

Stellar winds from B supergiant stars: Exploring the δ -slow hydrodynamic solution





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Stellar winds from B supergiant stars: Exploring the δ -slow hydrodynamic solution



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The wind of rotating B supergiants – II. The δ -slow hydrodynamic regime

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ABSTRACT

The theory of line-driven winds can explain many observed spectral features in early-type stars, though our understanding the winds of B supergiants remains incomplete. The hydrodynamic equations for slowly rotating stellar winds predict two regimes

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Stellar winds

Flows of gas ejected from the surface of the star It is a prominent phenomenon in OBA-type stars



Rigel (B8 Ia) and the Witch Head nebulae (Star Shadows Remote Observatory)



Stellar Winds: Why are they important?



Relevance of stellar winds

- Mass loss modifies the stellar evolution.
- Loss of angular momentum of stars.
- Estimation of distances and other relevant parameters.
- Interaction with the interstellar medium.
- Chemical evolution of galaxies.
- First generations of stars.
- Much more...
- However, the stellar wind is intriguing in its own right.



B-type supergiant stars

Main properties

- Heterogeneous group of stars.
- Diversity of evolutionary phases (blue region⇔red region of HR diagram).
- Photometric and spectroscopic variability.

Fundamental parameters

- 8 M $_{\odot} \lesssim$ Mass \lesssim 50 M $_{\odot}$
- $10^{4,7}~L_{\odot}$ \lesssim Luminosity $\lesssim 10^{5,6}~L_{\odot}$
- 12000 K $\lesssim T_{\rm eff} \lesssim 25\,000$ K
- $1.7 \lesssim \log g \lesssim 3$
- 20 R $_{\odot} \lesssim$ Radius \lesssim 70 R $_{\odot}$
- v sin i \lesssim 100 km s $^{-1}$

Region of the HR diagram occupied by B-type supergiant stars



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B-type supergiant stars

Wind Parameters

- Mass-loss rates: $\dot{M} \sim 10^{-7} \text{ a } 5 \times 10^{-6} \text{ M}_{\odot} \text{ yr}^{-1}$
- Terminal velocities: $v_{\infty}\sim 200~{\rm km~s^{-1}}({\rm late})~{\rm to}~1500~{\rm km~s^{-1}}$ (early)

$$\begin{cases} Q_{res} = \frac{\dot{M}}{R_* v_{\infty}^2} & \text{Resonance} \\ \\ Q = \frac{\dot{M}}{(R_* v_{\infty})^{1.5}} & \text{Recombination} \\ \\ (H\alpha) \end{cases}$$

Optical depth invariant

Spectral variability



 ${\rm H}\alpha$ line profiles of 55 Cygni (B3 la) from July to August 2013 (Haucke+,2016).



Radiation-driven wind theory

Brief historical overview

Milne (1924): Radiation force drives the ions, favored by the Doppler effect.

Lucy & Solomon (1970): Momentum transfer of the radiation field in resonance lines.

Castor, Abbott, & Klein (1975): CAK theory - The first analytical solution of radiation-driven winds (including weak line acceleration).

Abbott (1982): Line-force parameterization.

Basic hypotheses

- Stationary state.
- Homogeneous wind.
- Spherical symmetry.
- Point source (photons with radial direction).
- No rotation, magnetic fields, etc.

Hydrodynamic equations for the wind

Continuity equation

$$\dot{M} = -rac{dM_*}{dt} = 4\pi r^2
ho v = constant$$

Momentum equation

$$v \frac{\partial v}{\partial r} = -\frac{1}{\rho} \frac{\partial P}{\partial r} + gr$$

$$g_r = -\frac{GM_*}{r^2} + g_{rad}^C + g_{rad}^L$$

Energy equation \rightarrow Isothermal wind.

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Radiative acceleration

Continuum acceleration

$$\begin{aligned} \mathbf{g}_{rad}^{\mathsf{C}}(\mathbf{r}) &= \frac{1}{c} \oint \int_{\nu=0}^{\infty} \kappa_{\mathsf{C}} \, I_{\nu}(\mathbf{r}, \tilde{\mathbf{n}}) \, \tilde{\mathbf{n}} \, d\omega \, d\nu \\ \text{can be expressed as: } g_{rad}^{\mathsf{C}} &= \frac{\sigma_{e} L_{*}}{4\pi r^{2} c} \\ g + g_{rad}^{\mathsf{C}} &= -\frac{GM_{*}(1-\Gamma)}{r^{2}} \, \text{con } \Gamma = \frac{\sigma_{e} L_{*}}{4\pi c GM_{*}} \end{aligned}$$

Acceleration due to momentum transfer in spectral lines

$$\mathbf{g}_{rad}^{L}(\mathbf{r}) = \sum_{lineas} \frac{\kappa_{L} \Delta \nu_{D}}{c} \oint \int_{x=-\infty}^{\infty} \phi\left(x - \frac{\mathbf{\tilde{n}} \cdot \mathbf{v}(\mathbf{r})}{v_{th}}\right) I_{\nu}(\mathbf{r}, \mathbf{\tilde{n}}) \, \mathbf{\tilde{n}} \, d\omega \, dx$$

Sobolev approximation

For a small resonance region

$$\mathbf{g}_{rad}^{L} = \sum_{lineas} \frac{\kappa_{L} \nu_{0} v_{th}}{c^{2}} \oint I^{c}(\omega) \, \mathbf{\tilde{n}} \, d\omega \left[\frac{1 - e^{-\tau_{0}}}{\tau_{0}} \right]$$

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Sobolev optical depth

$$\tau_{sob} = \tau_0 \, \Phi = \kappa_L \, \rho \, \left(\frac{v_{th}}{\mu^2 \frac{\partial v}{\partial r} + (1 - \mu^2) \frac{v}{r}} \right) \, \Phi$$

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Parameterization of the radiation force due to the spectral lines

Castor, Abbott, & Klein (1975)

$$g_{rad}^{L} = \frac{\sigma_{e}F}{c}\mathcal{M}(t)$$

Force multiplier

$$\mathscr{M}(t) = \sum_{lines} \frac{\Delta \nu_D F_{\nu}}{F} \frac{1}{t} (1 - e^{-\eta t})$$

$$\eta = \frac{\pi e^2}{m_e c} g_u f_{ul} \frac{n_l / g_l - n_u / g_u}{\rho \sigma_e \Delta \nu_D}$$

Force multiplier (Abbott, 1982)

$$\mathscr{M}(t) = k t^{-\alpha} \left(\frac{n_e}{W(r)}\right)^{\delta}$$
with parameters $k \to \infty$ is

with parameters k , lpha y δ

Interpretation of parameters

- k → Effective number of contributing lines for momentum
- $\alpha \rightarrow \text{Slope of line intensity distribution}$ $dN(\nu, \kappa_L) = -N_0 f_{\nu}(\nu) \kappa_L^{\alpha-2} d\nu d\kappa_L$ that allows us to write: $\sum_{\text{lineas}} g_{rad}^L \rightarrow \int g_{rad}^L dN/d\kappa_L d\kappa_L$
 - $\delta \rightarrow {
 m ionization}$ structure of the wind

Line-force parameters

$T_{\rm eff}$	log g	k	α	δ	Fuente				
[K]									
10 000	1.5	0.36	0.54	0.05	A82				
15 000	2.0	0.26	0.51	0.12	A82				
20 000	2.5	0.32	0.56	0.02	P86				
30 000	3.5	0.17	0.59	0.09	P86				
A82: Abbott(1982) - P86: Pauldrach+(1986)									

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β Velocity Law



Velocity law with $\beta = 0.5$

$$v(r) = v_{\infty} \left(1 - b \frac{R_*}{r}\right)^{\beta}$$
 with $b = 1 - \left(\frac{v(R_*)}{v_{\infty}}\right)^{\frac{1}{\beta}}$



Improvements to CAK theory [modified CAK theory or m-CAK]

- Correction for finite star size.
- Inclusion of rotation.

(Pauldrach, Puls & Kudritzki, 1986; Friend & Abbott, 1986)



WLR from m-CAK theory



extragalactic distances using the stellar wind properties (Dmom).

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Rotating radiation-driven winds

Equations for a rotating wind

1D symmetry in the equatorial plane.

Mass conservation: $F_m = 4\pi r^2 \rho v = \text{constant}$

Momentum equation: $v \frac{dv}{dr} = -\frac{1}{\rho} \frac{dp}{dr} - \frac{G M_*(1-\Gamma)}{r^2} + \frac{v_{\phi}^2(r)}{r} + g^L \left(\rho, \frac{dv}{dr}, n_e\right)$

Energy equation \rightarrow Isothermal wind

Rotational rate Ω

$$\Omega = v_{
m rot}/v_{
m crit}$$
 $0 \leqslant \Omega < 1$
 $v_{
m crit} = \sqrt{rac{2GM_*}{3R_*}}$
Maeder & Meynet (2000).

Centrifugal force

$$v_{\phi}^2/r = v_{\rm rot}^2 R_*^2/r^3$$

 $v_{\rm rot}$ is the equatorial rotation speed

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Hydrodynamic solutions

Fast Solution

- Classical (~m-CAK) solution
- High values of the terminal velocity
- Ω < 0.75 (slow rotators)



$\Omega_{\rm slow}$ solution

- Found by Curé (2004)
- Ω > 0.75 (high rotators)
- Low terminal velocities and dense flows



Figures from Curé & Araya (2023) O5V star with $T_{\rm eff}{=}~45\,000$ K, $\log g{=}~4.0,~R/R_{\odot}~=12$

$\delta_{ m slow}$ solution

- Found by Curé et al. (2011)
- For high values of parameter δ (changes in ionization)
- Low terminal velocities and dense flows



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Questions to answer

Most of B-type supergiants are not fast rotators ($\Omega \leq 0.6)$

i.e.: Howarth(2004),Hunter+(2008),Vink+(2010),de Burgos+(2023)

We can rule out the Ω_{slow} solution

We can choose between *fast* and $\delta_{\rm slow}$ solutions

Questions

- In what cases does each solution appear? Can the domains of each solution be delimited in the space of the radiation force parameters?
- Can the wind of B-type supergiants be effectively modeled using $\delta_{\rm slow}$ solutions?
- How do $\delta_{\rm slow}$ solutions modify key relations of radiation-driven wind theory such as the WLR?
- Could the transition between one solution and another explain the variability observed in the spectrum?



Calculation of wind models

Option 1	Option 2	Option 3			
Self-consistent models	Partially consistent models	Non-consistent models			
Input values	Input values	Input values			
$T_{\rm eff}$, log g, R_*, abundances, $\Omega.$	$T_{\mathrm{eff}}, \log g, R_*, \Omega,$ abundances, α , δ , k .	$T_{\rm eff}$, log g, R_* , $\Omega,$ abundances, $\beta,$ $\dot{M},$ v_∞ .			
Method					
1) Selving hydrodynamia anystiana	Method	Method			
and radiation transport in moving media, including radiative acceleration calculated consistently with NLTE	 Solving the hydrodynamic equations adopting a parameterization for the radiative acceleration. 	1) Employing a β velocity law instead of solving the hydrodynamic equations.			
rates. 2) Generating the synthetic spectrum. 3) Comparison with observations	 Solving the radiation transport equation for moving media, using the hydrodynamic solution. 	 2) Solving the radiation transport equation for moving media, using the β law. 3) Obtaining the synthetic spectrum. 4) Comparison with observations. 5) Process iteration. Crowther+(2006), Markova & Puls(2008), Searle+(2008), Haucke+(2018) 			
 4) Iterative refinement process. 	3) Generating the synthetic spectrum.				
Mostly for O-type and WR stars.	4) Comparison with observations.				
Pauldrach+(1994), Krtička & Kubát(2001, 2017),	5) Iterative refinement process.				
Sander+(2017), Sundqvist+(2019), Björklund+(2021), Poniatowski+(2021,2022).	Taresch+(1997), Pauldrach+(2001), Noebauer & Sim(2015), Lattimer & Cranmer(2021)				

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Calculation codes

We choose option 2 because, currently, there are no self-consistent codes that produce the $\delta_{
m slow}$ solution.

Hydrodinamic equations

HYDWIND

Curé and collaborators (Univ. Valparaíso, Chile)

Basic features

- Input: Fundamentales parameters, Ω , k, α y δ .
- Spherical Symmetry Equatorial plane
- Inner boundary condition adopted:

$$\int_{R_*}^{\infty} \sigma_e \rho(r) dr = 2/3 \text{ or } \rho(R_*) = \rho_*$$

- Execution time: few minutes.
- It gives *fast*, Ω_{slow} , or δ_{slow} solutions.
- Output: radial grid, velocities and densities for the wind.

Radiative transfer

FASTWIND

Puls and collaborators (LMU Munich)

Basic features

- Input: Fundamental parameters, hydro solution (or β, v_∞, M).
- Spherical Symmetry.
- NLTE code considering line blanketing.
- Radiative transfer in Sobolev approximation and CMF.
- Unified model (photosphere + wind).
- Diagnostic range: optical.
- Execution time: 15 30 min.
- Output: continuum radiation distribution + line profiles (H, He, Si, C, N, O).



Most suitable δ values for B-type supergiants

Do values of δ higher than ~ 0.25 exist in a stellar wind to achieve a δ_{slow} solution?

Early calculations indicate $\delta \lesssim 0.12$ (Abbott, 1982; Pauldrach+. 1986).

Most recent non-LTE calculations for line-force parameters assume the material to be 'frozen in

ionization' (δ = 0), e.g. Noebauer & Sim(2015), Lattimer & Cranmer (2021), or are limited to O-type

supergiants (Gormaz-Matamala+2019,2022).

 δ values for BSGs

Puls, Springmann & Lennon (2000) analytically derived $\delta\gtrsim 1/3$ for a medium composed of neutral hydrogen as a trace element.

Kudritzki (2002) demonstrated that $\delta\sim 1$ for winds of low optical depth and very low metalicity.

We postulate that BSGs have a different ionization structure compared with O-type stars.

First, we examine the distribution of solution domains based on the values of the line-force parameters (k, α, δ) .

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Solution domains in δ and Ω space



There exists a distinct gap between fast and δ_{slow} solutions.

The HYDWIND code does not identify any stationary solution within the gap. The gap is consistently present in all models, regardless of the values of $T_{\rm eff}$, log g, or Ω .

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Interaction between k and δ , and the wind parameters

Model T19

 $egin{array}{c} lpha &= 0.5 \ \Omega &= 0 \end{array}$

The value of v_{∞} remains unchanged when different values of *k* are considered.

There is no change in the position or width of the gap (in δ space).





Interaction between k and δ , and the mass-loss rates

Dependence of solutions on the parameter k

The mass loss can either increase or decrease with δ , depending on the value of k, in both the *fast* and the δ_{slow} regimes.

Model T19

There is no change in the position or width of the gap (in δ space).





Interaction between k and δ , and the wind parameters

Dependence of solutions on the parameter k

Model T19

The change in the slope of \dot{M} as a function of $\delta_{\rm slow}$ for k = 0.1, 0.2, and 0.32. In contrast, the slope in v $_{\infty}$ does not change.





Interaction between α and δ , and the wind parameters

Model T19

In contrast to the parameter k, α completely modifies the terminal velocities.

 \dot{M} is also highly sensitive to this parameter.

Changing the value of α also alters the gap in δ .





Gap Properties

Gap location



- δ_m represents the average value of δ across the edges of the gap.
- The location of the gap is almost independent of T_{eff}.
- For B supergiants exhibiting higher rotation rates, the gap is located at small values of δ.



Gap width



- $\Delta \delta$ is the width of the gap in δ values.
- The width decreases as Ω increases.
- Gaps are narrower in models with lower $T_{\rm eff}.$

Gap Properties







- There is little to no change in v_{∞} for low $T_{\rm eff}$.
- The jump increases in magnitude for faster rotators.



- The jump in \dot{M} is smaller for larger rotators.
- M
 ⁱ can double its value if changes in δ result in crossing the gap.

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Line profiles from different wind regimes



$H\alpha$ line profiles

The models have nearly identical values of Q.

The H α profiles generated by the *fast* and δ_{slow} regimes are quite similar.

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$H\alpha$ line profiles

$H\alpha$ line profiles for different wind regimes (model T19) Ω=0.0 Ω=0.2 Ω=0.4 Ω=0.6 720 698 671 504 0.47 0.50 0.57 0.76 δ=0.0 Dependence of -13.01 -12.97 -12.84 -12.57 $H\alpha$ on Ω and δ 2 543 525 0.47 468 241 0.44 0.56 0.78 δ=0.1 Sample of $H\alpha$ line profiles for model T19. -12.86 -12.81 -12.66 -12.09 2 409 391 221 0.38 0.41 0.64 Terminal velocities and Flux/Fc Gap δ=0.2 1 mass-loss rates [in -12.74 -12.67 -12.11 units of 2 266 255 232 $10^{-6} M_{\odot} \text{ yr}^{-1}$]. The 202 0.29 0 48 0.27 0.36 values of log Q are at δ=0.3 bottom right. -12.60 -12.55 -12.40 -12.18 2 231 225 208 183 0.07 0.08 0.12 0.25 δ=0.4 -13.10 -13.02 -12.78 -12.40 185 5568 λ(Å)

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$H\alpha$ line profiles





$H\alpha$ line profiles



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Comparison with observations





Comparison with observations

Star	S pectral type	T _{eff} (kK)	log g (dex)	R_* (R_{\odot})	log L/L _☉ (dex)	$v \sin i$ (km s ⁻¹)	(km s^{-1})	v_{mic} (km s ⁻¹)	v_{mac} $(km s^{-1})$
HD 47 240	B1 Ib	19.0	2.40	30	5.02	95	122	10	60
HD 99 953	B1/2 Iab/b	19.0	2.30	25	4.87	50	64	18	50
HD 41 117	B2 Ia	19.0	2.30	23	4.79	40	51	10	65
HD 80 077	B2 Ia + e	17.7	2.20	195	6.53	10	13	10	10*
HD 92 964	B2.5 Ia	18.0	2.20	70	5.67	45	58	11	40
HD 53 138	B3 Ia	18.0	2.25	46	5.30	40	51	10	80*
HD 75 149	B3 Ia	16.0	2.10	61	5.34	40	51	11	52
HD 42 087	B4 Ia	16.5	2.45	55	5.31	80	103	15	80
HD 58 350	B5 Ia	15.0	2.00	54	5.12	40	51	12	70
HD 79 186	B5 Ia	15.8	2.00	61	5.32	40	51	11	53
HD 74 371	B6 Iab/b	13.7	1.80	73	5.23	30	39	10	60
HD 34 085	B8 Iae	12.7	1.70	72	5.08	30	39	10	52

Stellar parameters (Haucke+2018)

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Comparison with observations



Observations were performed at CASLEO using the REOSC spectrograph (2005-2015).

A subsample of stars was selected based on the presence of emission in the $H\alpha$ line profile.



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Comparison with observations



$H\alpha$ line profiles

Fast regime fittings

When fitting the line profiles, we primarily focus on adjusting the emission component of the P Cygni profile.

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Comparison with observations



 $\delta_{\rm slow}\,$ regime fittings

The wings appear slightly improved compared to the *fast* case.

However, many absorption components are still too deep.



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Comparison with observations



There are no significant differences between the H α fittings for both the *fast* and δ_{slow} regimes.

 ${\rm H}\alpha \\ {\rm dichotomy} \\$





Wind parameters from fittings

Fast regime

Star	Ω	v _{crit}	v_{∞}	Ń	k	α	δ	$\log D_{mon}$
HD 47240	0.55	222.5	347.2	0.075	0.070	0.500	0.000	26.96
HD 99953	0.33	191.7	193.8	0.080	0.090	0.494	0.150	26.69
HD 41117	0.27	183.9	306.9	0.179	0.113	0.520	0.000	27.22
HD 80077	0.03	470.0	-	-	-	-	-	-
HD 92964	0.20	287.1	317.5	0.640	0.120	0.500	0.200	28.03
HD 53138	0.21	238.8	227.5	0.205	0.190	0.420	0.170	27.30
HD 75149	0.23	224.8	450.1	0.443	0.155	0.480	0.000	27.99
HD 42087	0.35	290.7	622.8	0.826	0.530	0.420	0.000	28.38
HD 58350	0.27	187.5	179.0	0.184	0.240	0.420	0.170	27.18
HD 79186	0.24	209.2	399.1	0.714	0.140	0.510	0.000	28.15
HD 74371	0.22	176.8	211.9	0.323	0.190	0.450	0.120	27.57
HD 34085	0.25	154.0	256.3	0.339	0.150	0.500	0.050	27.67

$\delta_{\rm slow}$ regime

Star	Ω	v_{crit}	v_{∞}	Ň	k	α	δ	$\logD_{\rm mom}$	$v_{\infty}^{\mathrm{Ha18}}$	$\dot{M}^{\rm Ha18}$	β^{Ha18}	$\log D_{\rm mom}^{\rm Ha18}$
HD 47240	0.55	222.5	161.3	0.020	0.090	0.500	0.300	26.04	450	0.24	1	27.57
HD 99953	0.33	191.7	152.5	0.061	0.080	0.530	0.320	26.47	500	0.13	2	27.33
HD 41117	0.27	183.9	160.0	0.089	0.095	0.510	0.240	26.63	510	0.17	2	27.38
HD 80077	0.03	470.0	211.0	6.379	0.606	0.300	0.295	29.07	200	5.4	3.2	28.86
HD 92964	0.20	287.1	207.0	0.363	0.130	0.505	0.350	27.60	370	0.49	2	27.98
HD 53138	0.21	238.8	211.2	0.149	0.090	0.550	0.320	27.13	600	0.24	2	27.79
HD 75149	0.23	224.8	181.6	0.171	0.185	0.480	0.310	27.18	350	0.2	2.5	27.54
HD 42087	0.35	290.7	230.4	0.354	0.452	0.480	0.405	27.58	700	0.57	2	28.27
HD 58350	0.27	187.5	182.5	0.181	0.120	0.550	0.290	27.18	233	0.15	3	27.21
HD 79186	0.24	209.2	185.3	0.381	0.110	0.550	0.300	27.54	400	0.4	3.3	27.90
HD 74371	0.22	176.8	157.6	0.247	0.163	0.501	0.270	27.32	155	0.23	2.6	27.22
HD 34085	0.25	154.0	138.5	0.176	0.180	0.500	0.280	27.11	155	0.23	2.6	27.22

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Comparison with values from previous works



- Generally, the δ_{slow} solution yields the lowest values for the wind parameters.
- The fast solution provides values greater than those predicted by the β law.
- The measured values of v_∞ (UV) exceed those obtained by all models.

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Solution domains in δ and Ω space



There exists a distinct gap between fast and δ_{slow} solutions.

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Discussion

Wind momentum - Luminosity relation



- The WLR based on the δ_{slow} solution models is close to the empirical behaviour of the mid-B supergiants (Kudritzki+,1999).
- The WLR based on the *fast* solution is in better agreement with the results from Haucke+(2018) using a β-law.
- Both relations show a considerable dispersion.



Linear regressions

 $\delta_{
m slow}$ regime

 $\log D_{mom} = 1,48 \log L/L_{\odot} + 19,30$

fast regime

 $\log D_{mom} = 1,43 \log L/L_{\odot} + 20,11$

Discussion



The gap and the variability

- A change in wind regime can occur as a result of variations in δ.
- A higher rotational rate Ω reduces the required change in δ to transition between regimes.
- Could these changes in regime be due to binaries or stellar pulsations?

Jumping the gap



Conclusions

Hydrodynamic solutions

- We determined the domains of hydrodynamic solutions. The fast and δ_{slow} regimes are separated by a gap where no stationary solutions were found using the available codes.
- This distribution of domains is consistent across spectral subtypes.
- Rotation affects the distribution of domains.

Line profiles

- For the first time, we have fitted synthetic line profiles computed with the hydrodynamic solution δ_{slow} to observed ones for B supergiant stars.
- H α line profiles can be fitted with both fast and δ_{slow} models.
- The \u03c6_{slow} solution could be suitable for modeling the winds of certain B supergiants.
- Our fits predict a WLR close to that found for intermediate B supergiants.
- However, this solution is constrained by the maximum terminal velocity the wind can achieve. Consequently, it cannot account for the measured (or estimated) v_{∞} values in the UV for B supergiants.



Future work

- Given that H\u03c6 may not be the most suitable line for determining the most appropriate wind regime, this analysis should be expanded to include other spectral ranges, particularly IR and UV.
- This study analyzed only 12 stars. To reach a definitive conclusion, a larger sample is needed.
- Since the only hypergiant B in the sample was fitted exclusively with the δ_{slow} solution, further testing on a larger sample of hypergiants B would be intriguing. Moreover, some published works suggest employing a double-β velocity law, which closely resembles the δ_{slow} solution.
- The variability observed in the spectra of these stars could be explained by certain scenarios involving alternations in hydrodynamic solutions.

Models of Peculiar Stars Group



Introduction Solution Domains Comparison with observations Discussion and Conclusions



The End



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Discussion

Escenario

 Una mancha caliente en la superficie de una SG con viento dominado por la solución rápida.

Su alta ionización origina una región con viento dominado por la solución δ_{slow} (lento y denso).

- Cambios de régimen secuenciales en el período rotacional.
- Posible origen de (DACs).

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Modelo CIR





Una curiosidad



Key words: stars: massive — stars: rotation: starspots — stars: winds, outflows technique: photometry — technique: spectroscopy

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