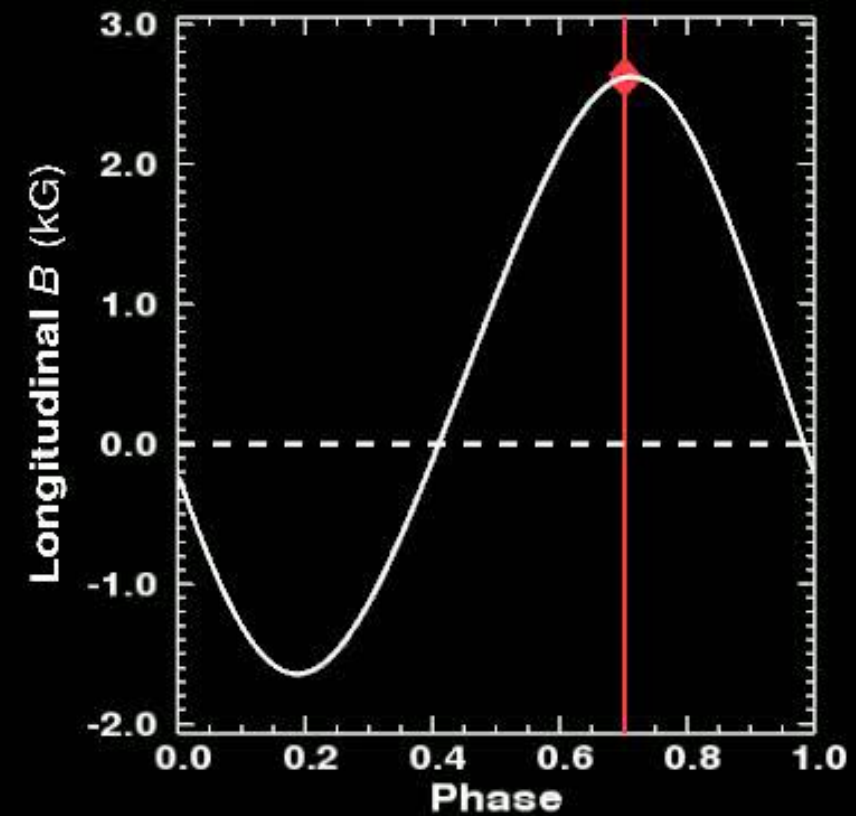
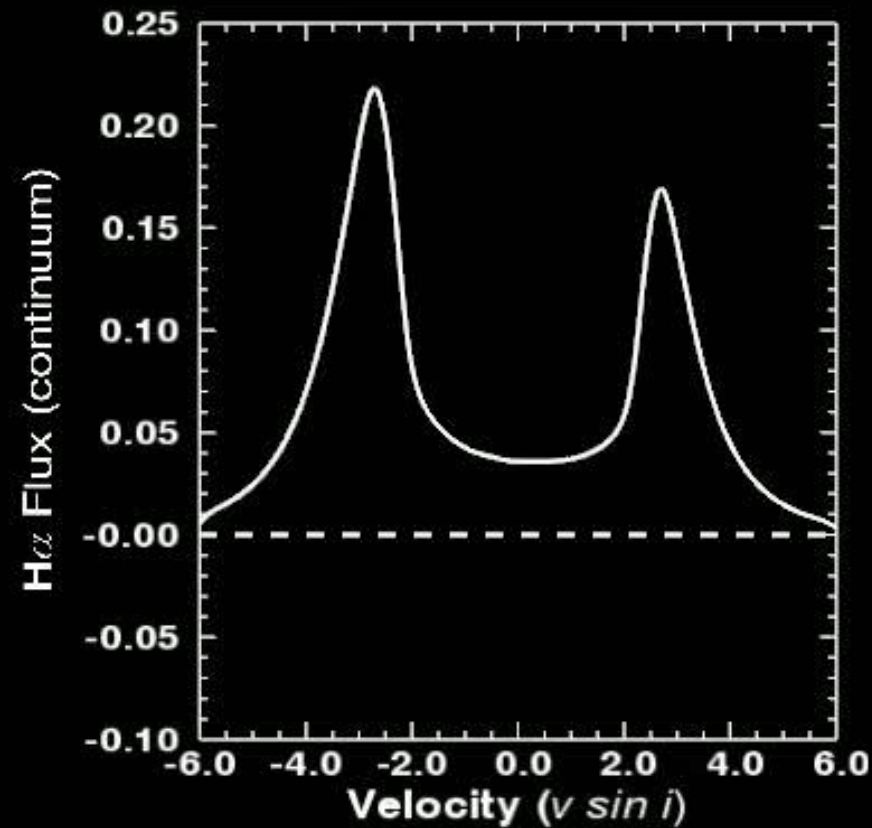
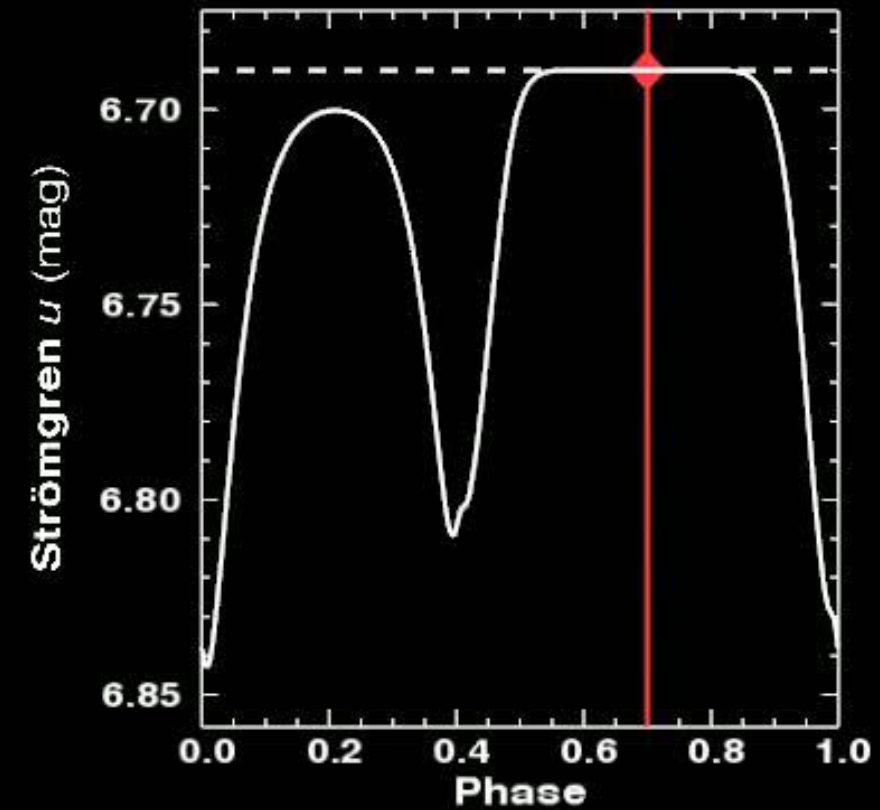
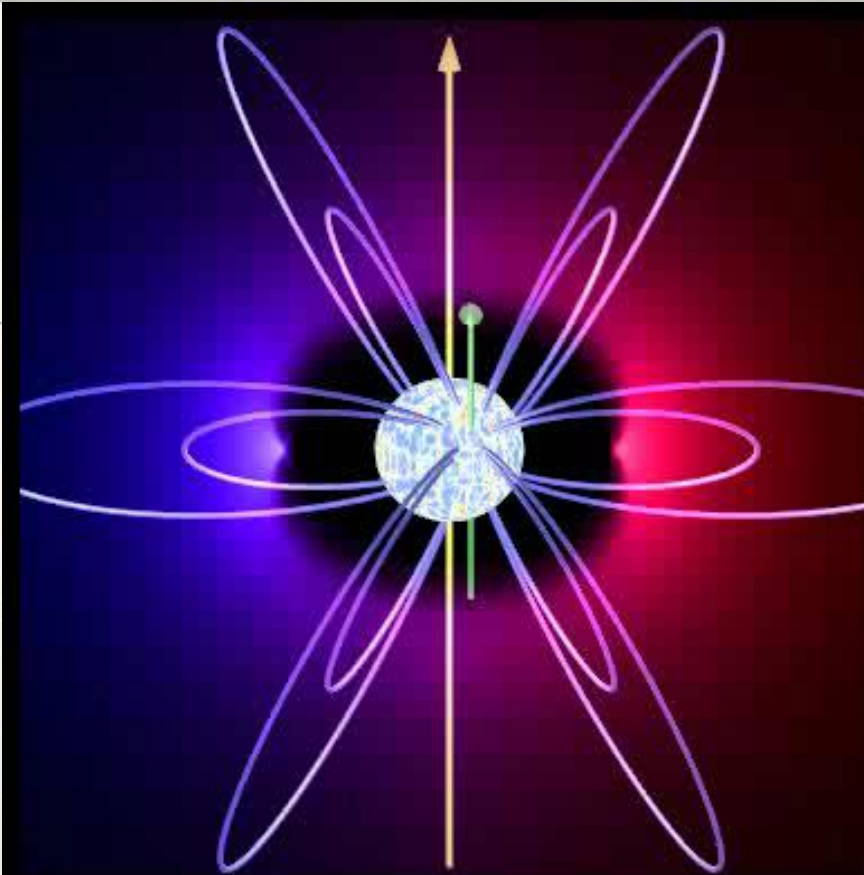
photometry

RRM model for σ Ori E

$$B^* \sim 10^4 \text{ G}$$

$$\eta^* \sim 10^6 !$$

tilt $\sim 55^\circ$



$H\alpha$

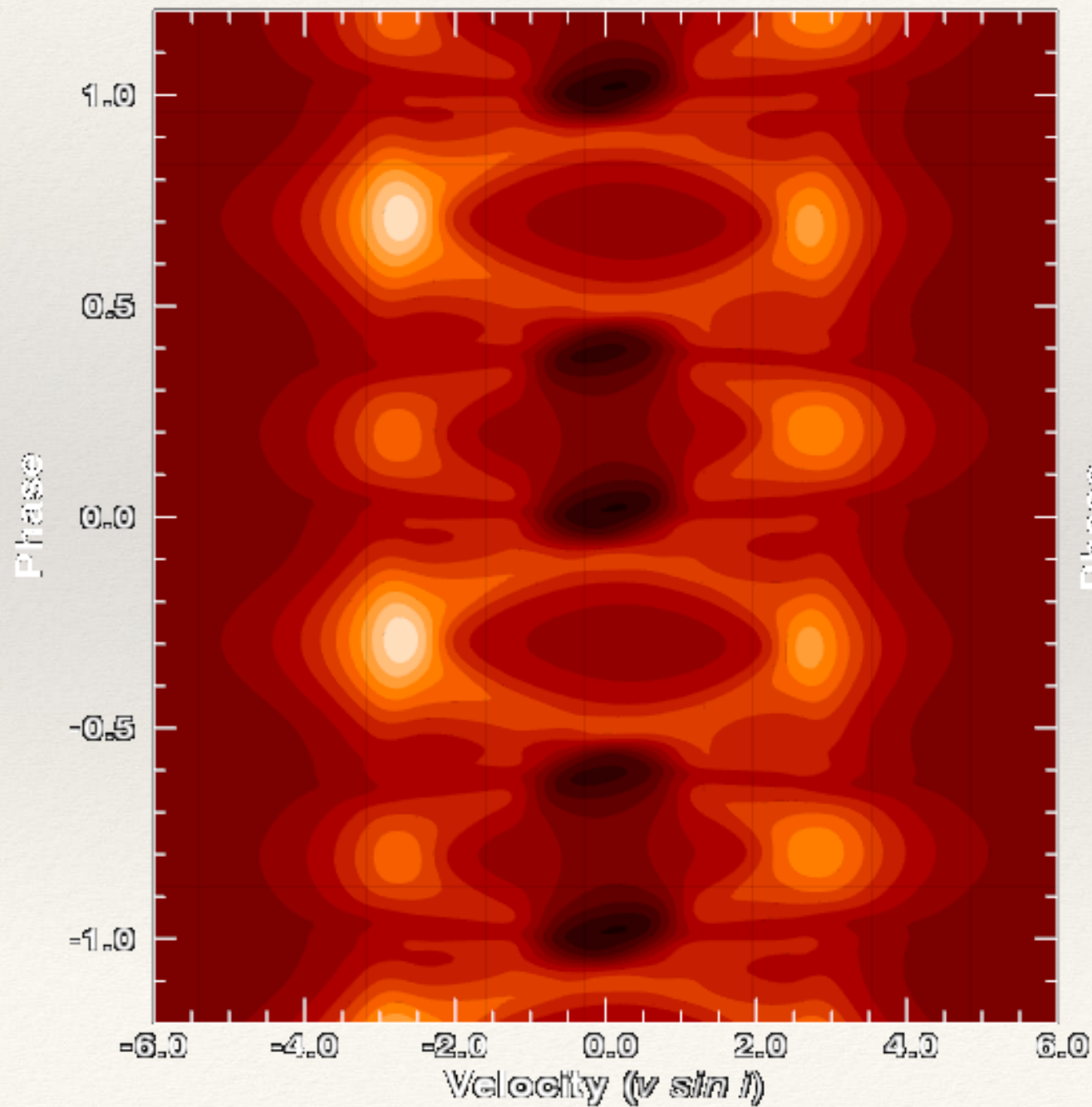
polarimetry

σ Ori E

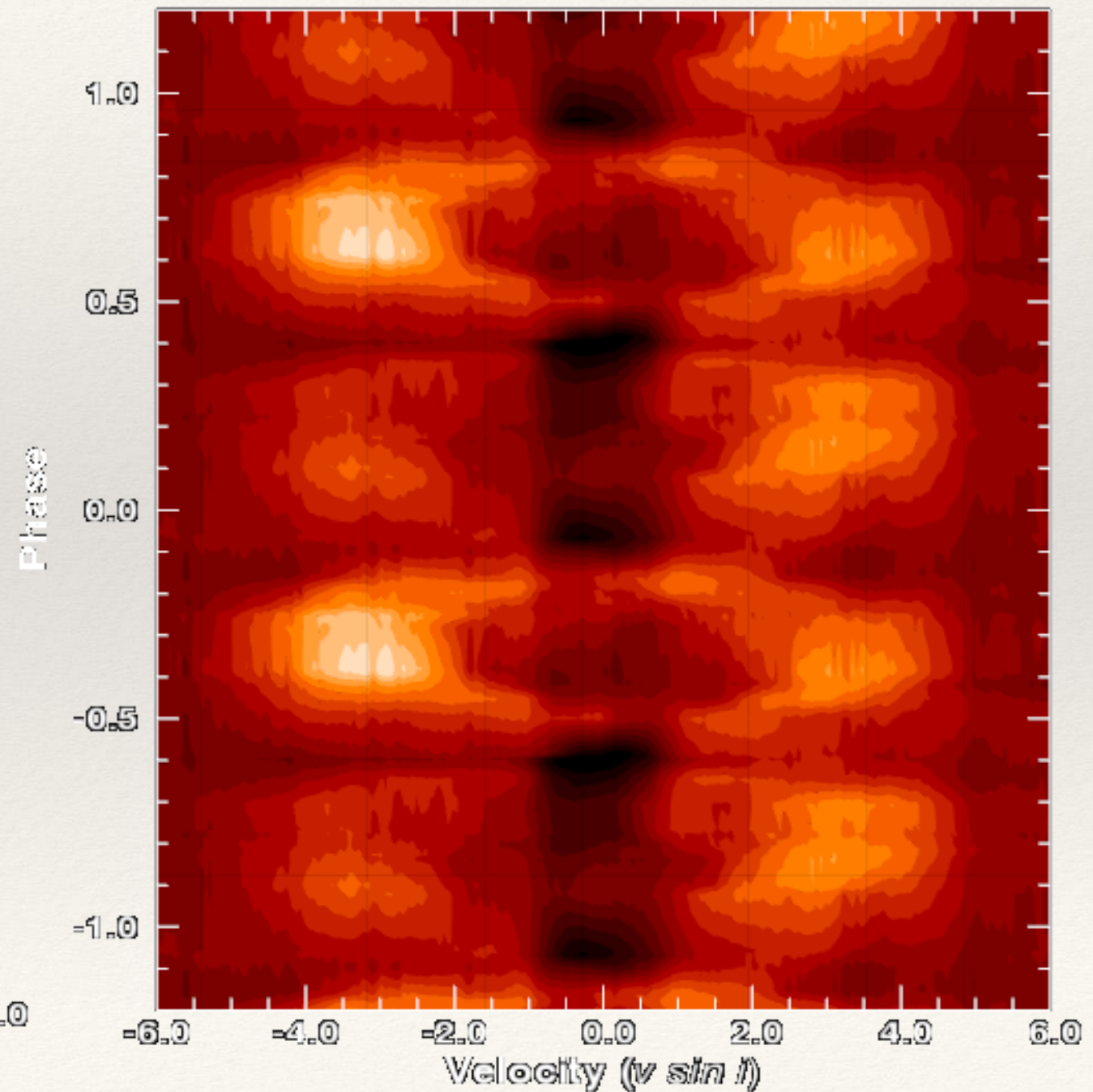
RRM Model

H α Observations

H α Emission



H α Emission



ARBITRARY-FIELD RRM (ARRM)

Oksala et al. 2016

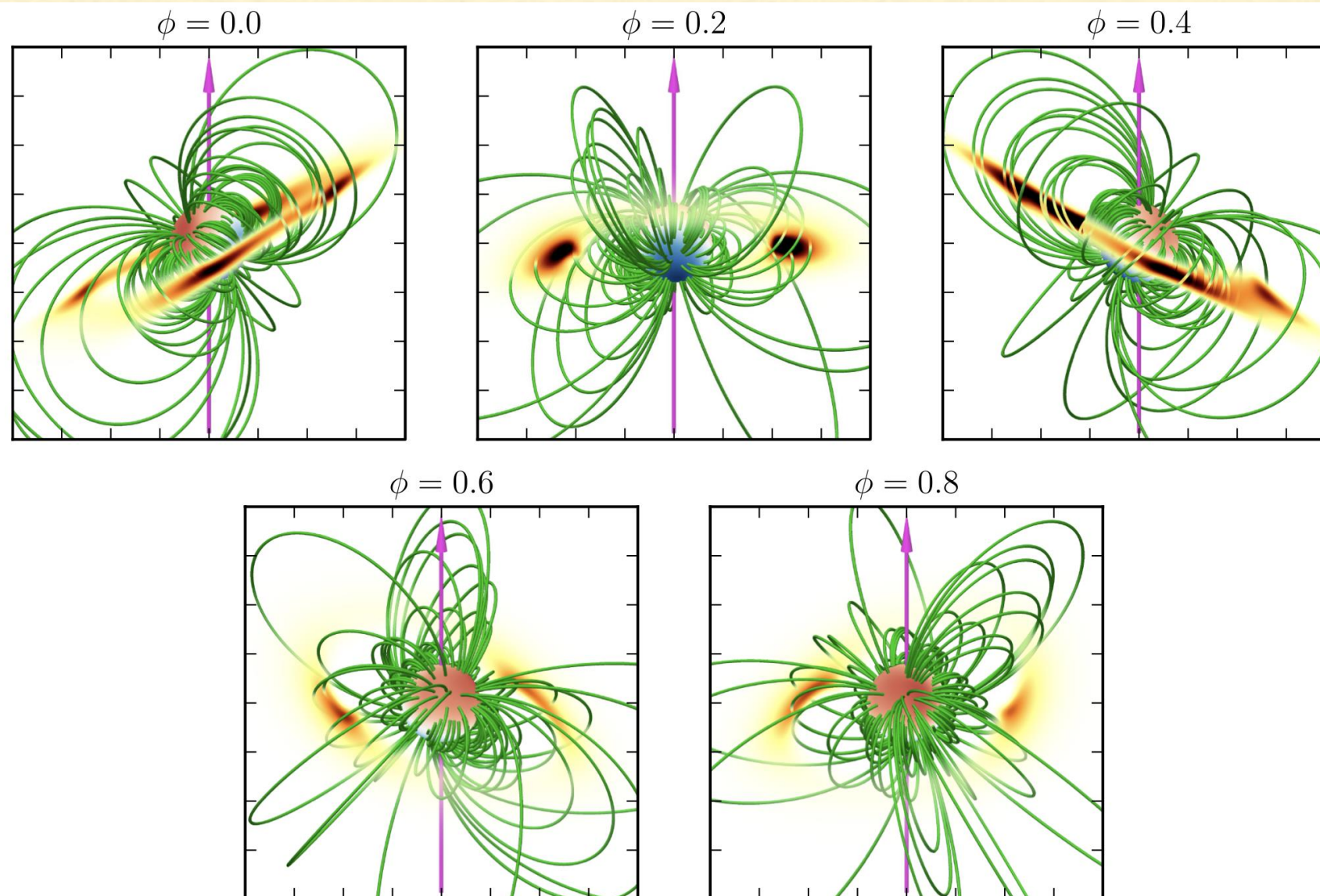


Figure 7. Visualizations of the plasma distribution predicted by the ARRM model, at the same five rotational phases adopted in previous figures. The star is coloured according to the radial magnetic field strength, as in the middle panels of Fig. 2; selected field lines are plotted in green, and the magenta arrow shows the star's rotation axis. The surrounding distribution of magnetospheric material is shown via an orange-coloured volume rendering, with the more opaque parts corresponding to higher column densities and vice versa. The tick marks on the surrounding boxes are spaced by $1R_*$.

IMPROVED RRM (ARRM)

Oksala et al. 2016

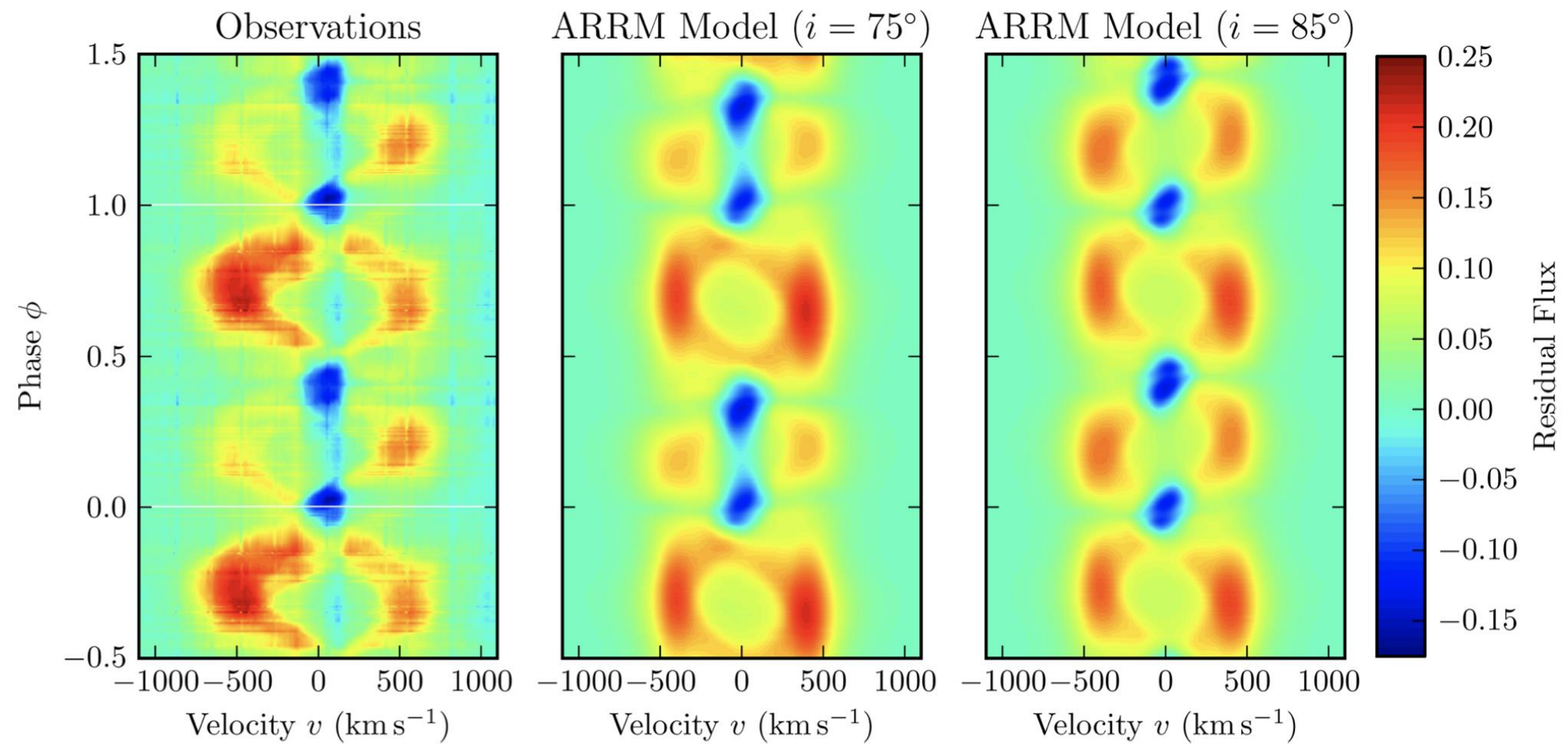
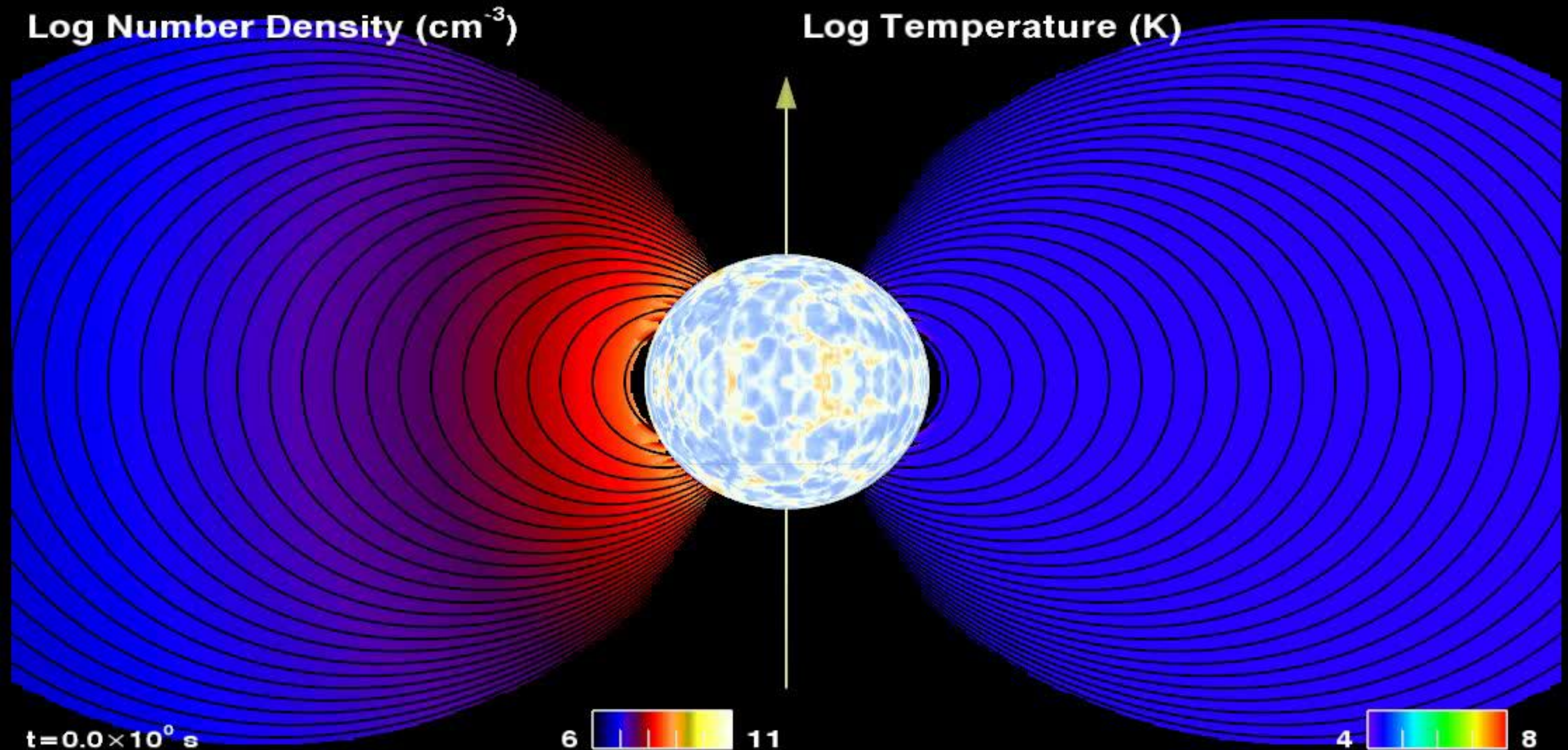
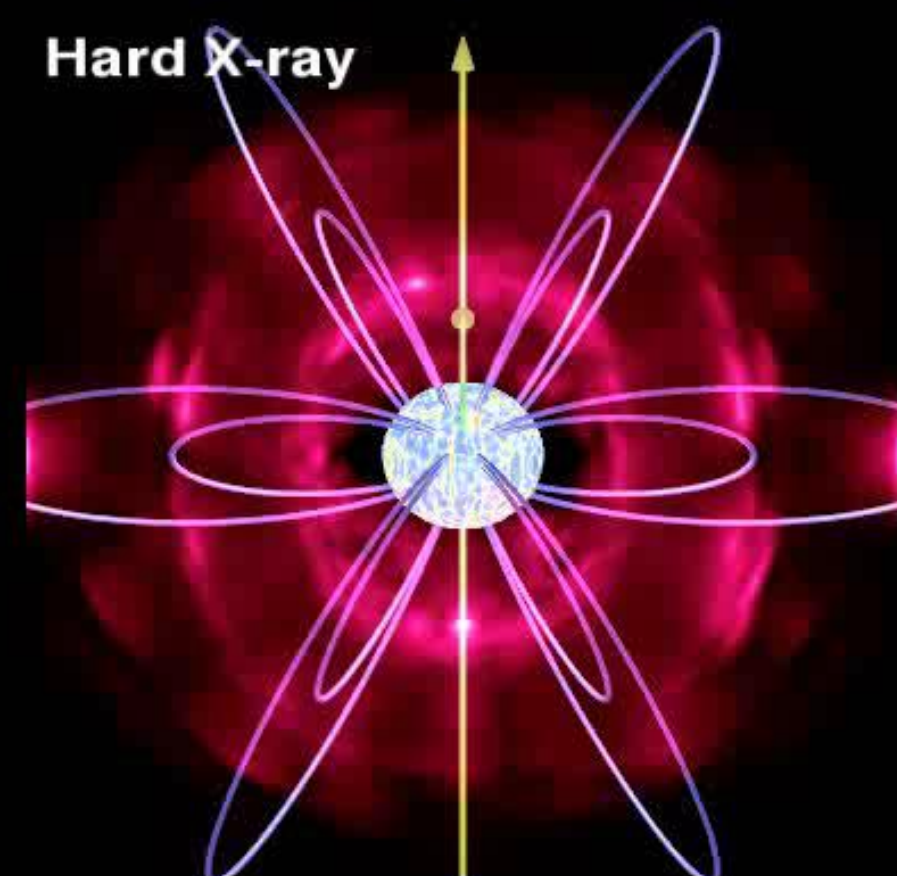
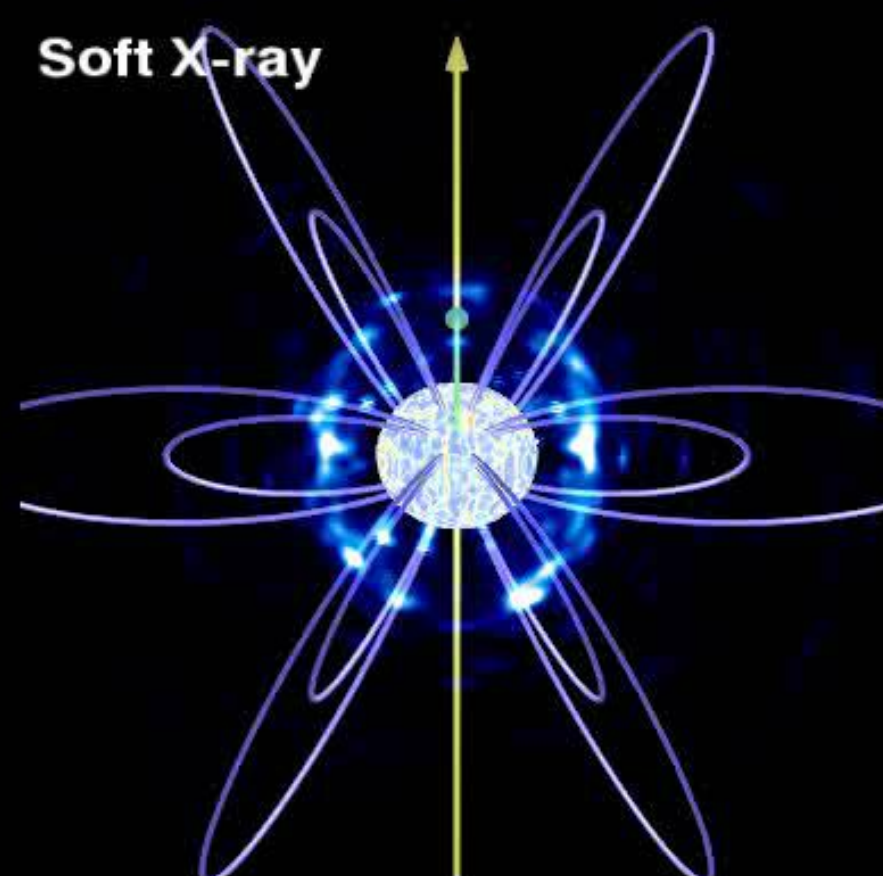
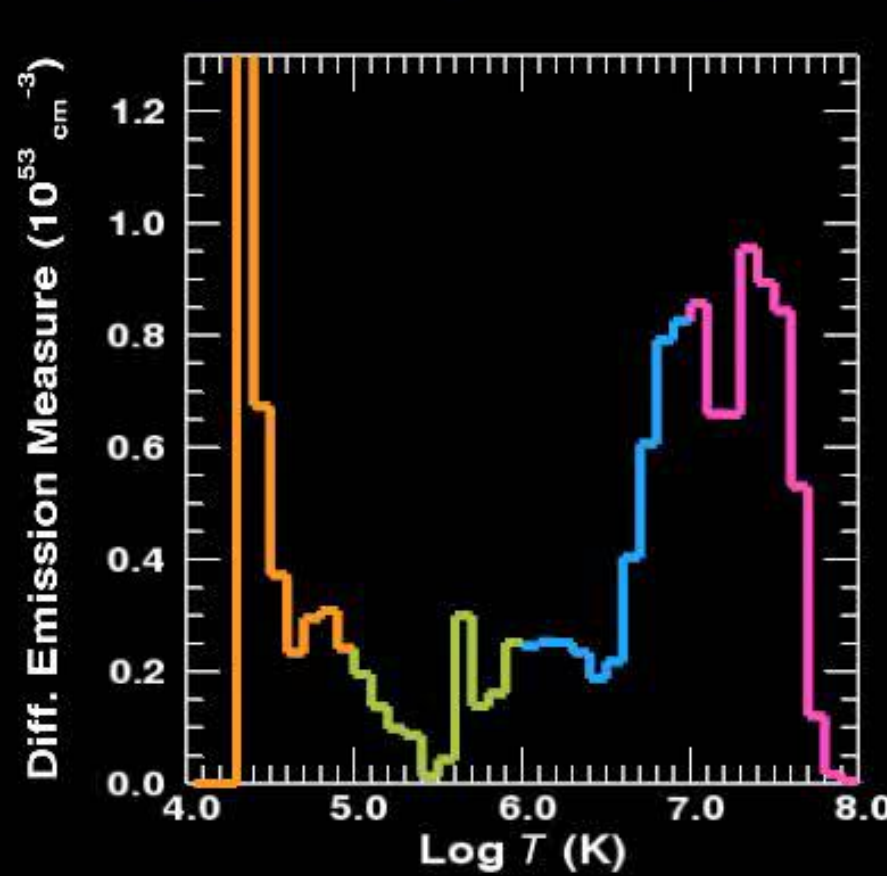
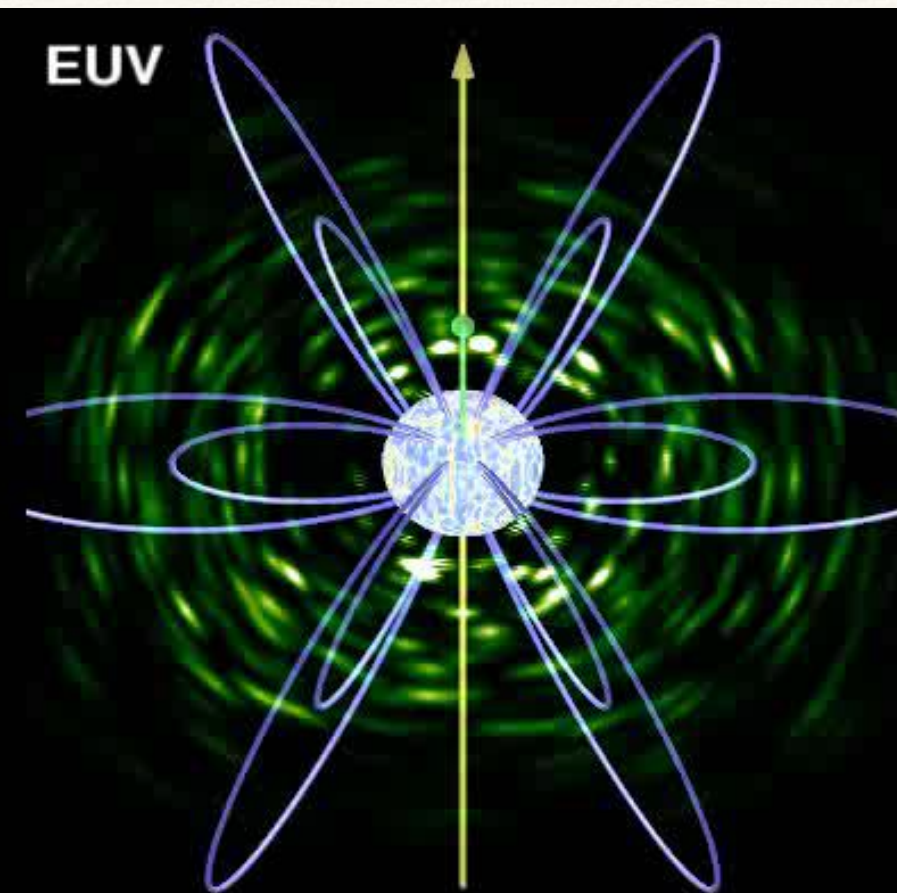
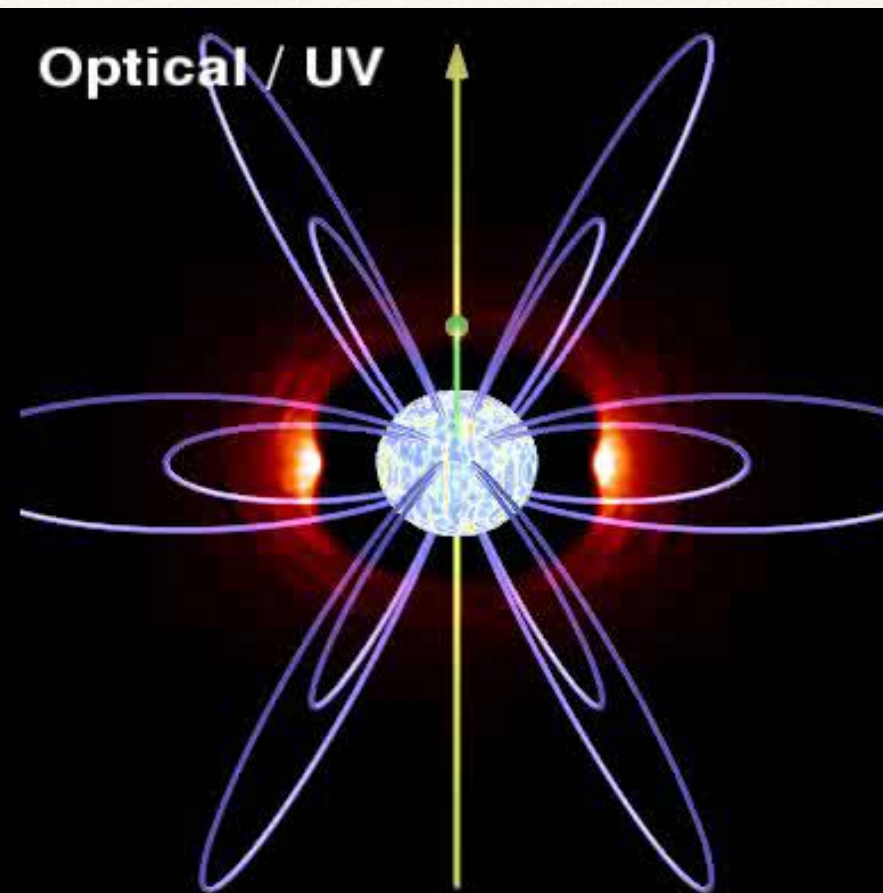
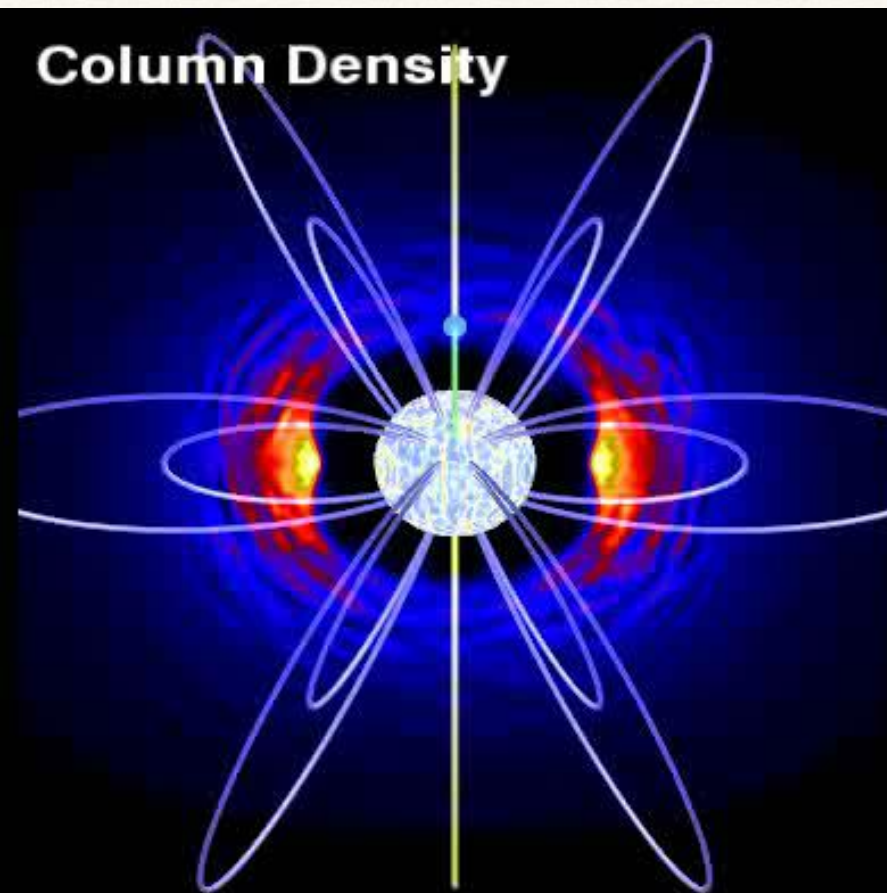


Figure 9. Comparison between observed (left) and modelled (middle and right) H α dynamic spectra of σ Ori E, in each case plotting the residual flux as a function of velocity and rotation phase. The middle plot is determined for an inclination angle, $i = 75^\circ$, while the right-hand plot is the same, but for $i = 85^\circ$. The observational data and the synthetic reference spectrum used to calculate the residuals are described in section 4 of [Paper I](#).

Rigid Field - Hydro Model

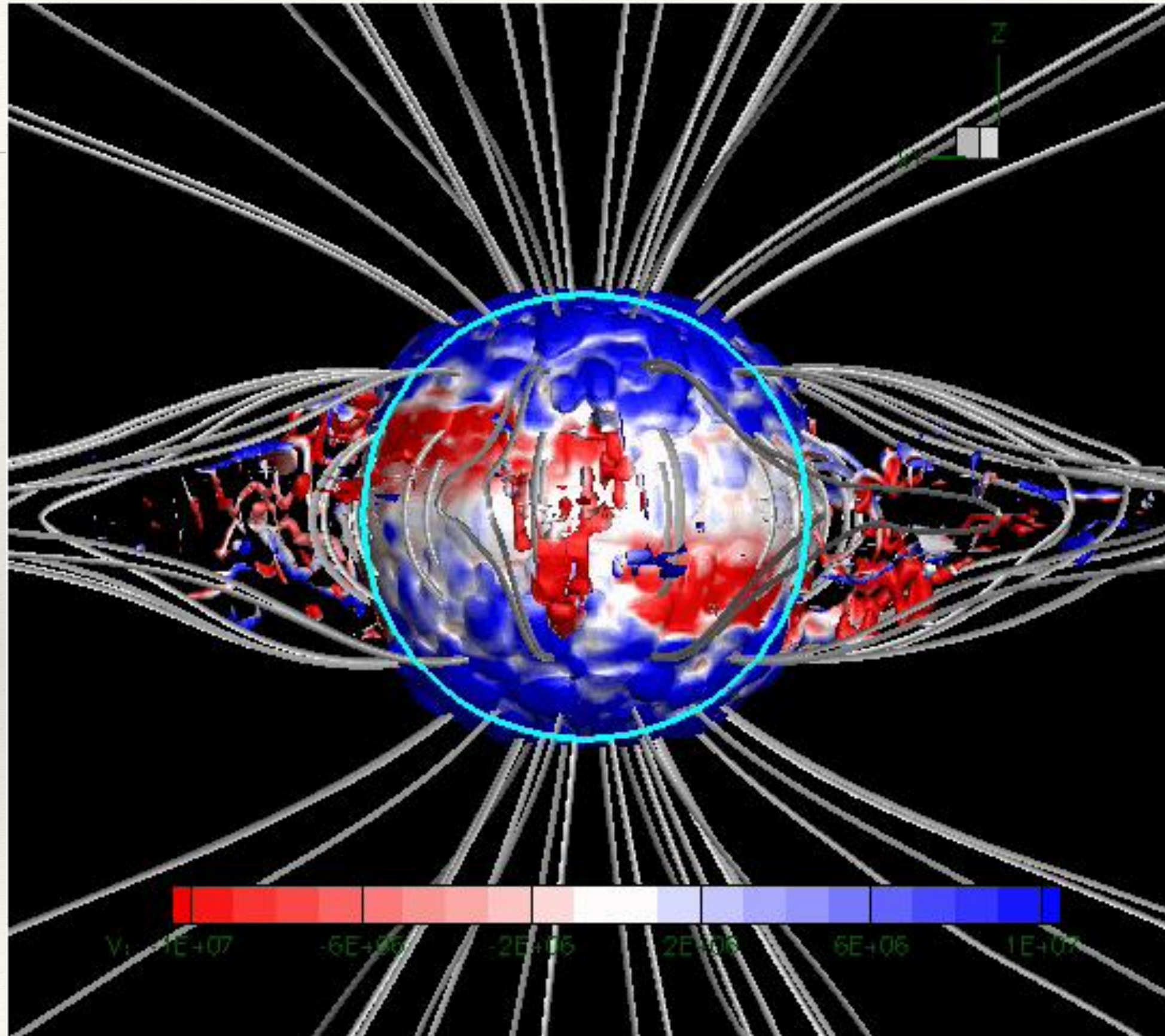
Townsend, Owocki and ud-Doula (2007)





Ultimately need 3D MHD

Iso-contour colored with radial V



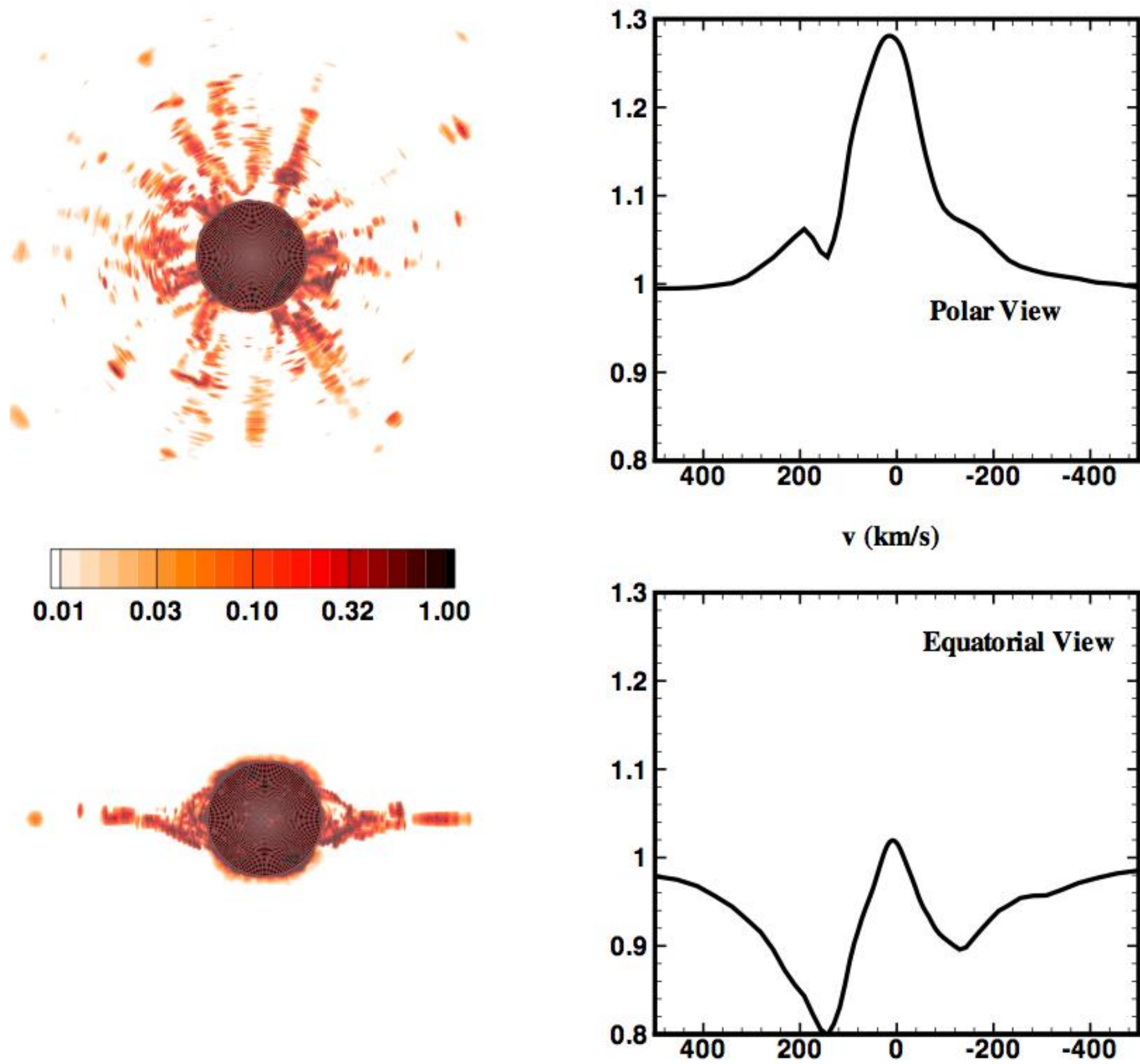


Figure 5. Synthetic H α surface brightness maps (left panels) and flux profiles (right panels) for observer viewing angles above the equator (upper panels) and magnetic pole (lower panels), as calculated from a snapshot of the 3D MHD wind simulation taken at 1000 ksec after initialization.

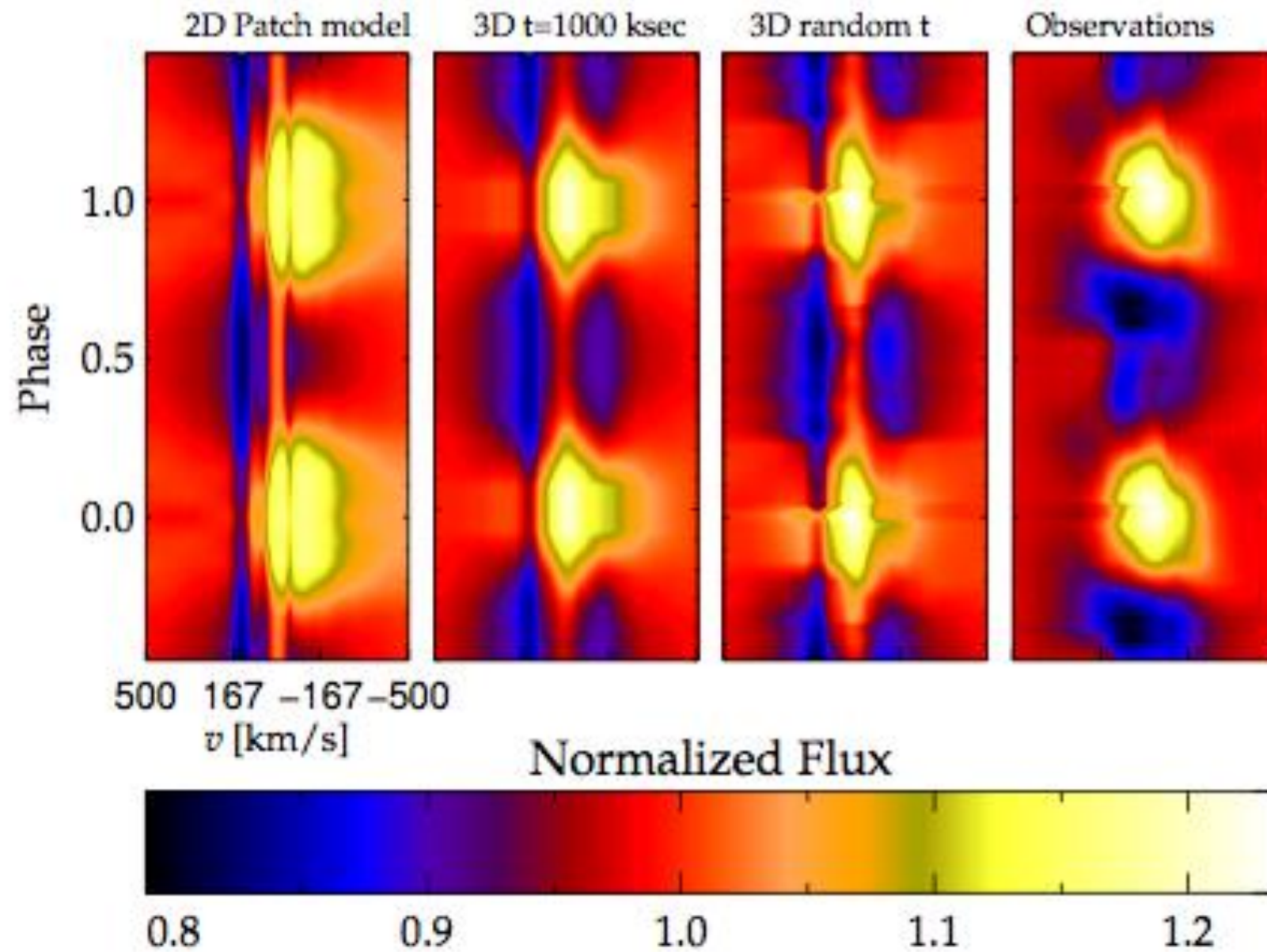
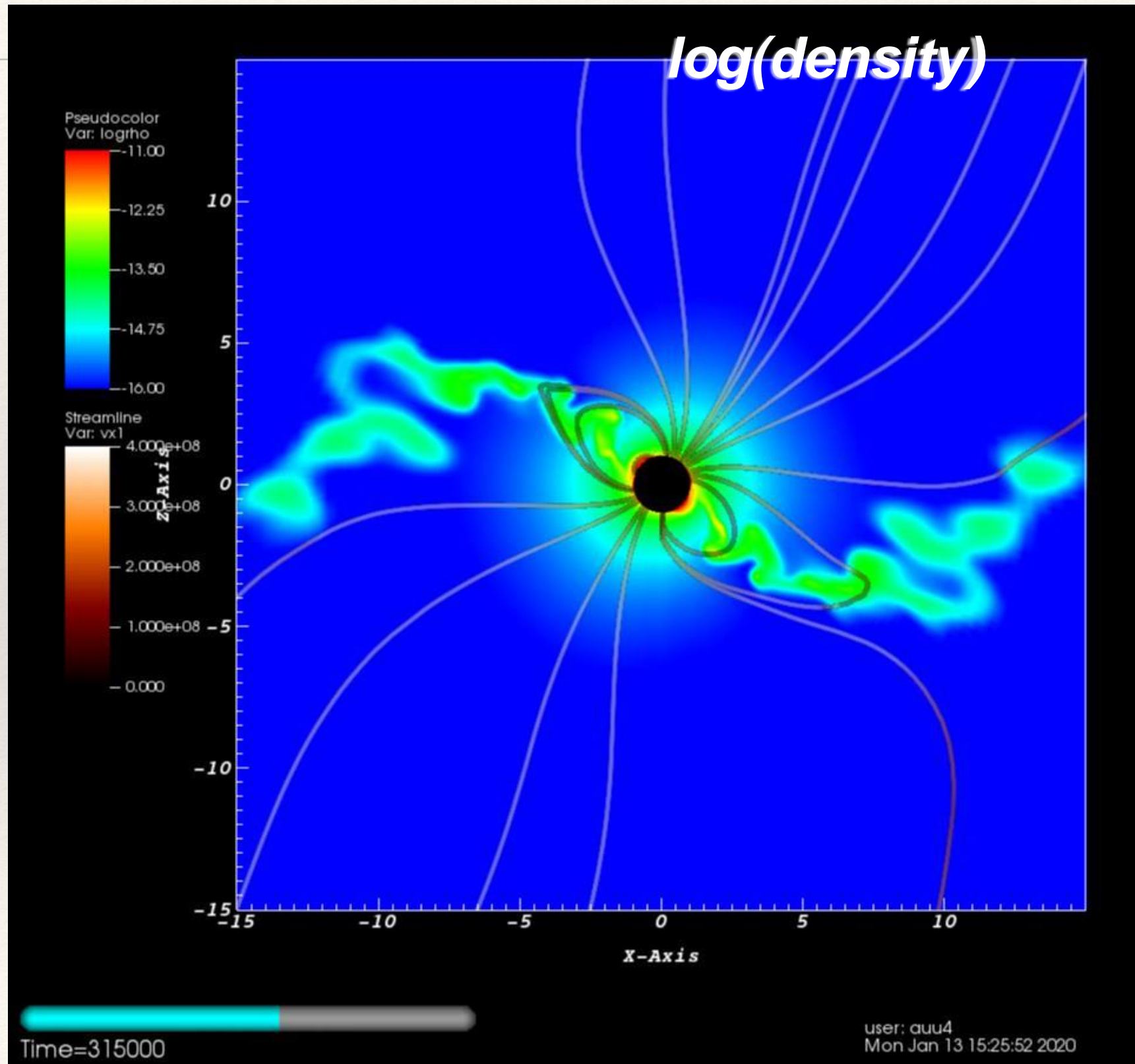


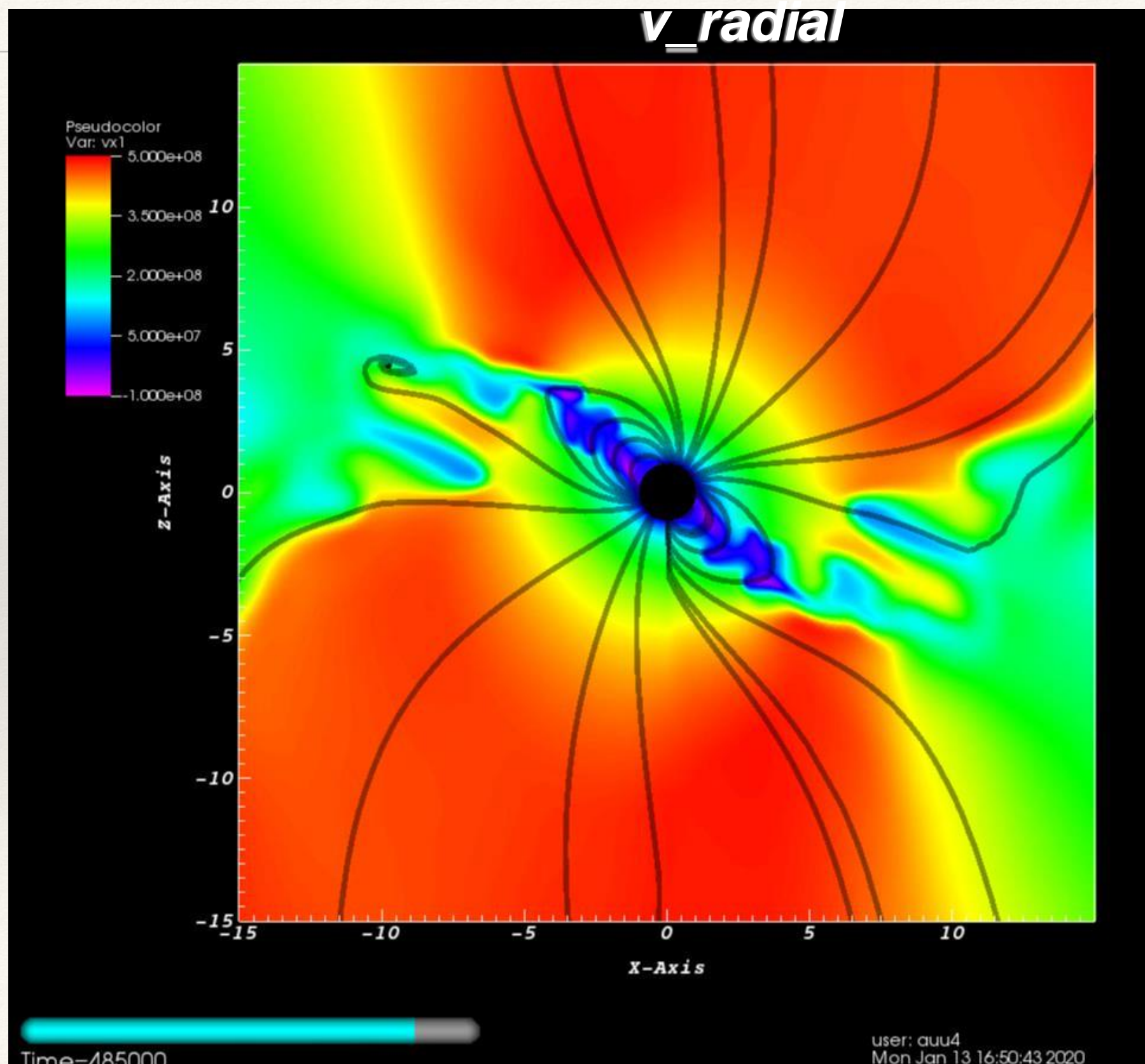
Figure 6. Observed and synthetic H α dynamic spectra of θ^1 Ori C. Synthetic spectra calculated from patching together 2D model snapshots (panel 1), a single 3D model snapshot (panel 2), and from a random selection of 3D snapshots (panel 3). For consistency, 3D snapshots having random phases that coincide with the observations have been selected in the third panel.

Oblique Dipole Challenging

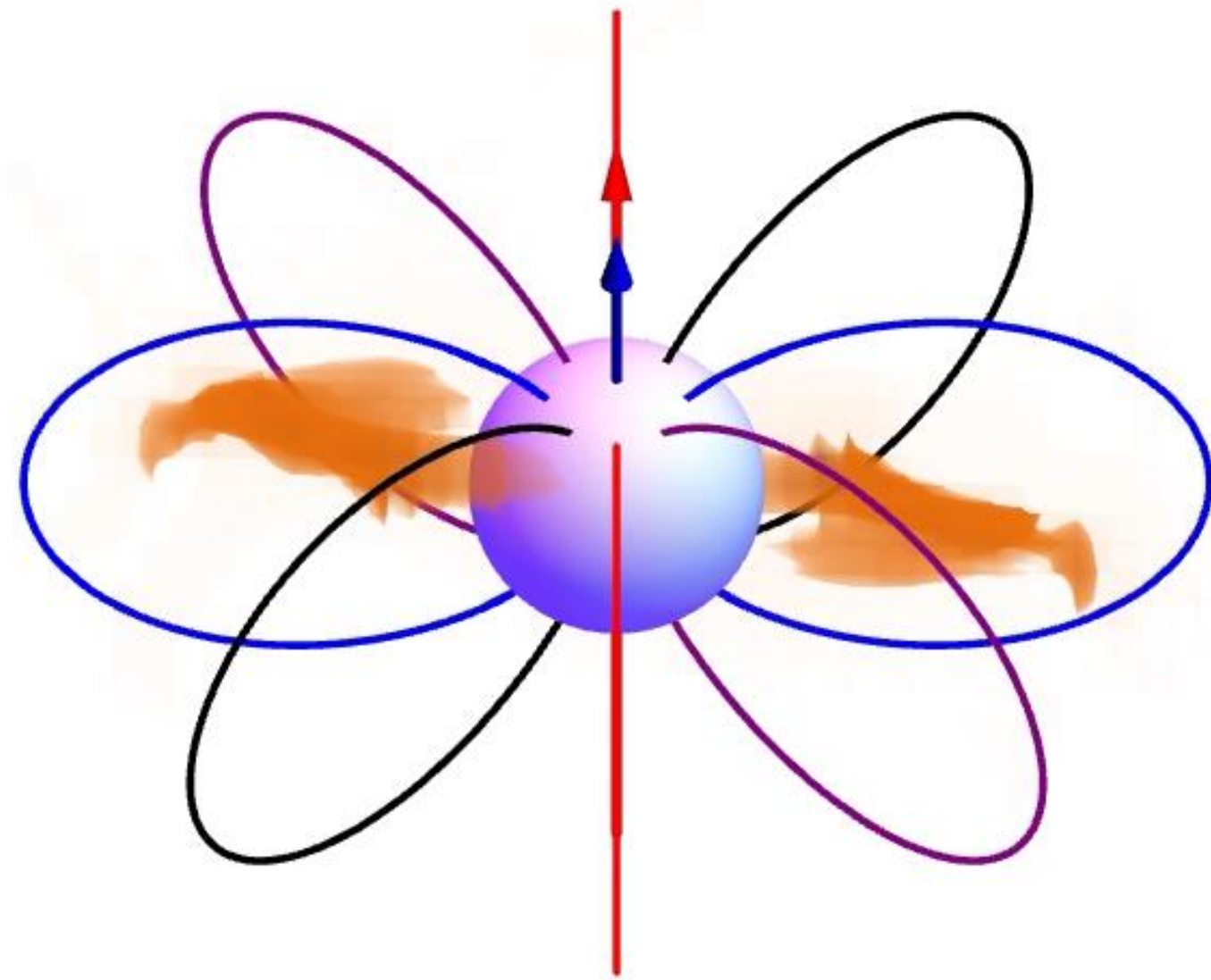
$$\beta = 45^\circ, \log(\eta_*) = 3.0, W=0.7$$



$$\beta = 45^\circ, \log(\eta_*) = 3.0, W=0.7$$



$$\beta = 45^\circ, \text{LOG}(\eta_*) = 3.0, W=0.5$$



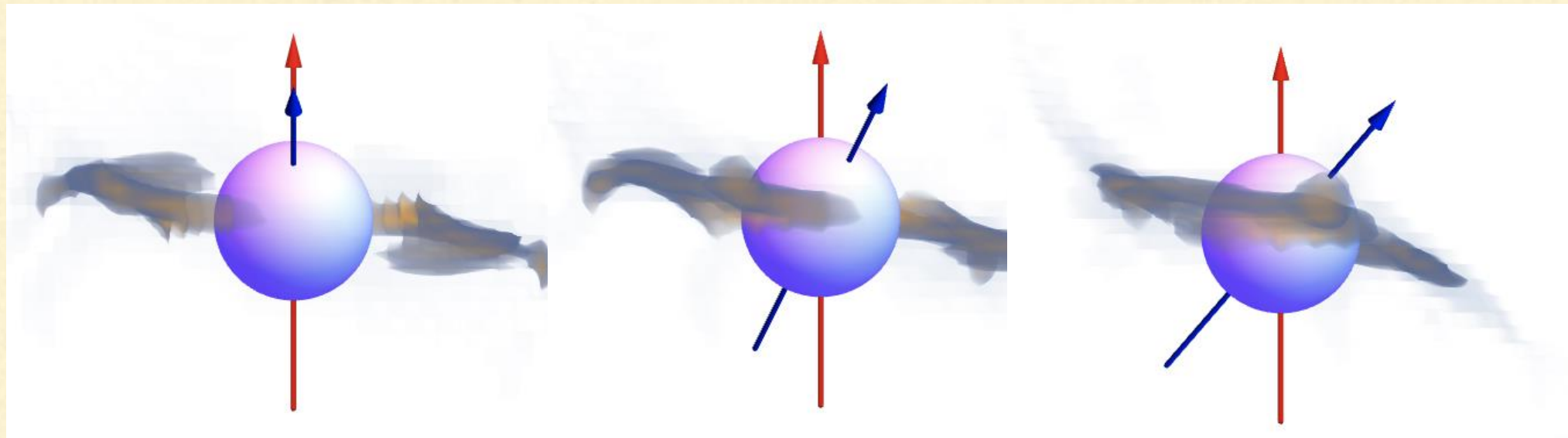
DENSITY DISTRIBUTION

phase=0

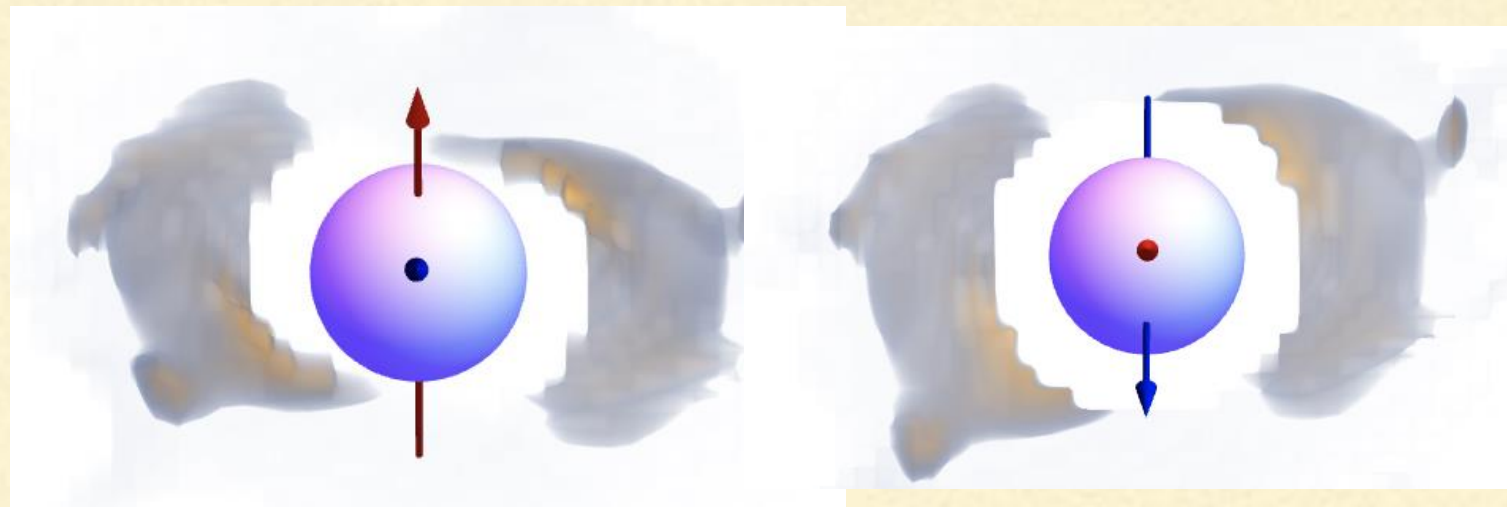
phase=0.125

phase=0.25

i=90



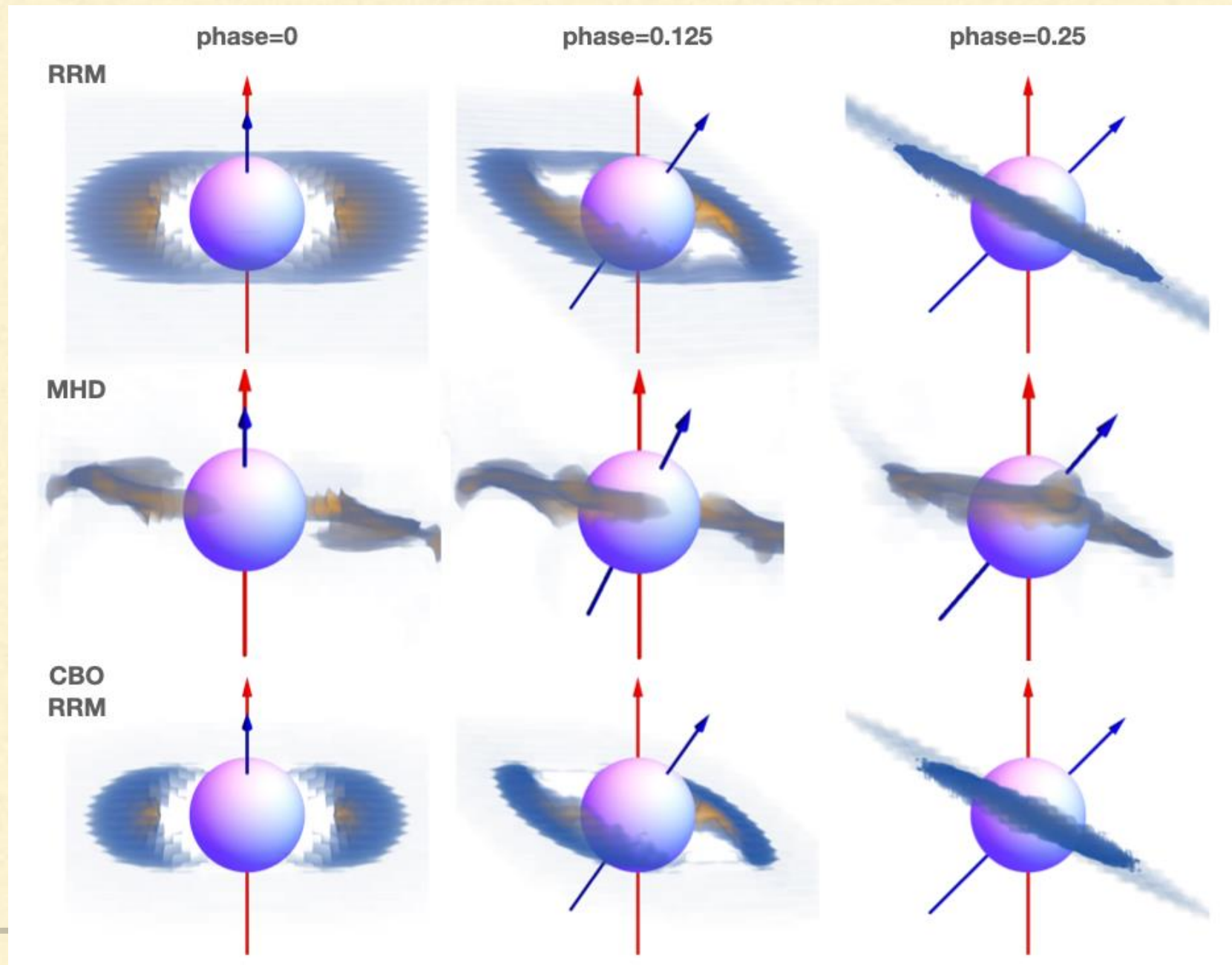
phase=0



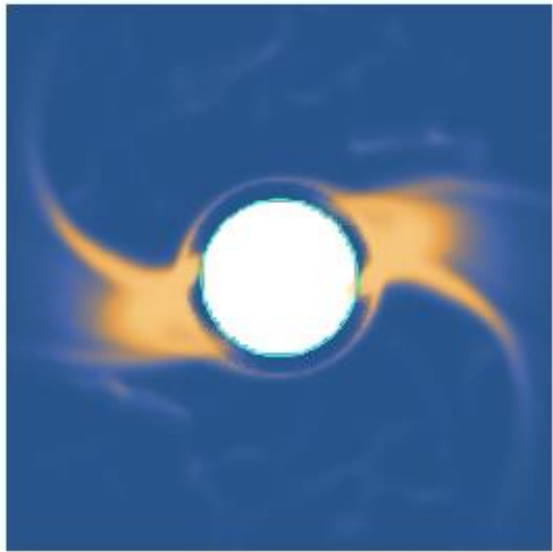
i=45

i=0

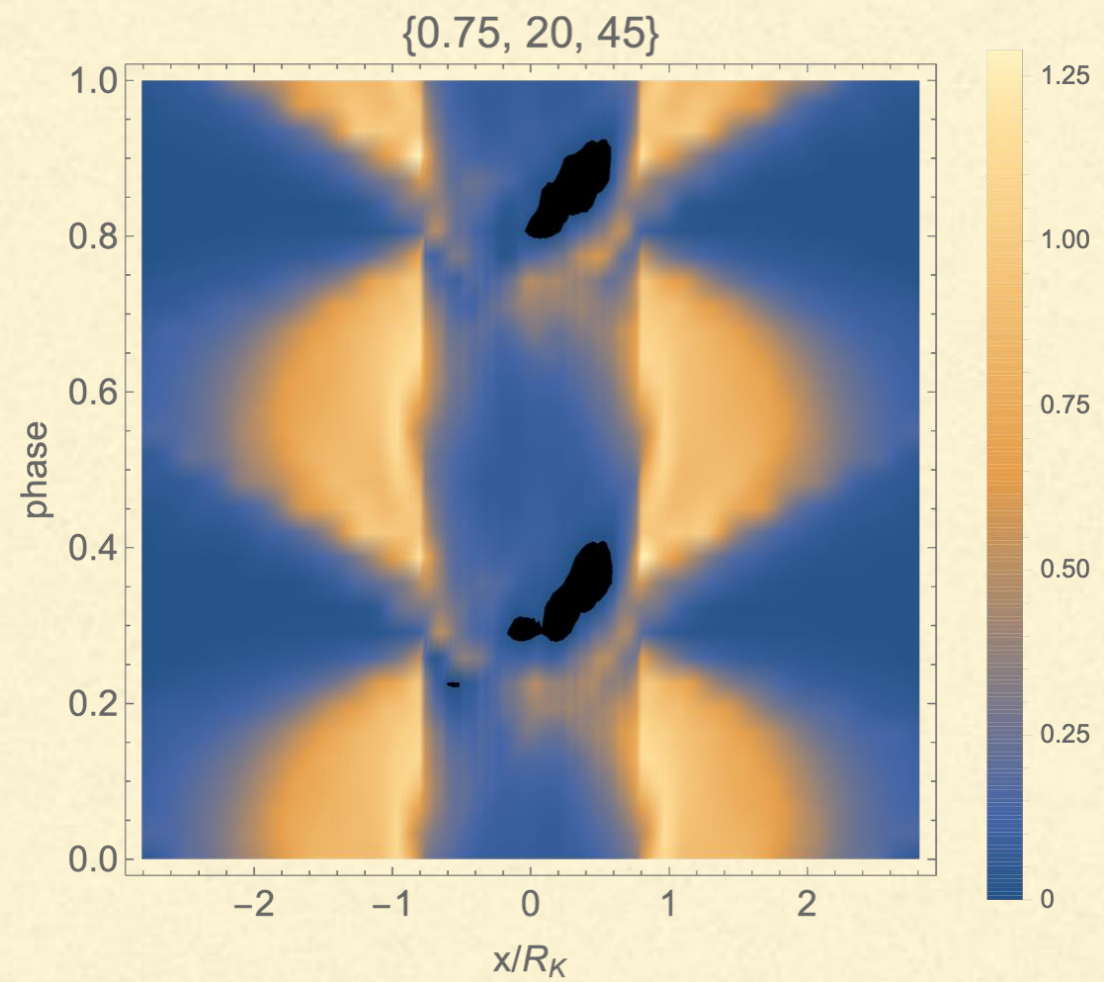
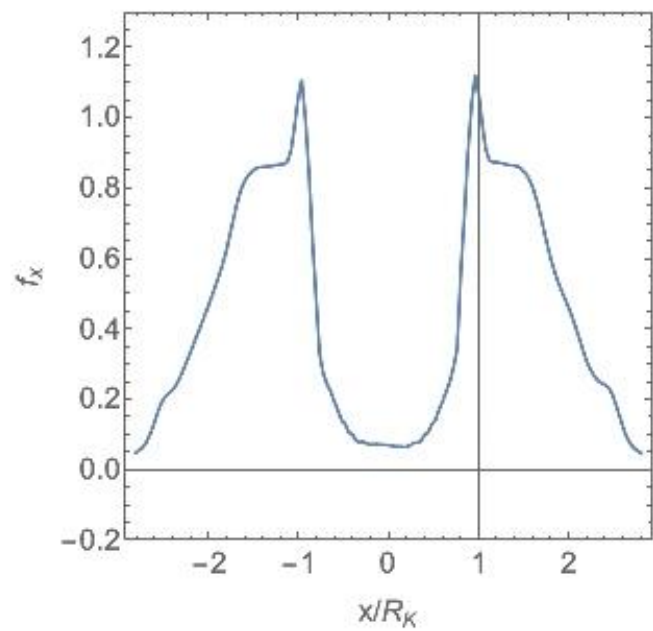
COMPARISON WITH RRM



SYNTHESIZING HALPHA



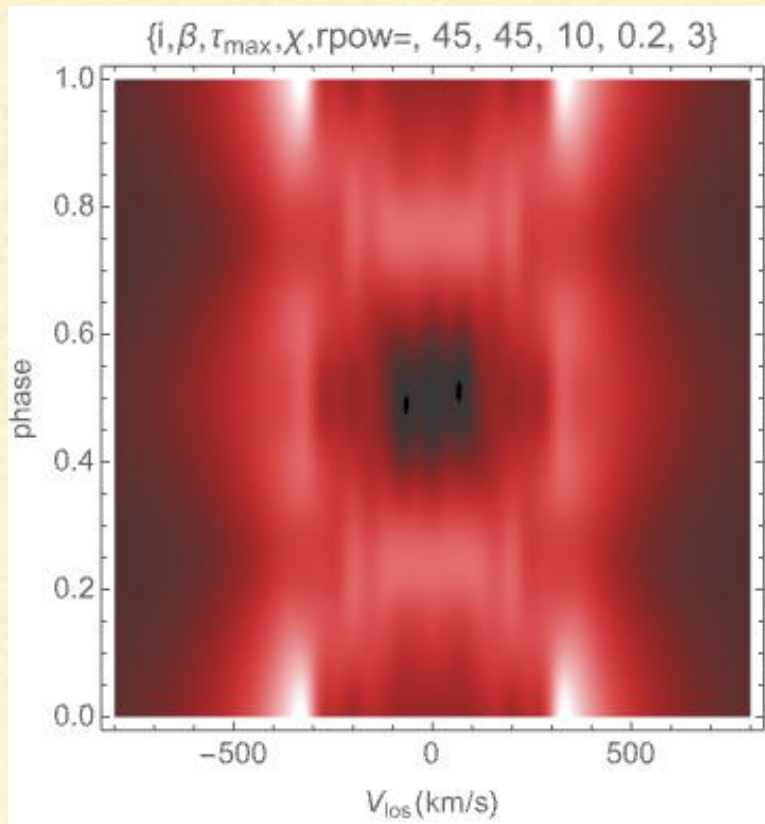
Halpa Line Profile
{0.75, 20, 45, 0.}



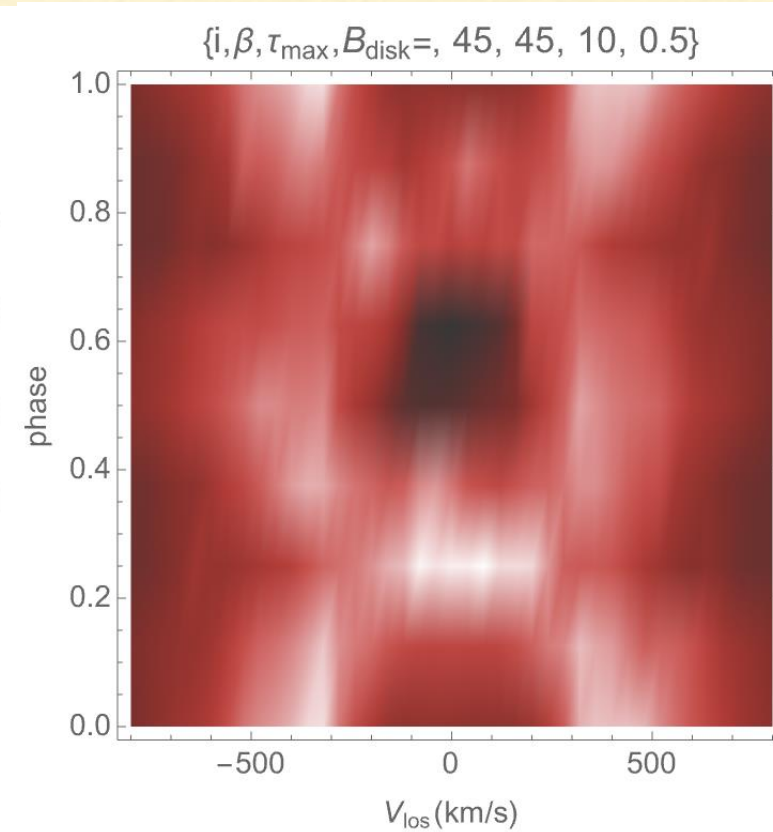
Dynamical Spectrum

H α PIH A

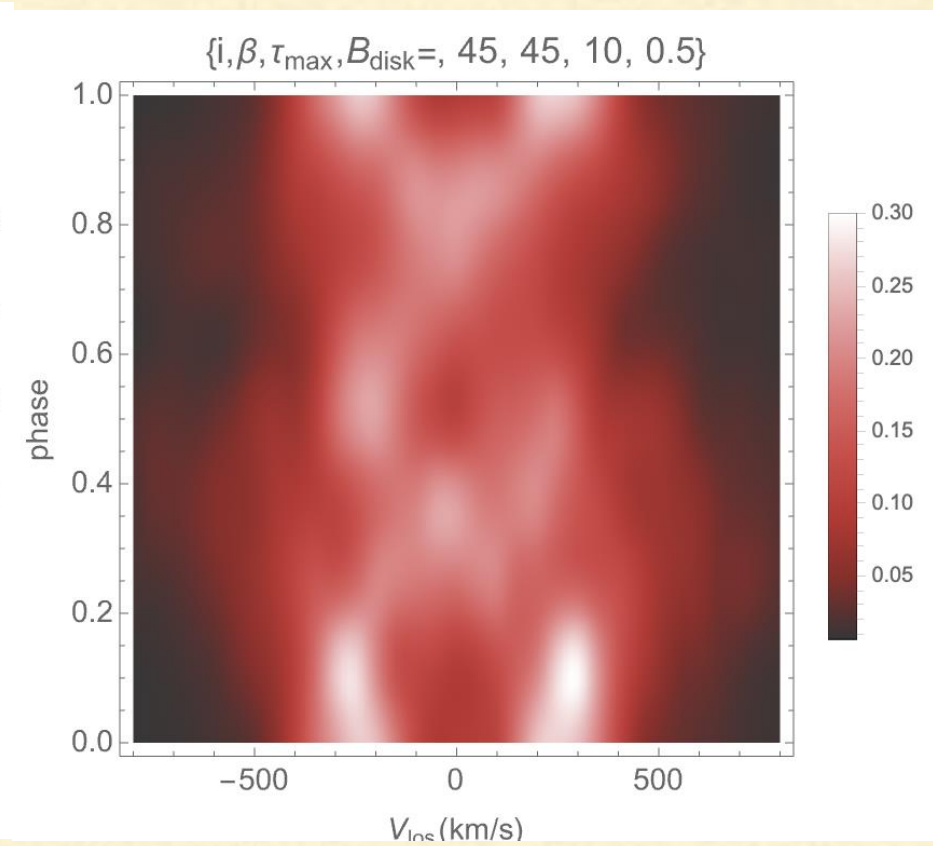
RRM



Rigid MHD

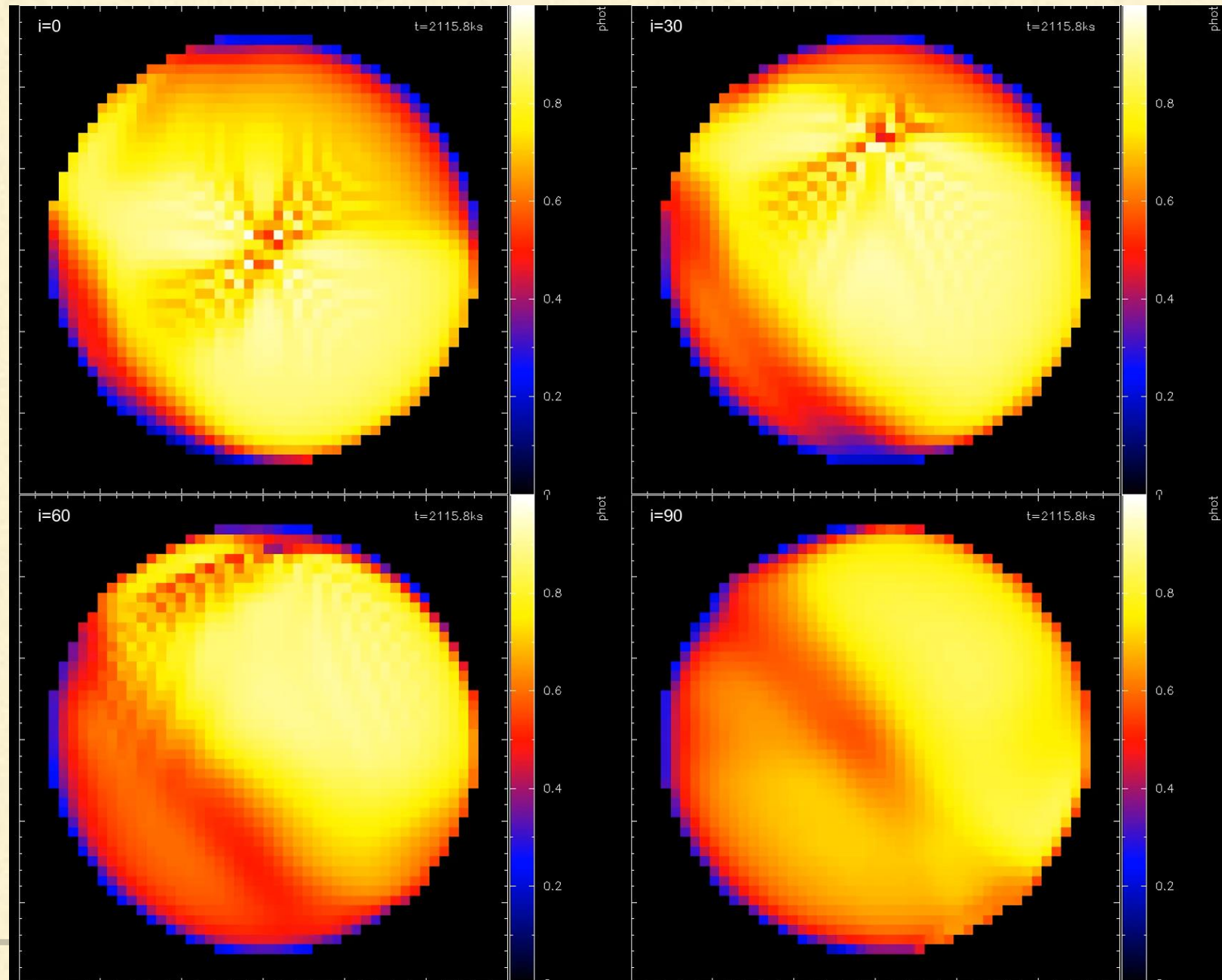


Full MHD



inclination 45deg

PHOTOMETRIC VARIATION



Conclusion

- ❖ 2D MHD of MCWS
 - ❖ slow rotating magnetic stars
 - ❖ can predict X-rays from magnetic stars
- ❖ Comparison with observations
 - ❖ Chandra & XMM
 - ❖ Optical photometry, spectroscopy, polarimetry
- ❖ 3D MHD of MCWS
 - ❖ 3D MHD for single stars can be done even for tilted dipole.
 - ❖ Basic disk topology is different from the one predicted by RRM model. In addition, there is significantly more variability in MHD models.
 - ❖ RRM assumes full rigid rotation; MHD suggests moderate breakdown due to rotational effects