

# **Astronomická spektroskopie**

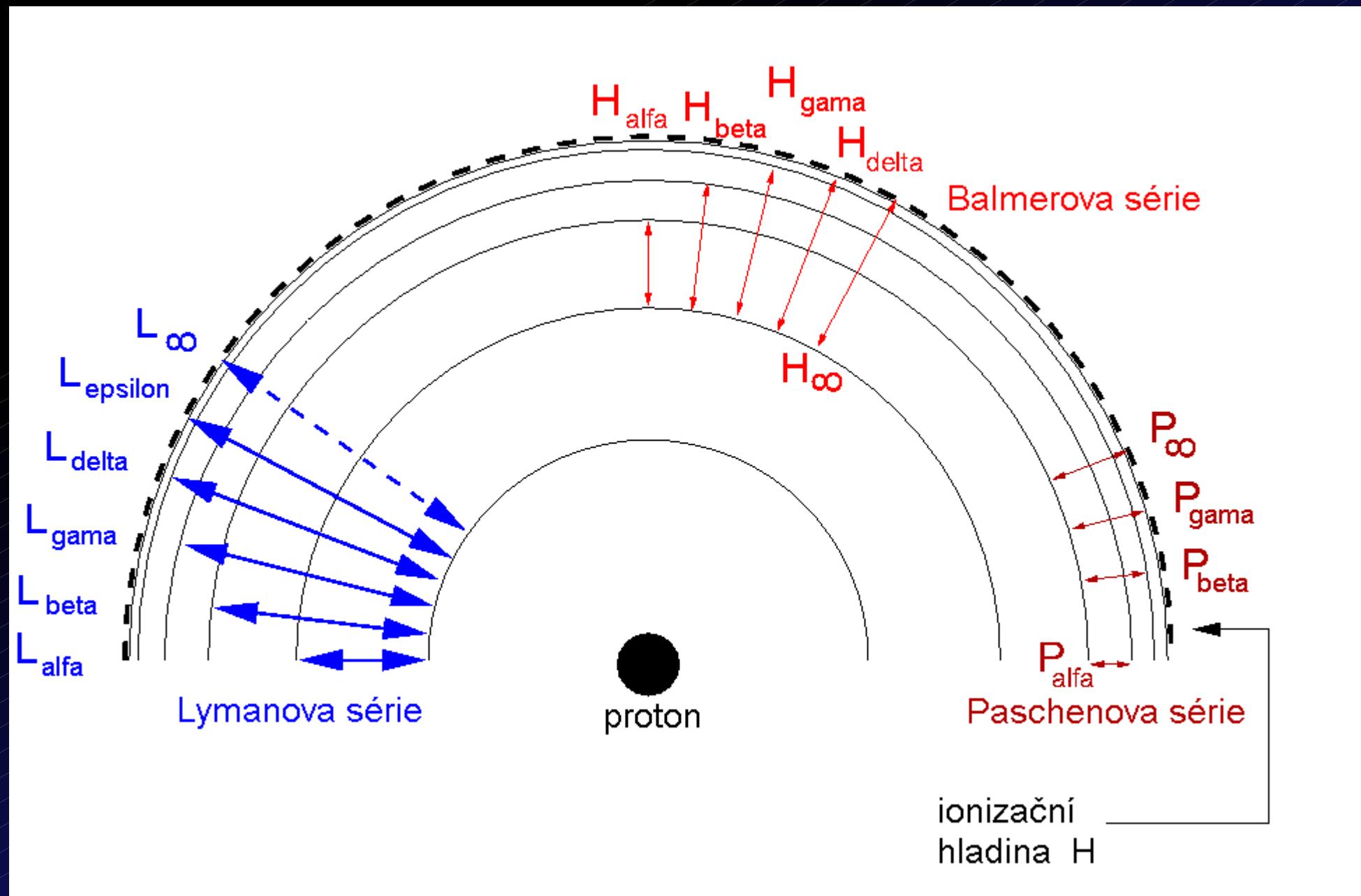
## **Základy a aplikace**

Petr Škoda  
Astronomický ústav AVČR

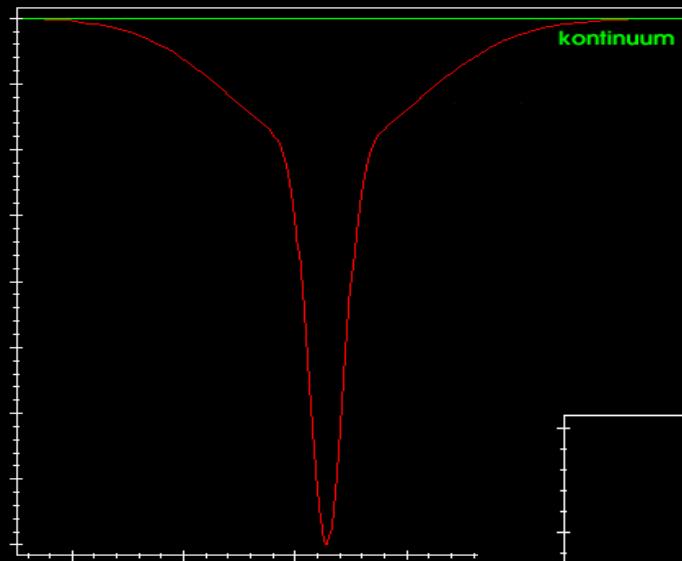
S použitím materiálu od J. A. Smitha (GEMINI) a M. Šlechty (ASU Ondřejov)

Workshop o amatérské spektroskopii, Valašské Meziříčí 5.5.2007

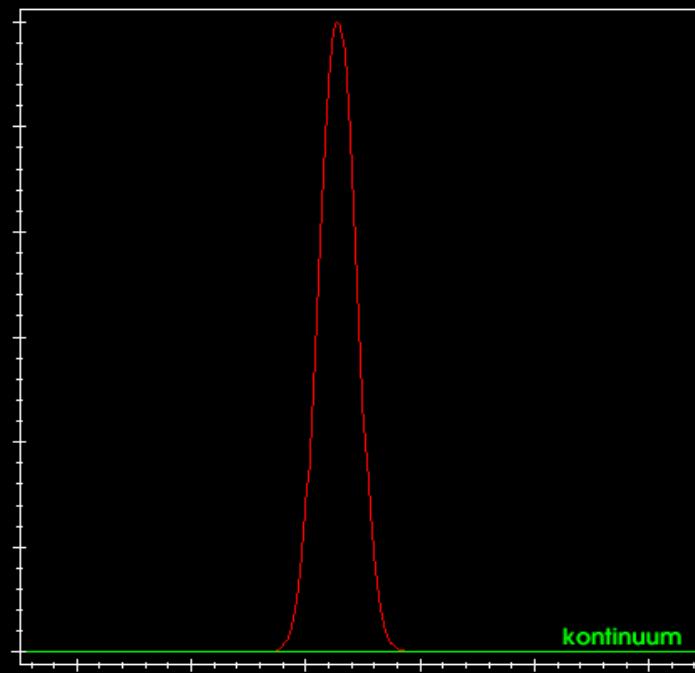
# Vznik spekter



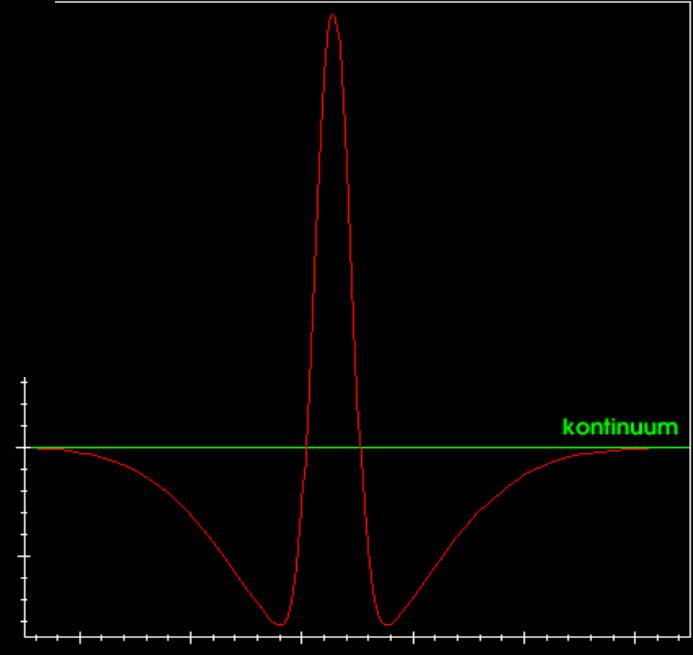
# Typy čar



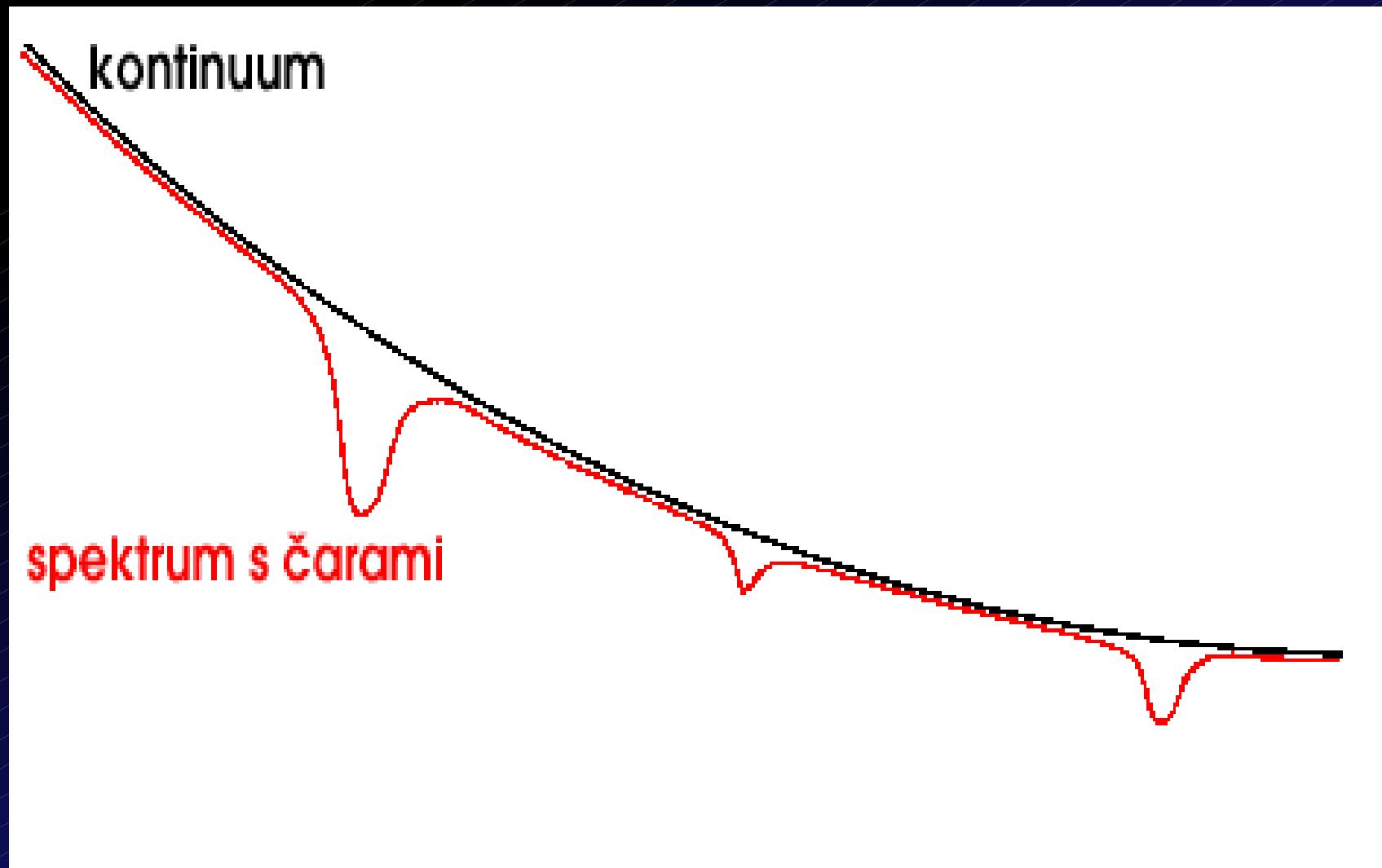
emisní čára (bez absorpčních křidel)



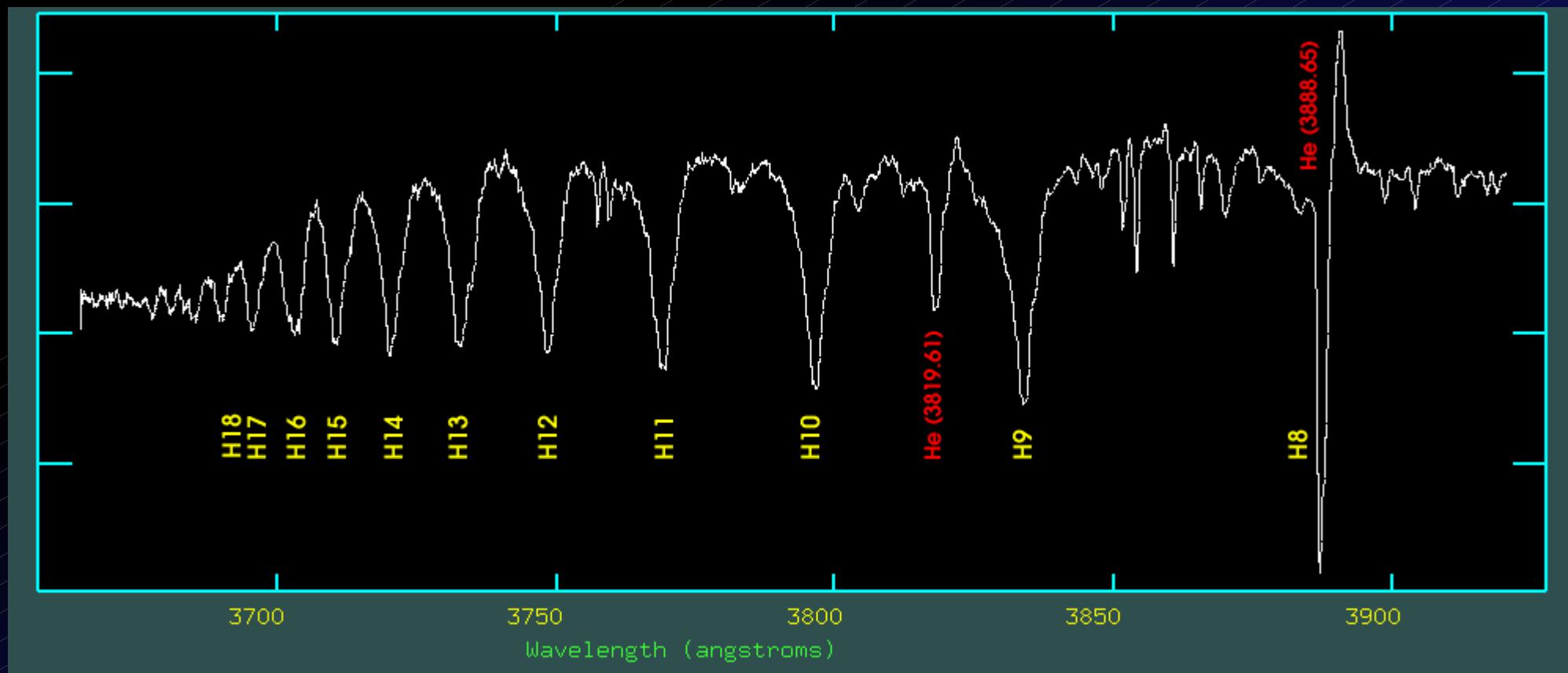
emisní čára (s absorpčními křídly)



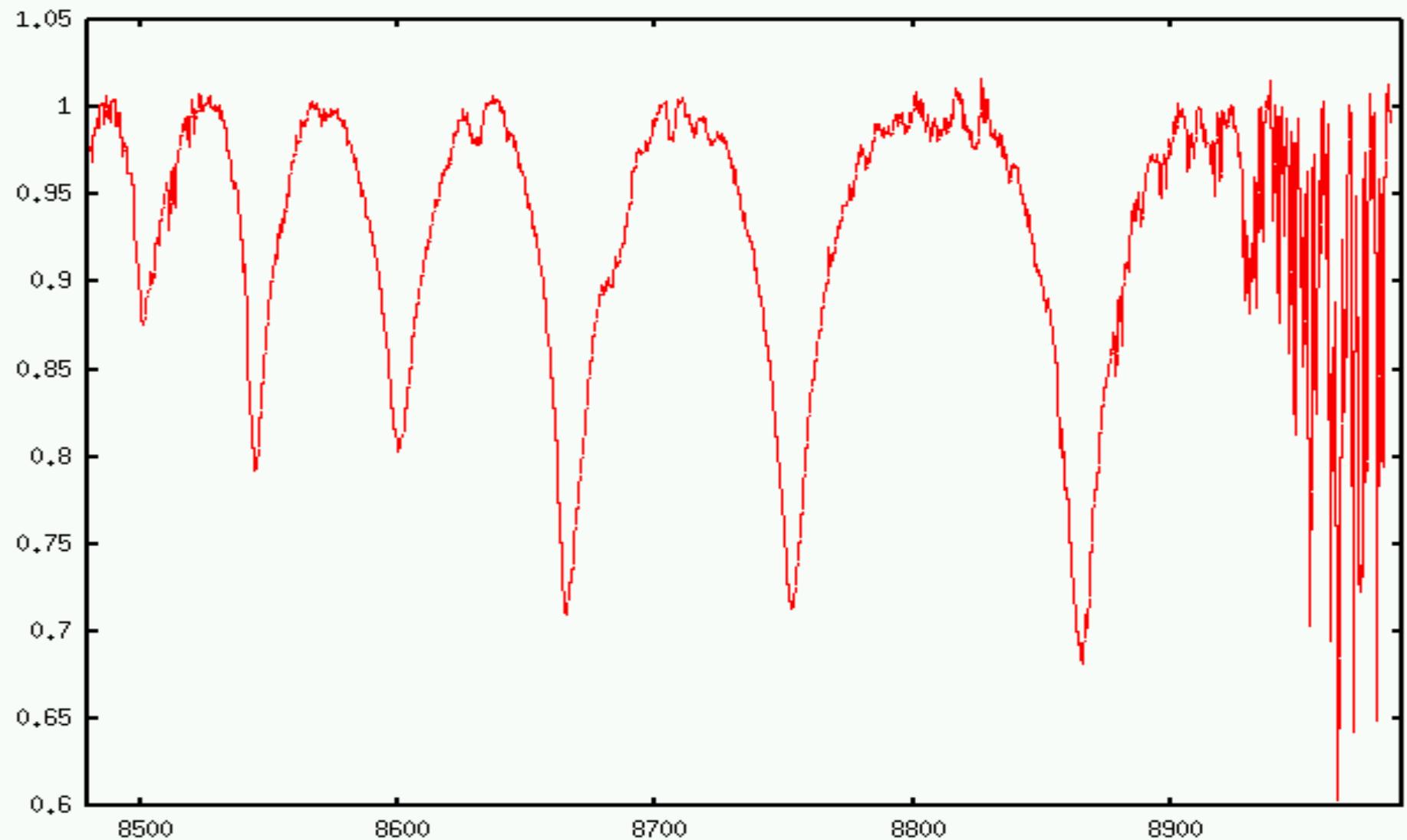
# Tvar kontinua (Planck ?)



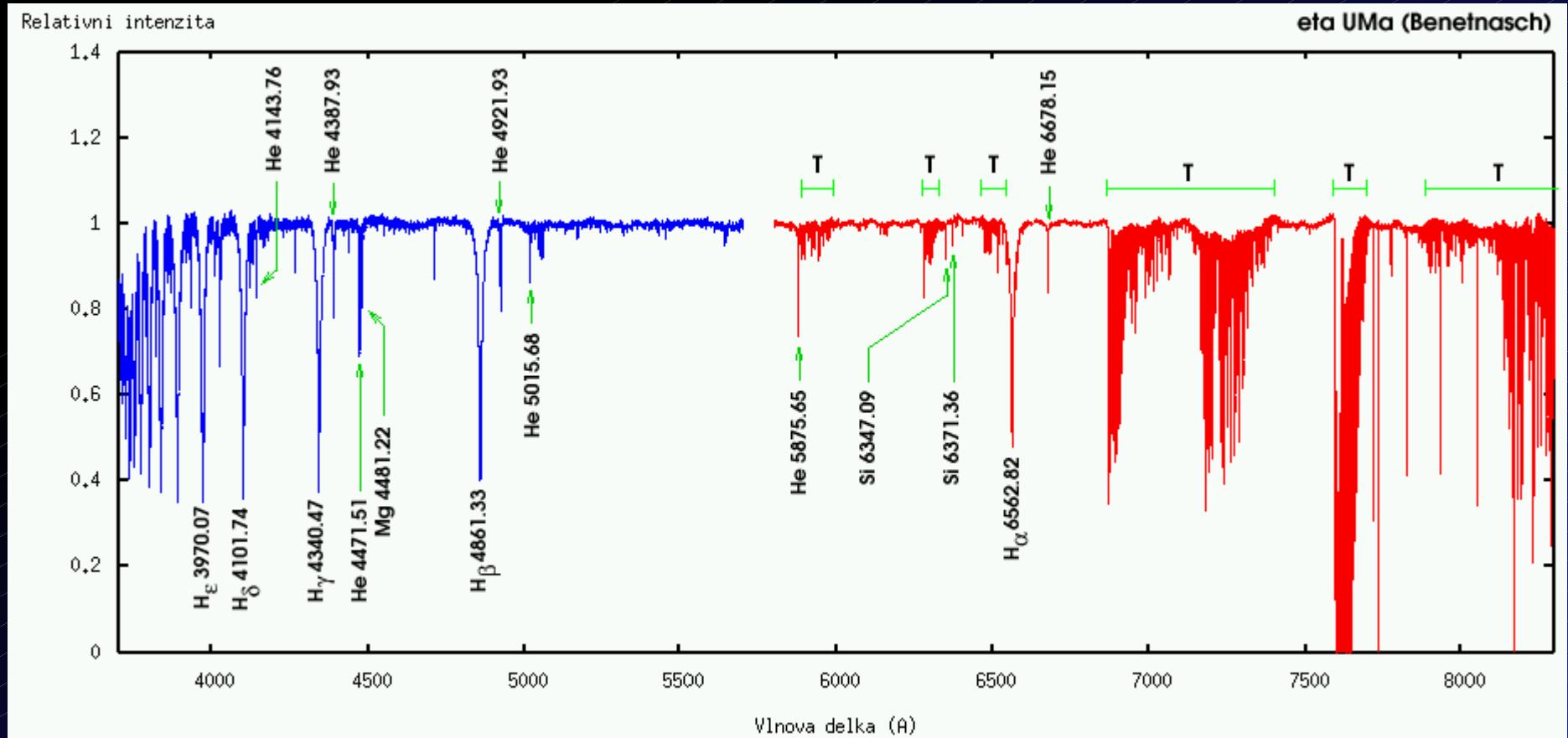
# Balmerova hrana



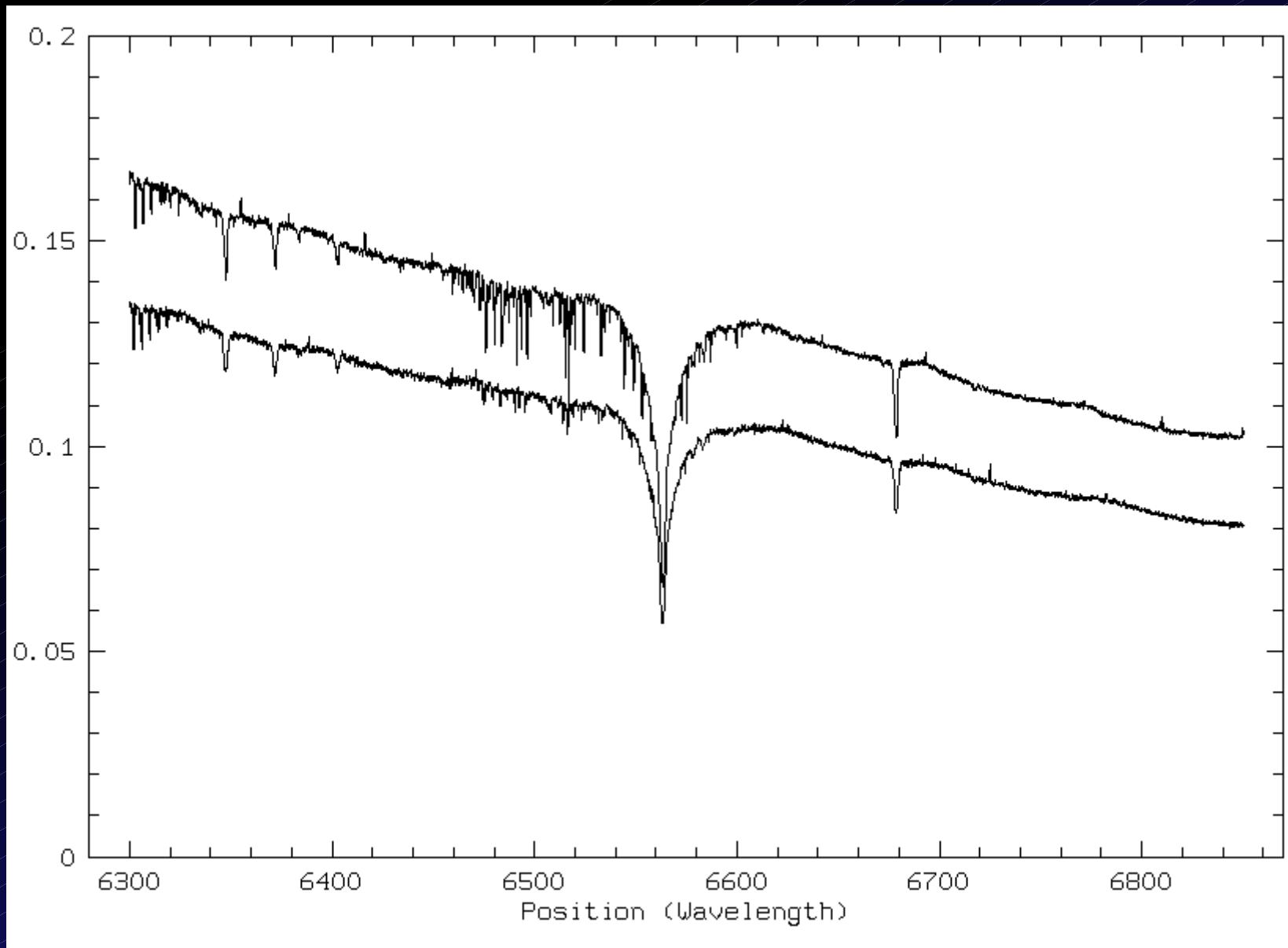
# Paschenova hrana



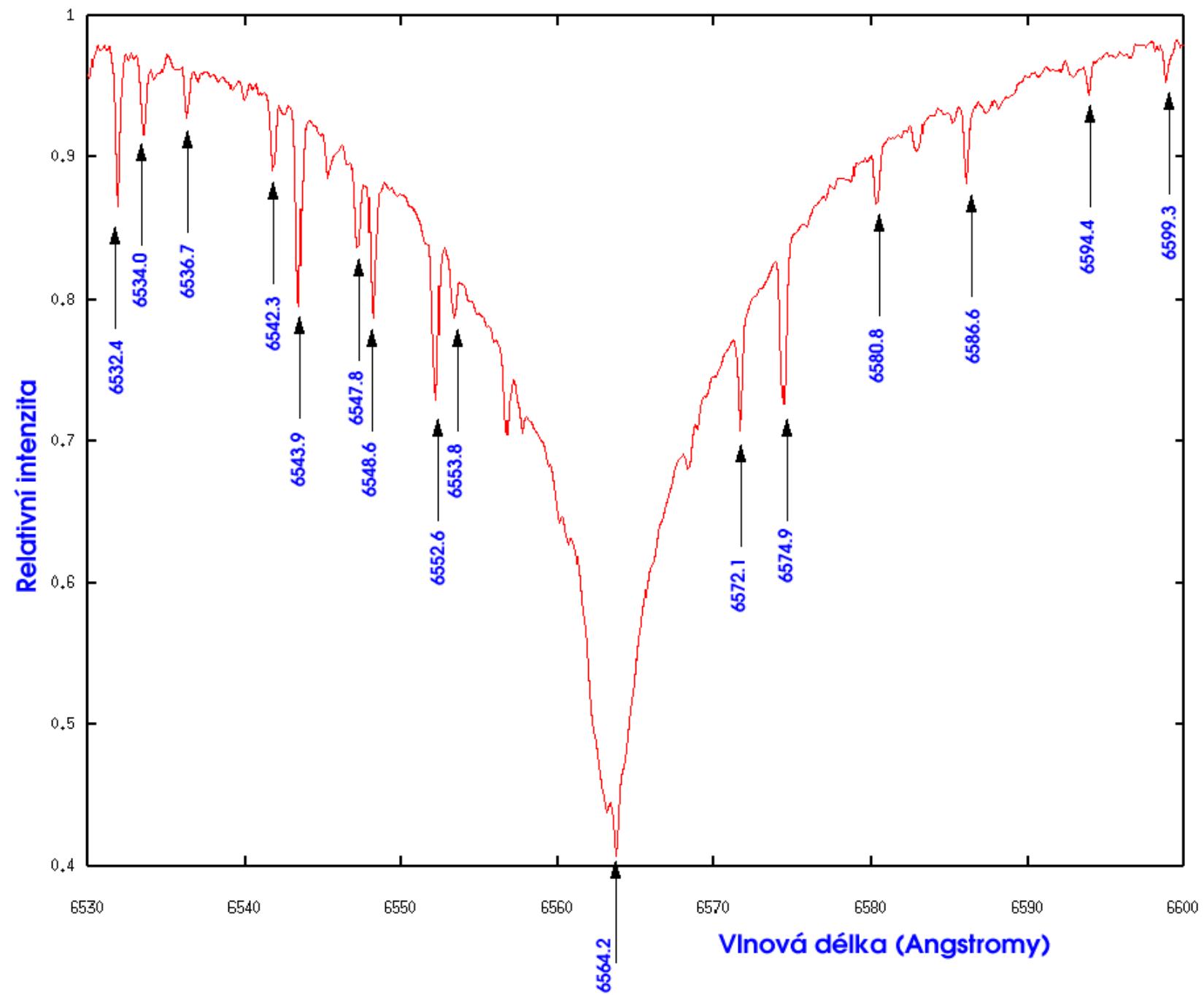
# Typické čáry horkých hvězd



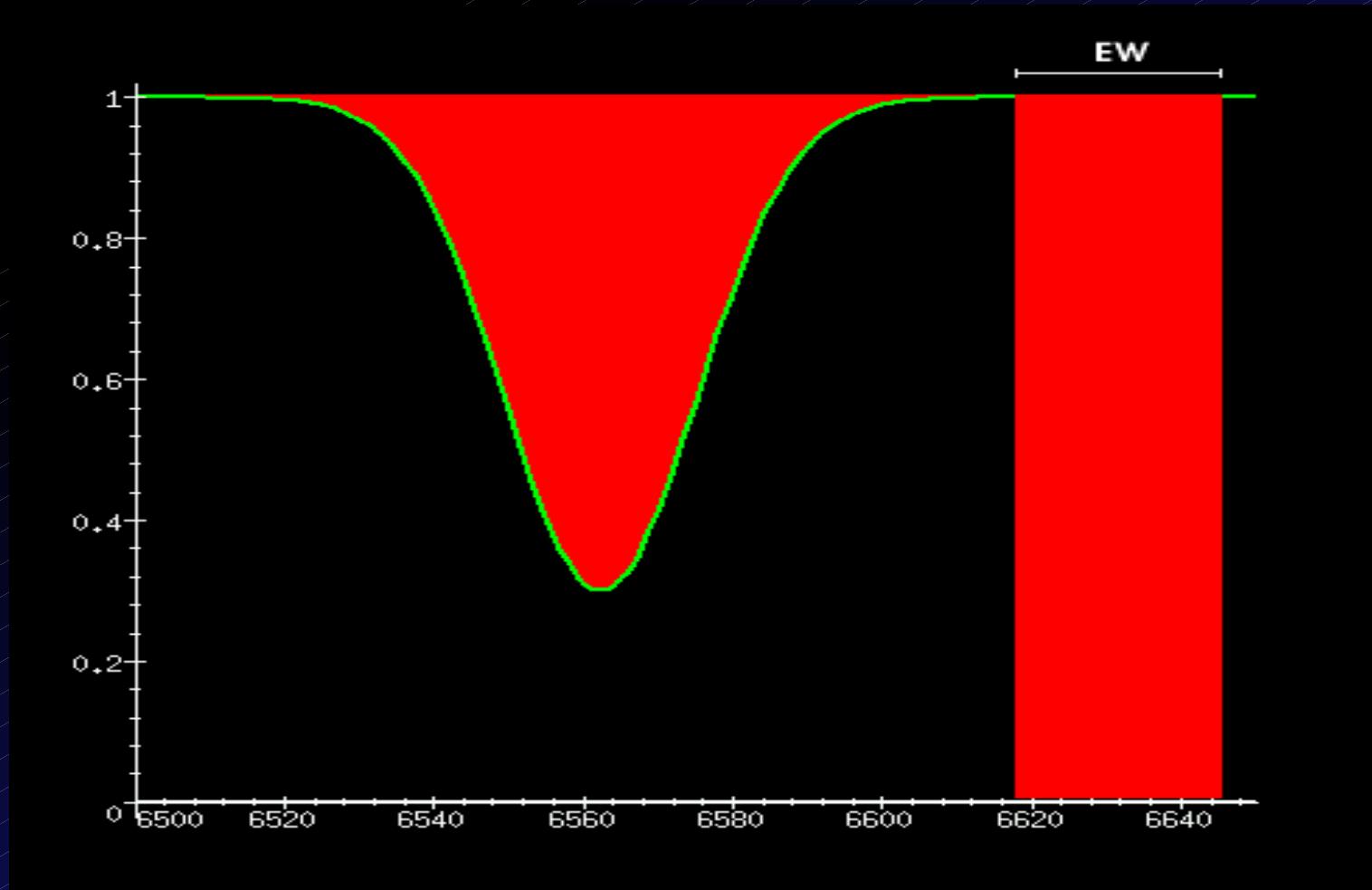
# Telurické čáry – vlhkost



## Polohy telurických čar v oblasti čáry vodíku H alfa

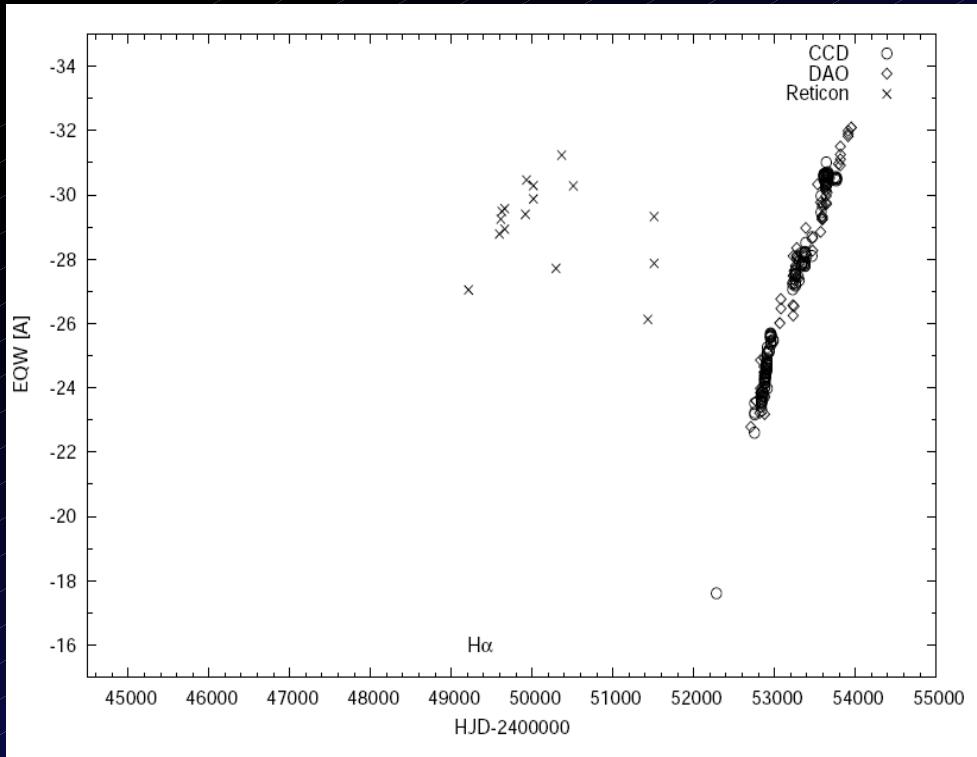


# Ekvivalentní šířka

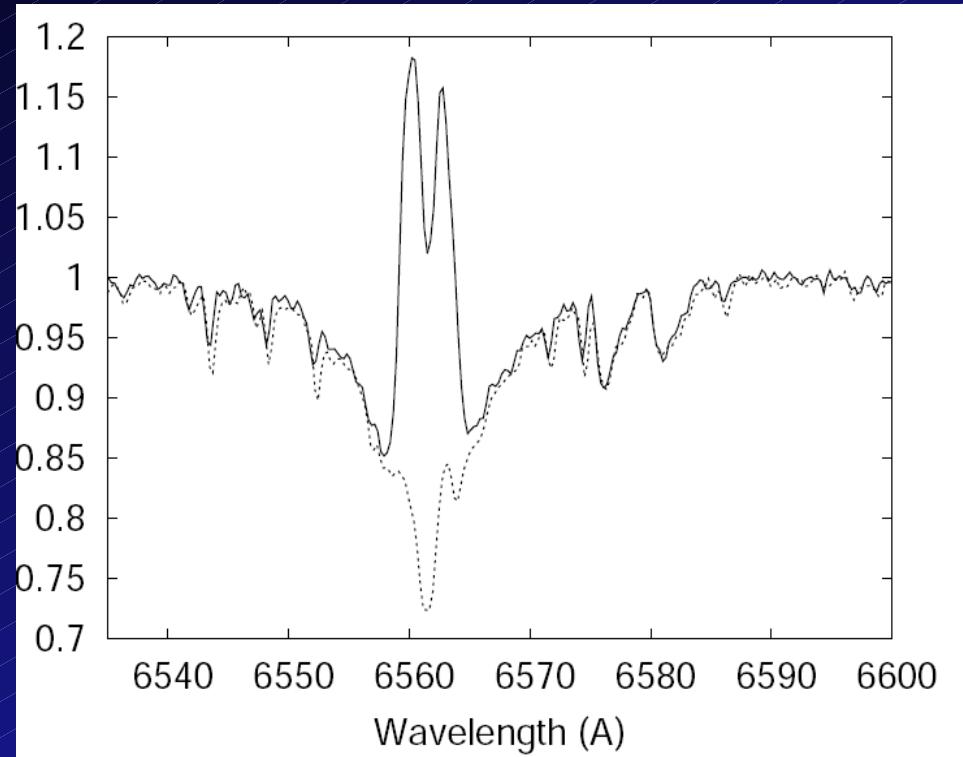


# Changes of EW in Time

- Moments in general (asteroseismology – mode identification)
- Emission lines – negative EW
- Estimates of expanding shell
- Sensitive to continuum placement – shallow lines
- Abundances - check normalization – different lines same ion

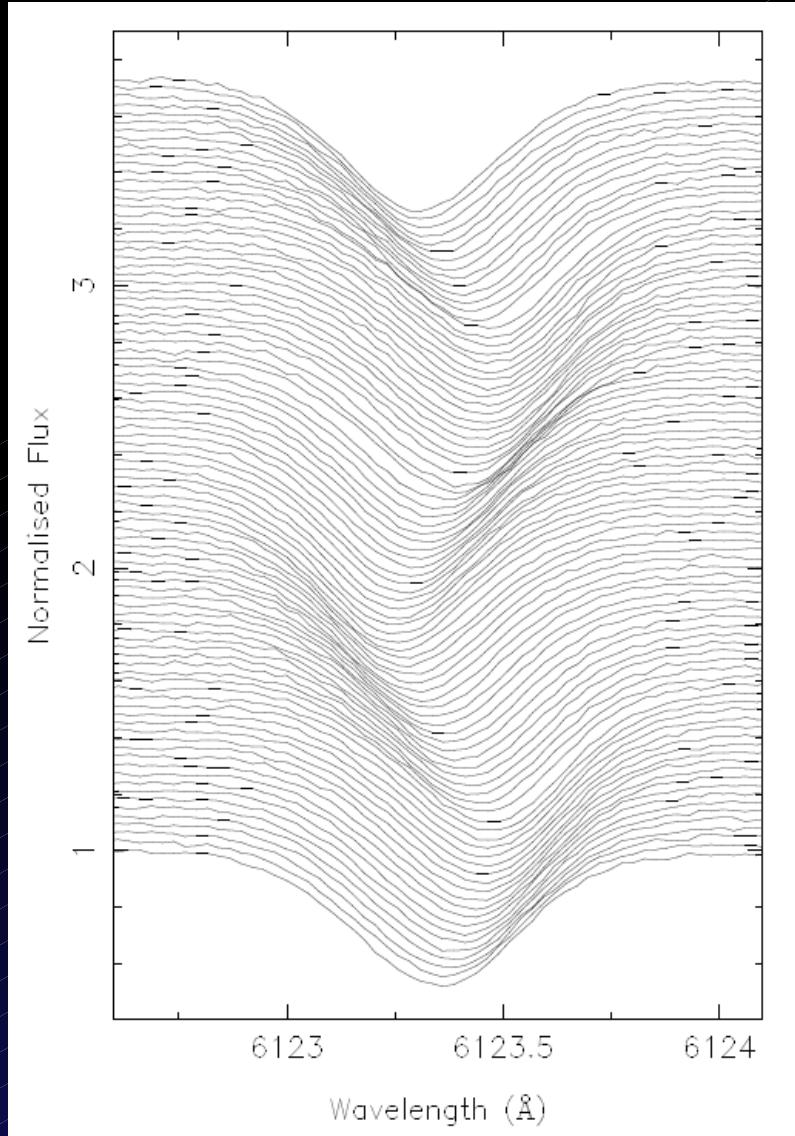


Omi Cas : Koubeky et al. 2004

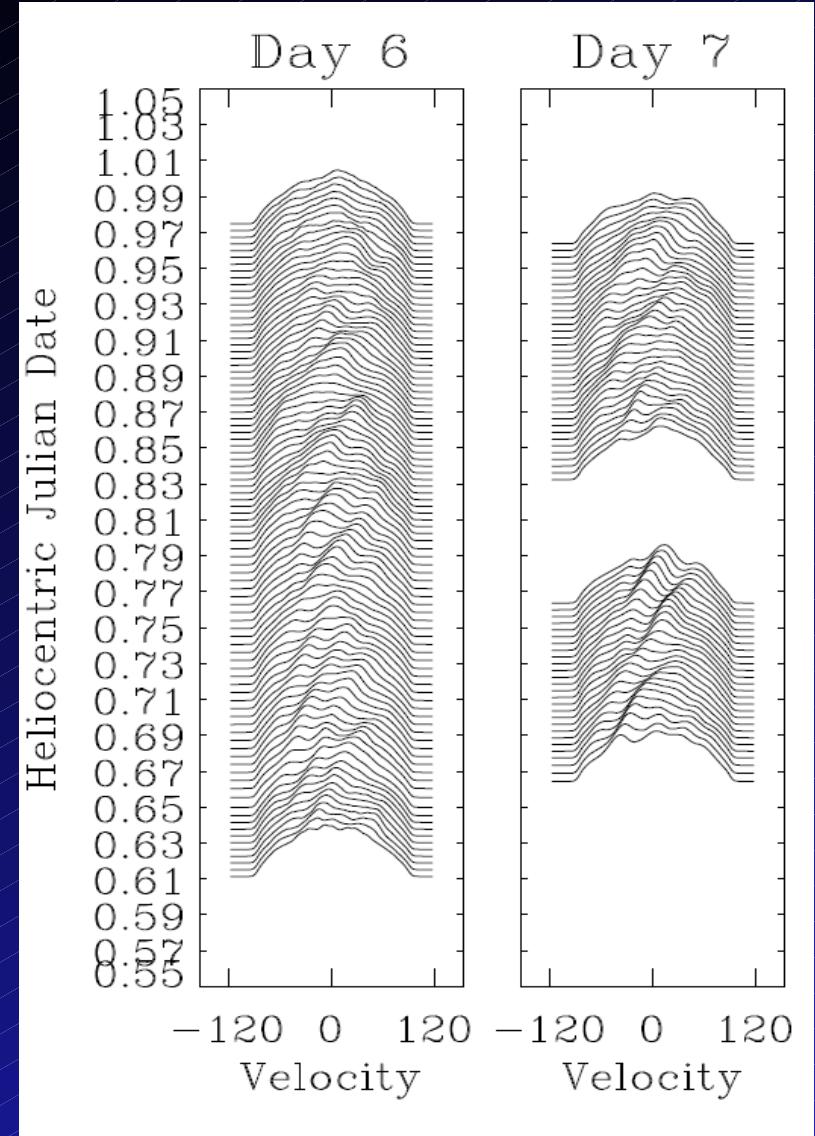


HD6226 : Slechta and Skoda 2004

# Measured Pulsations

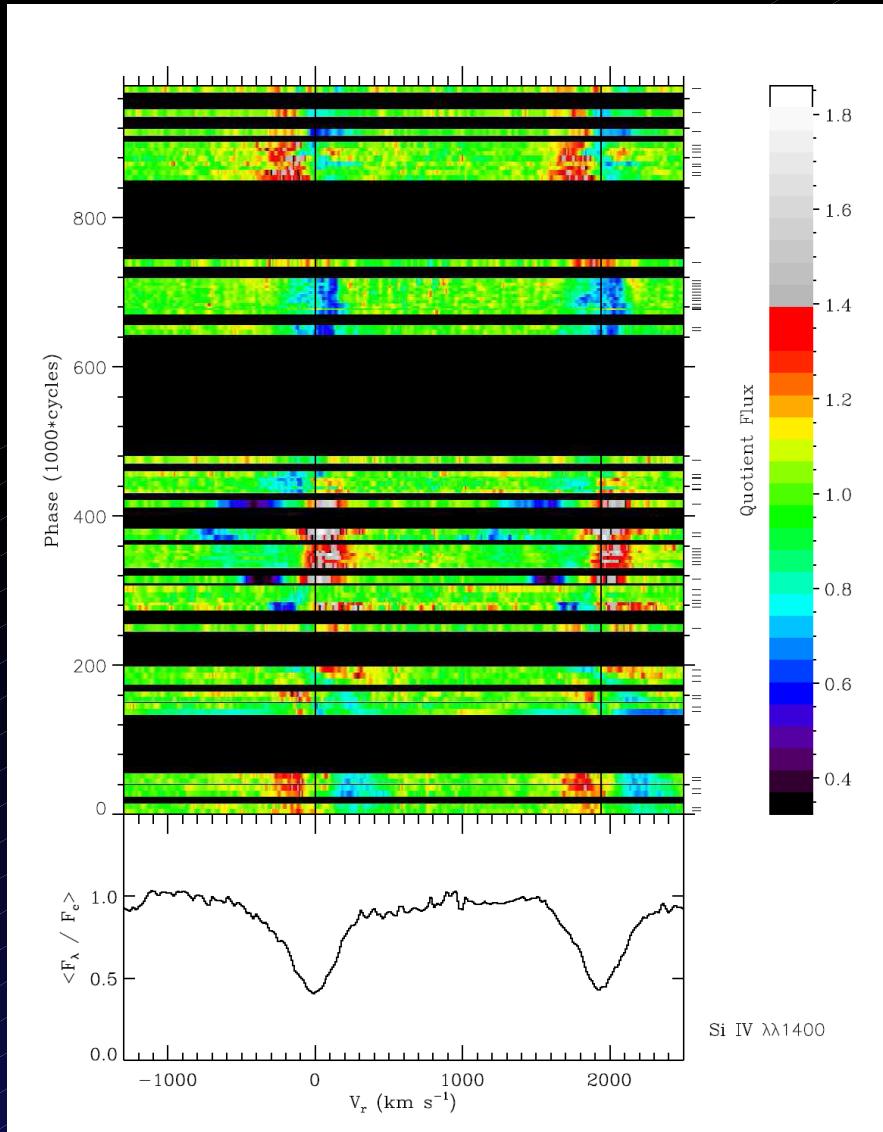


Rho Pup – del Sct type



Eps Cep - del Sct type

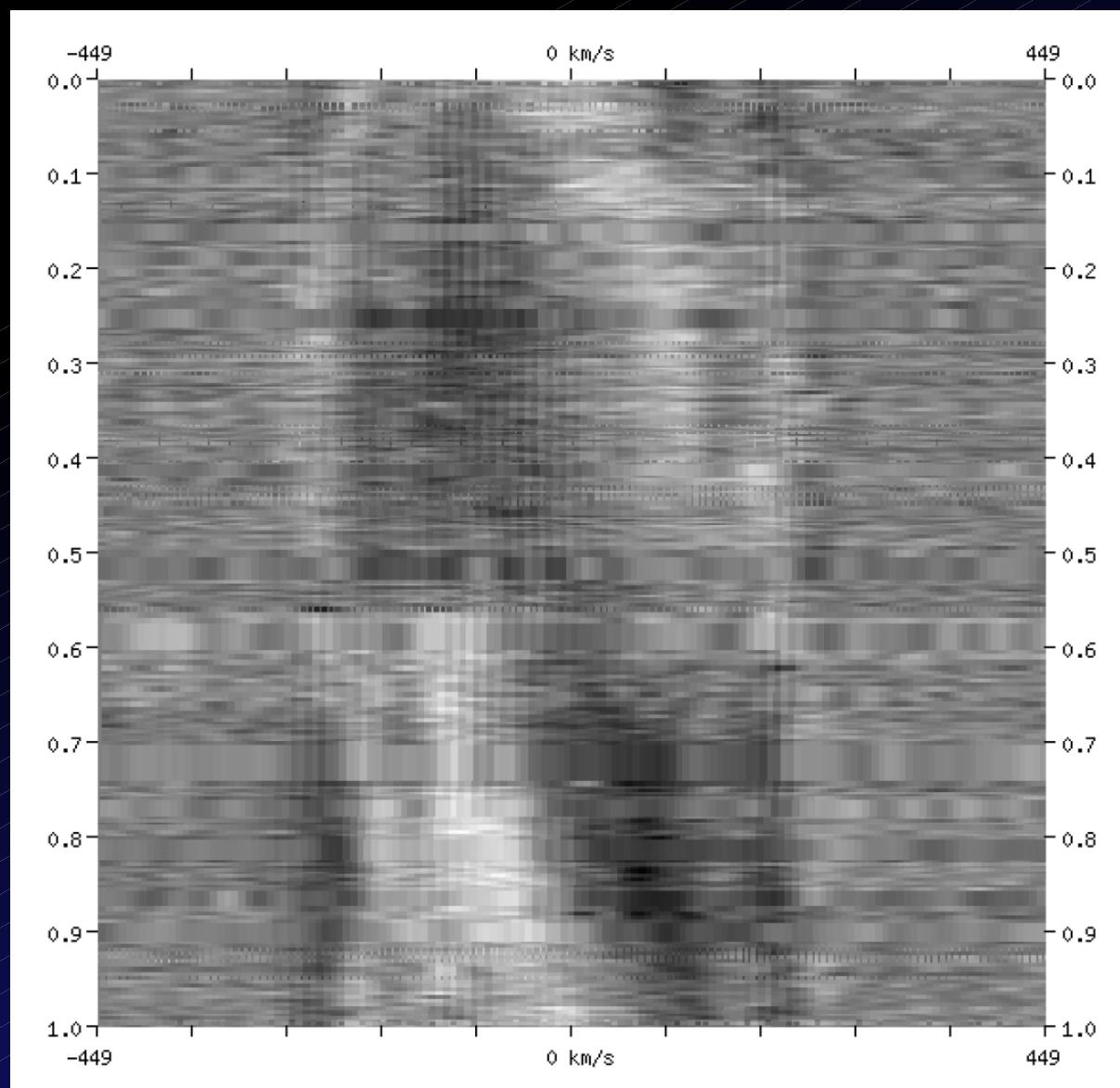
# Dynamic Spectra



Interactive features, color cuts, LUT  
Multiple lines at the same time  
Quotient or Differential  
X axis : lambda or RV  
Y axis : phase or time

For study of LPV (asteroseismology, winds)  
Requires  
time (JD) - winds  
period (see Period analysis) - phase (LPV)  
change of template (average, median)  
removing bad data (interactive overplotting)

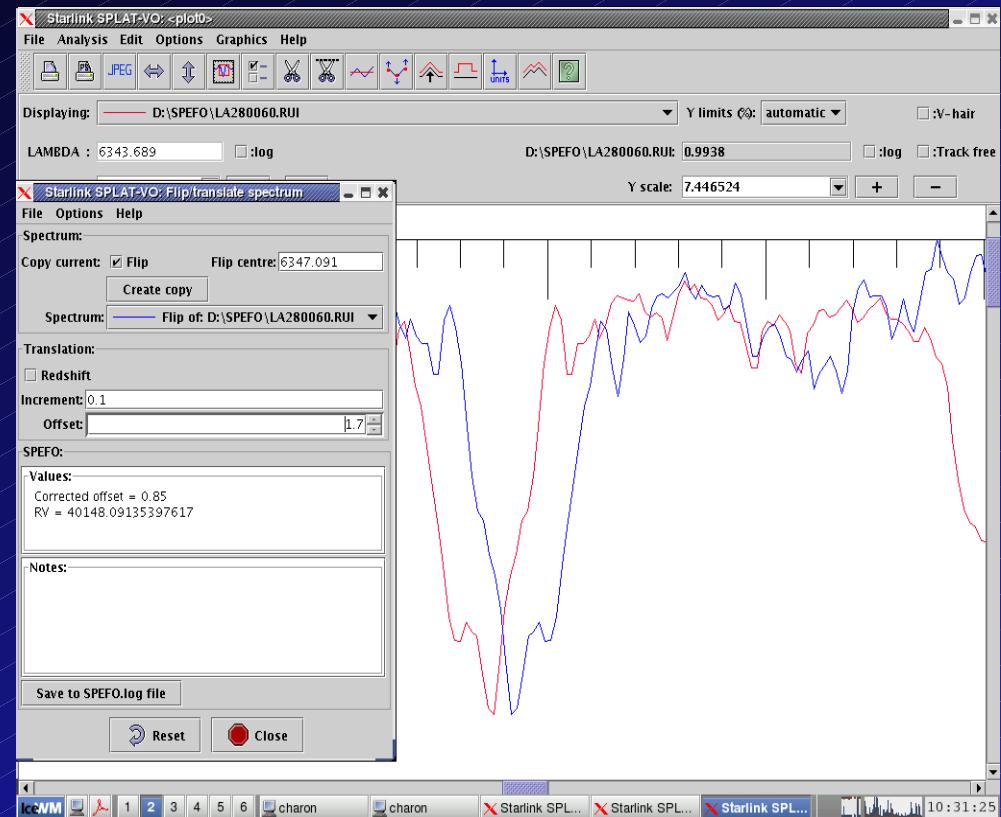
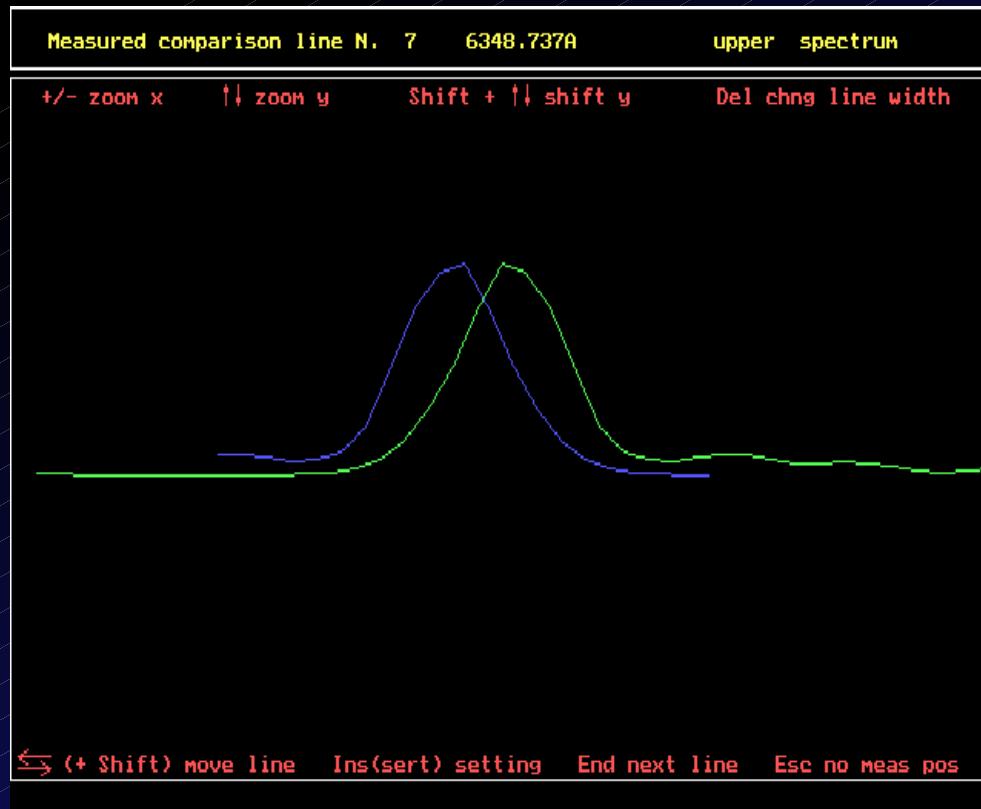
# Dynamic Spectra



Netolický 2004

# RV by Mirroring

Shift until best match of direct and flipped profile - interactive  
Complicated profiles (Be)  
Adjustable region of interest (wing/core)  
Needs reference line position

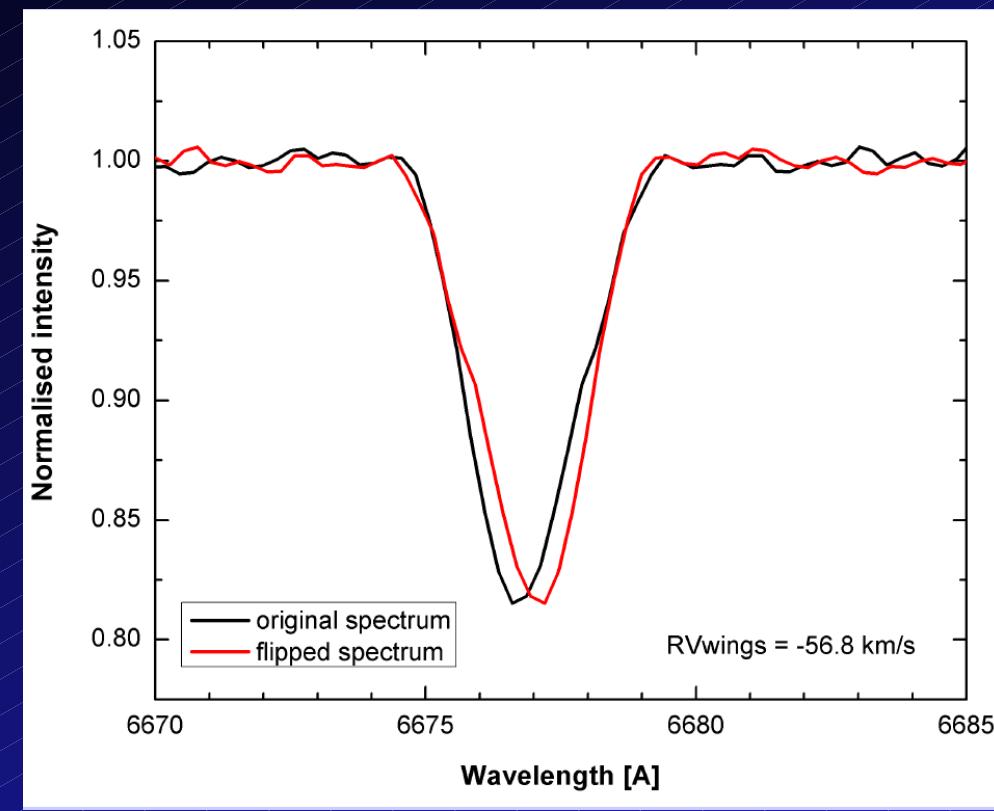
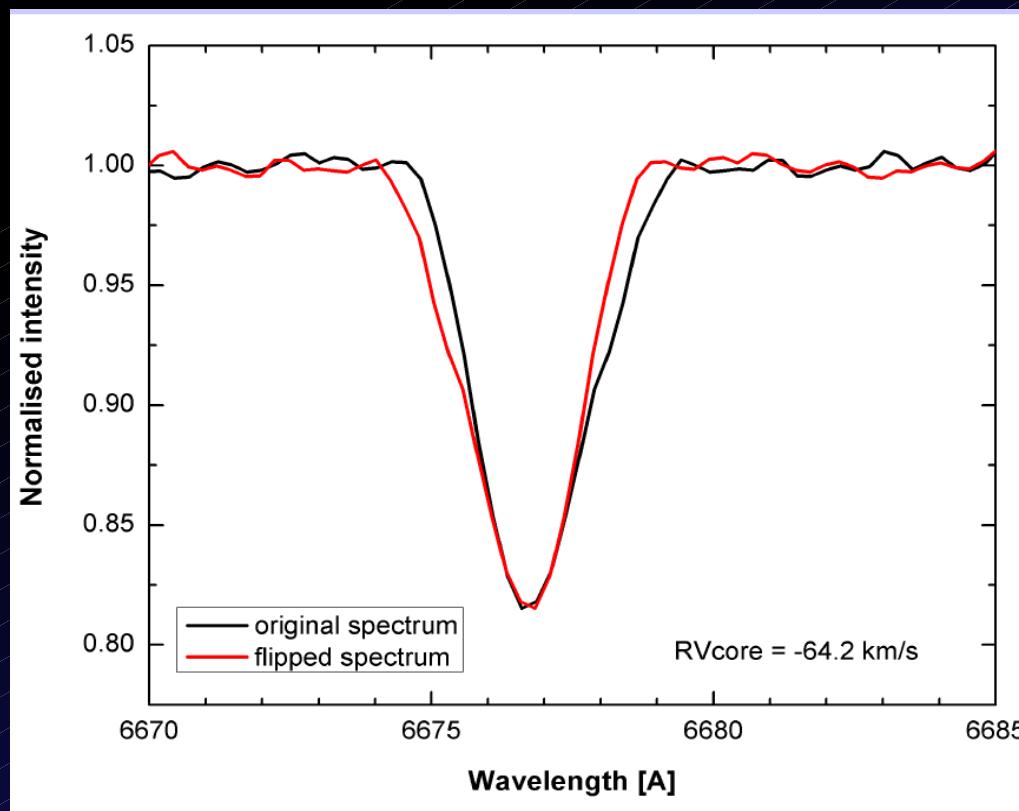


# Mirroring Method

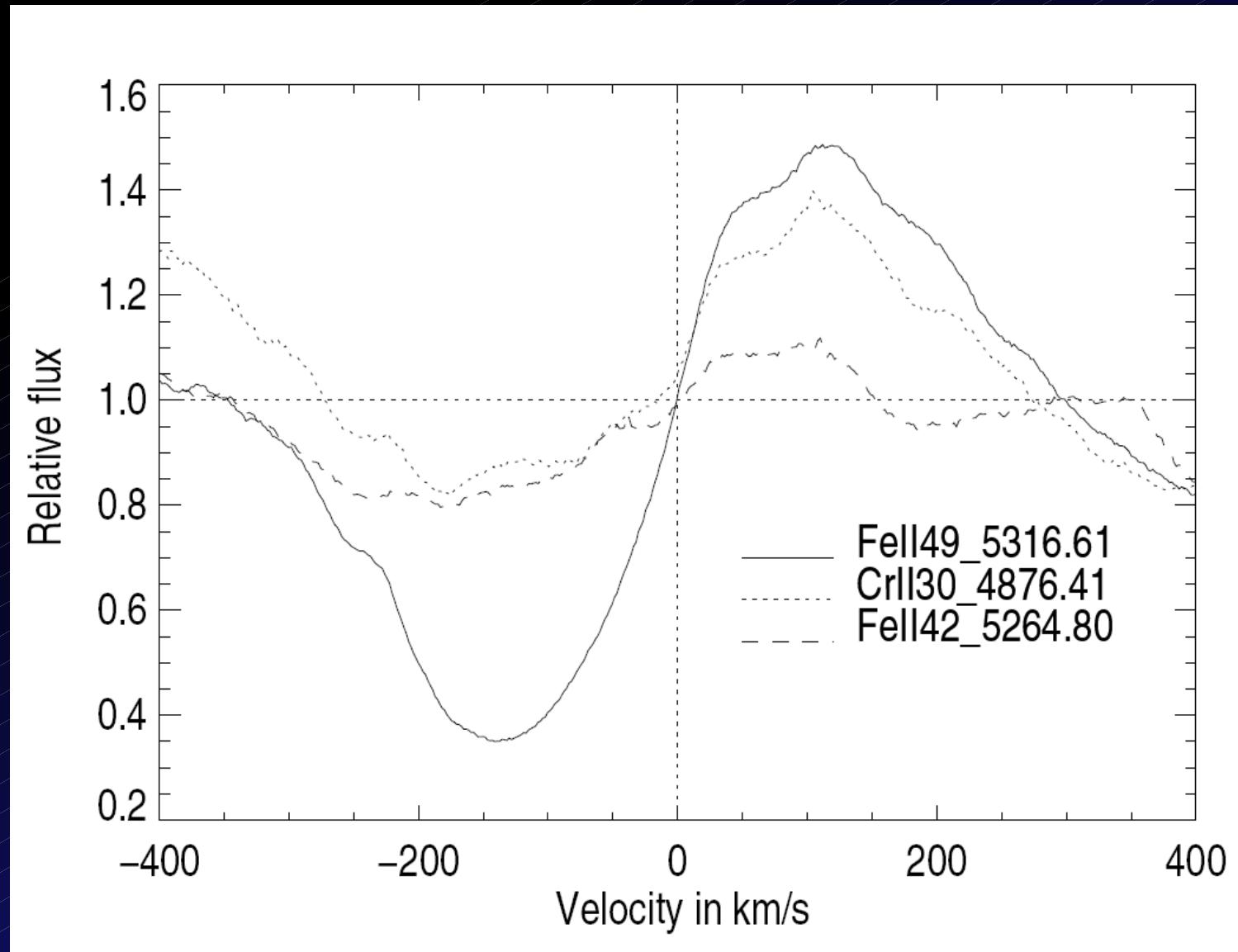
Separate match of core from match of wings – where in depth ?

Different physics (shells, shears, winds)

Asymmetry – how to handle ?



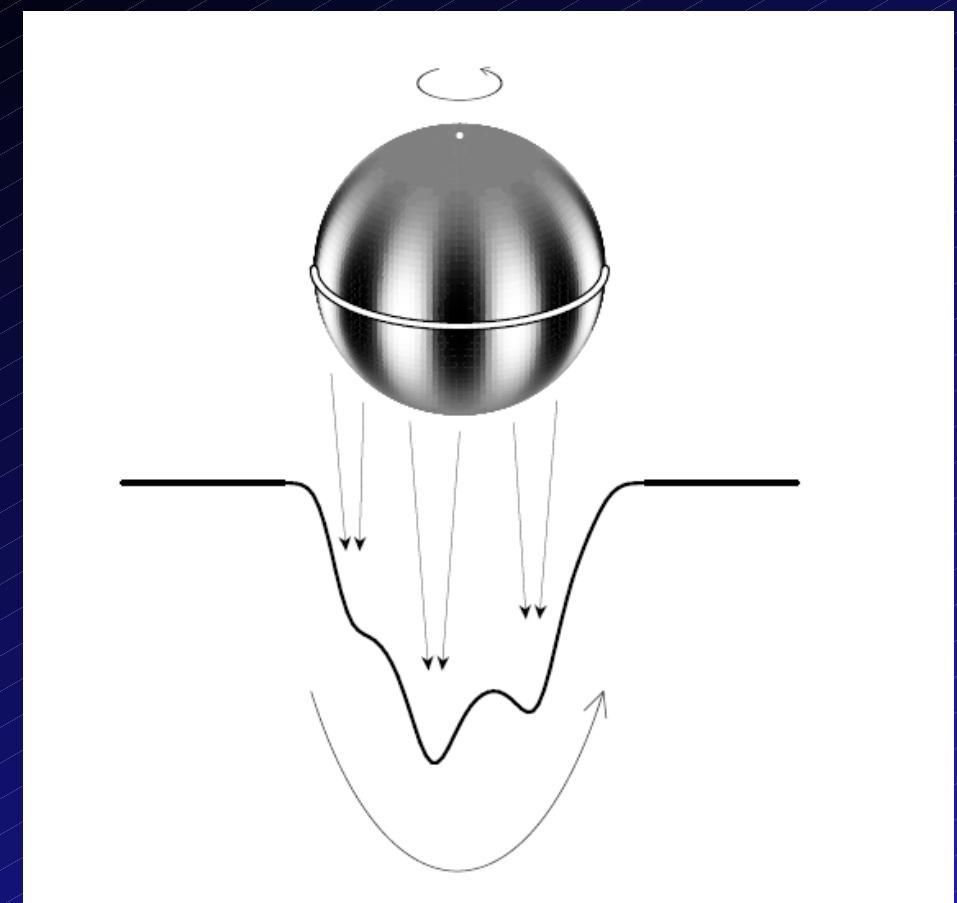
# Different Lines overplotted RV scale



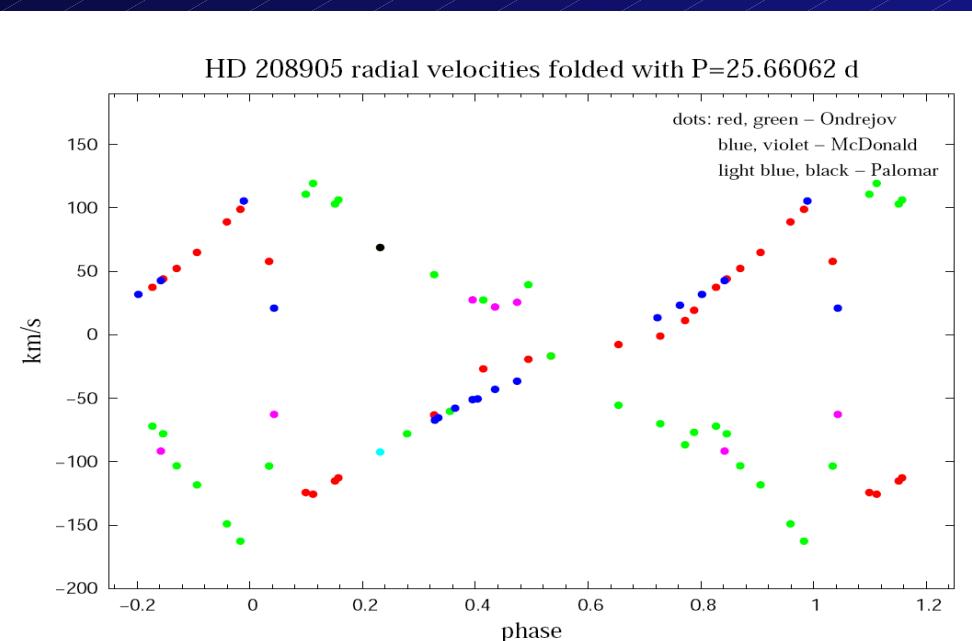
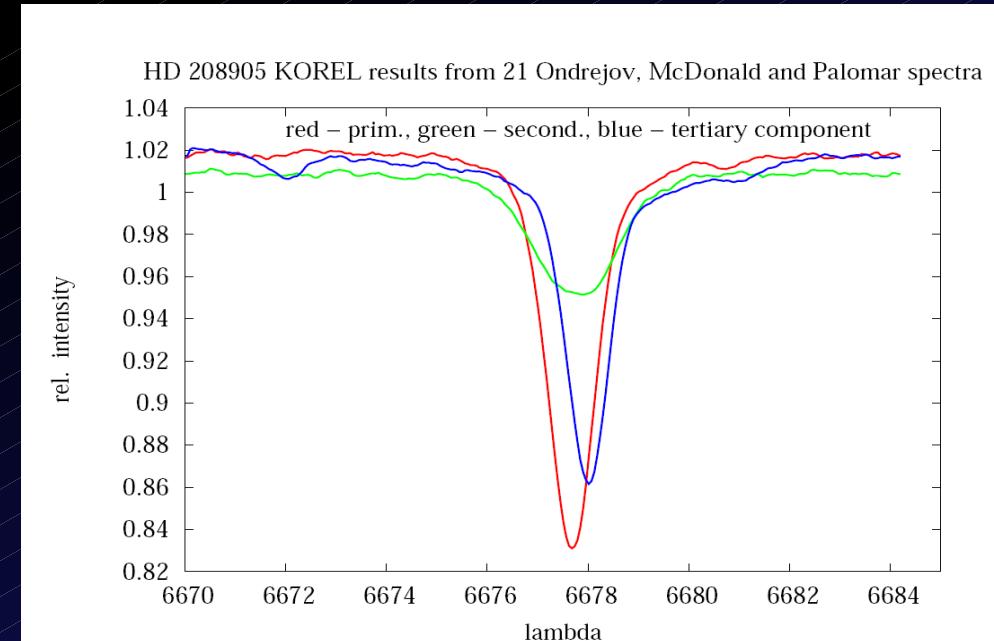
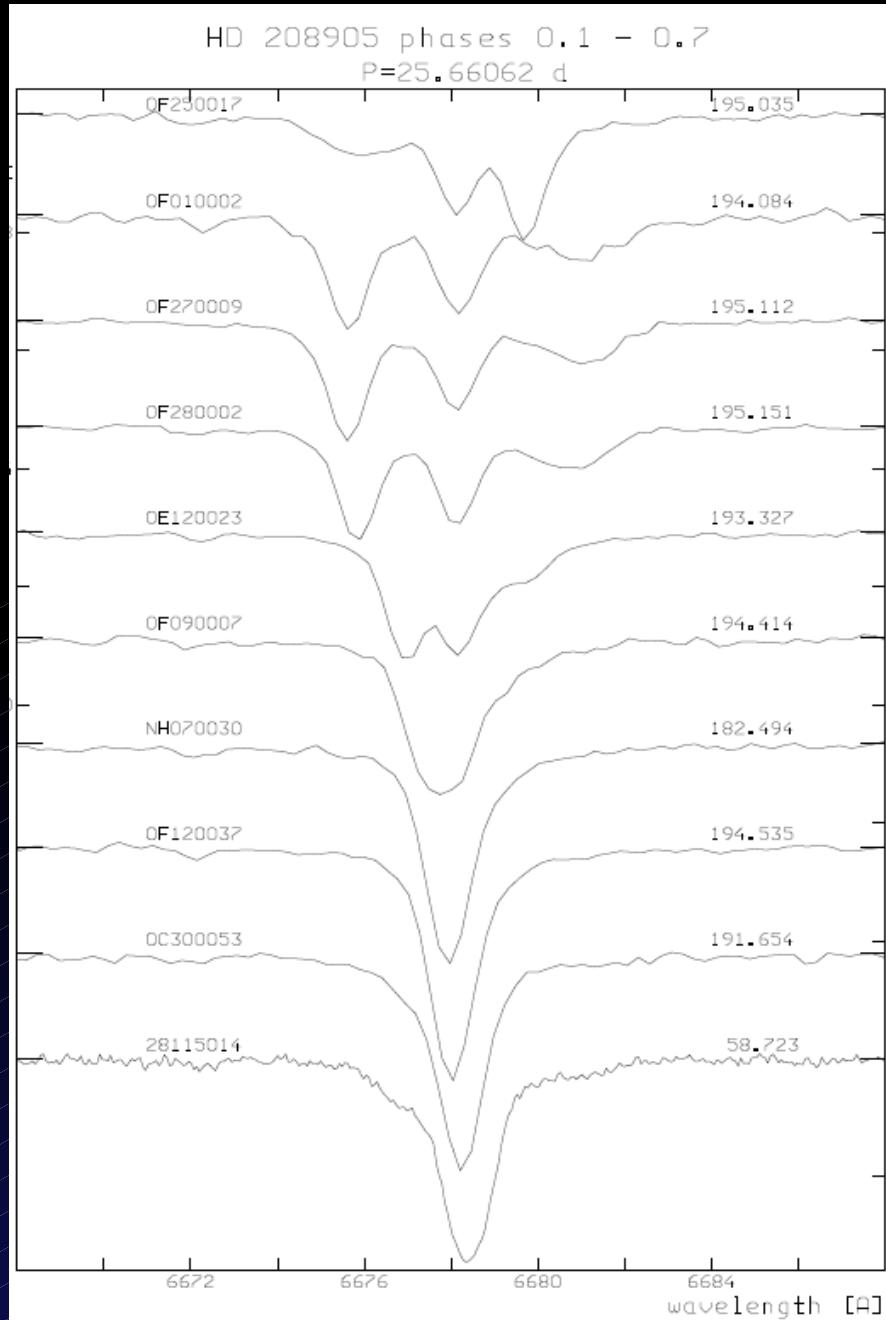
# Doppler Imaging - Bumps

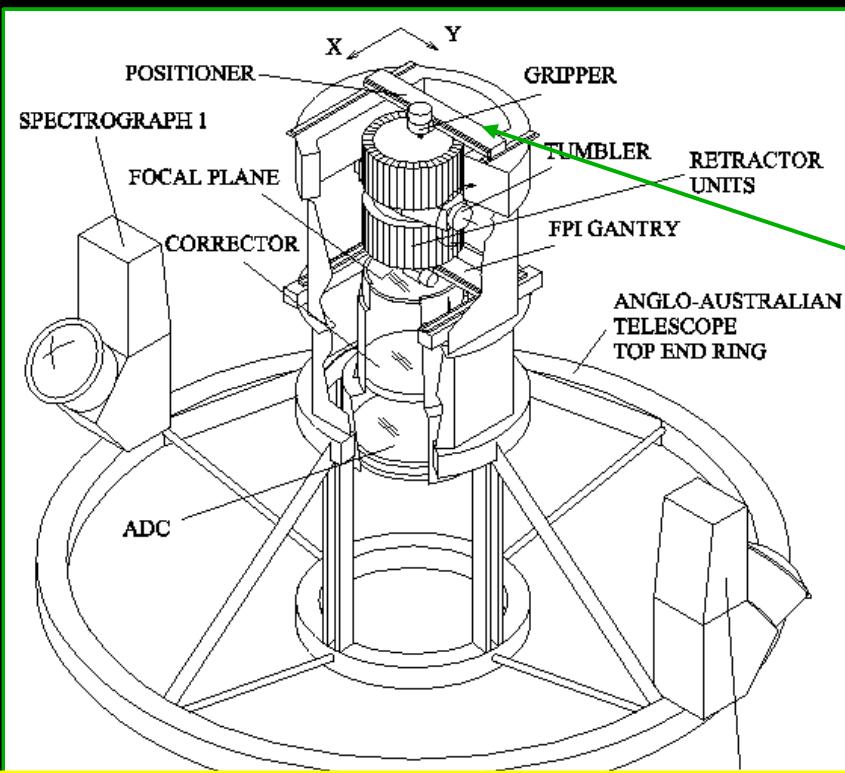
Vogt & Penrod -80s  
Zet Oph  
Ball VOGT

- Requires high SNR
  - ( $>300-500$ )
  - Perfect rotation coverage
  - Artefacts otherwise
  - NRP or solar spots
- Doppler Tomography
  - Accretion jets in Algols
  - Orbits in RV phase space

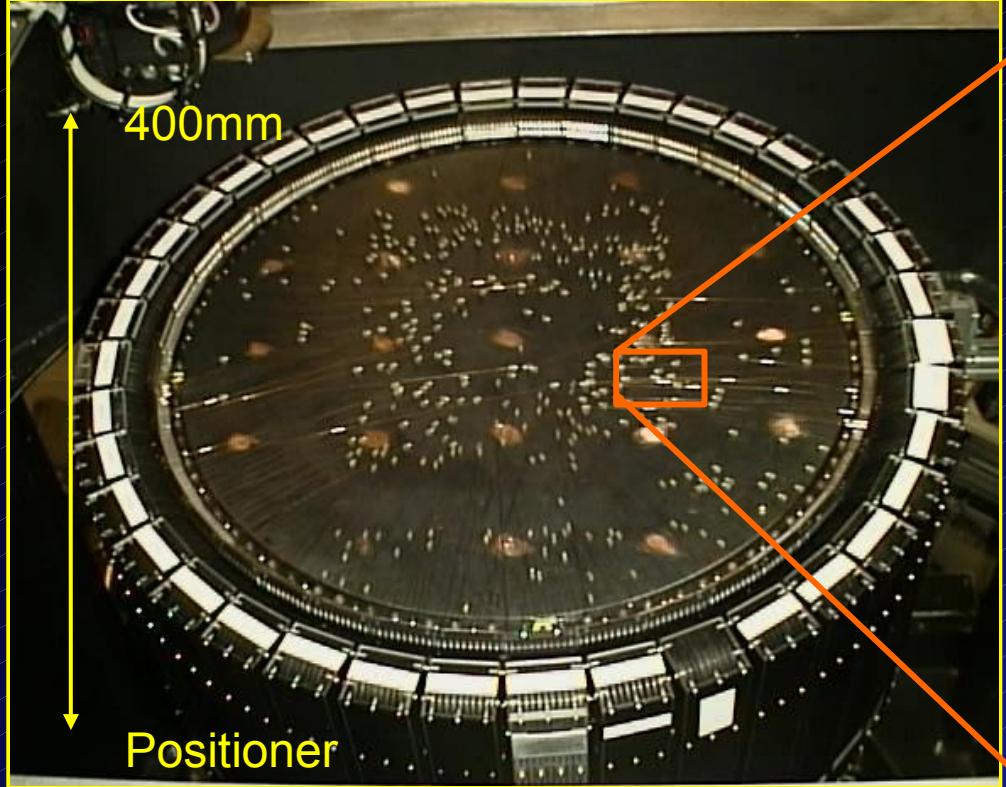
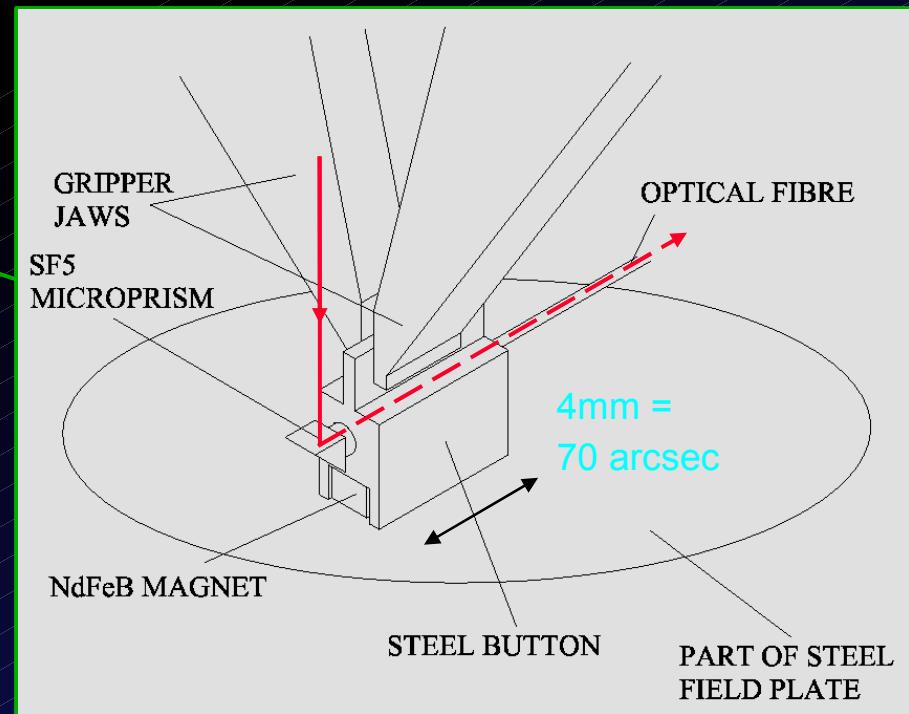


# Spectra Disentangling in Fourier Space - KOREL

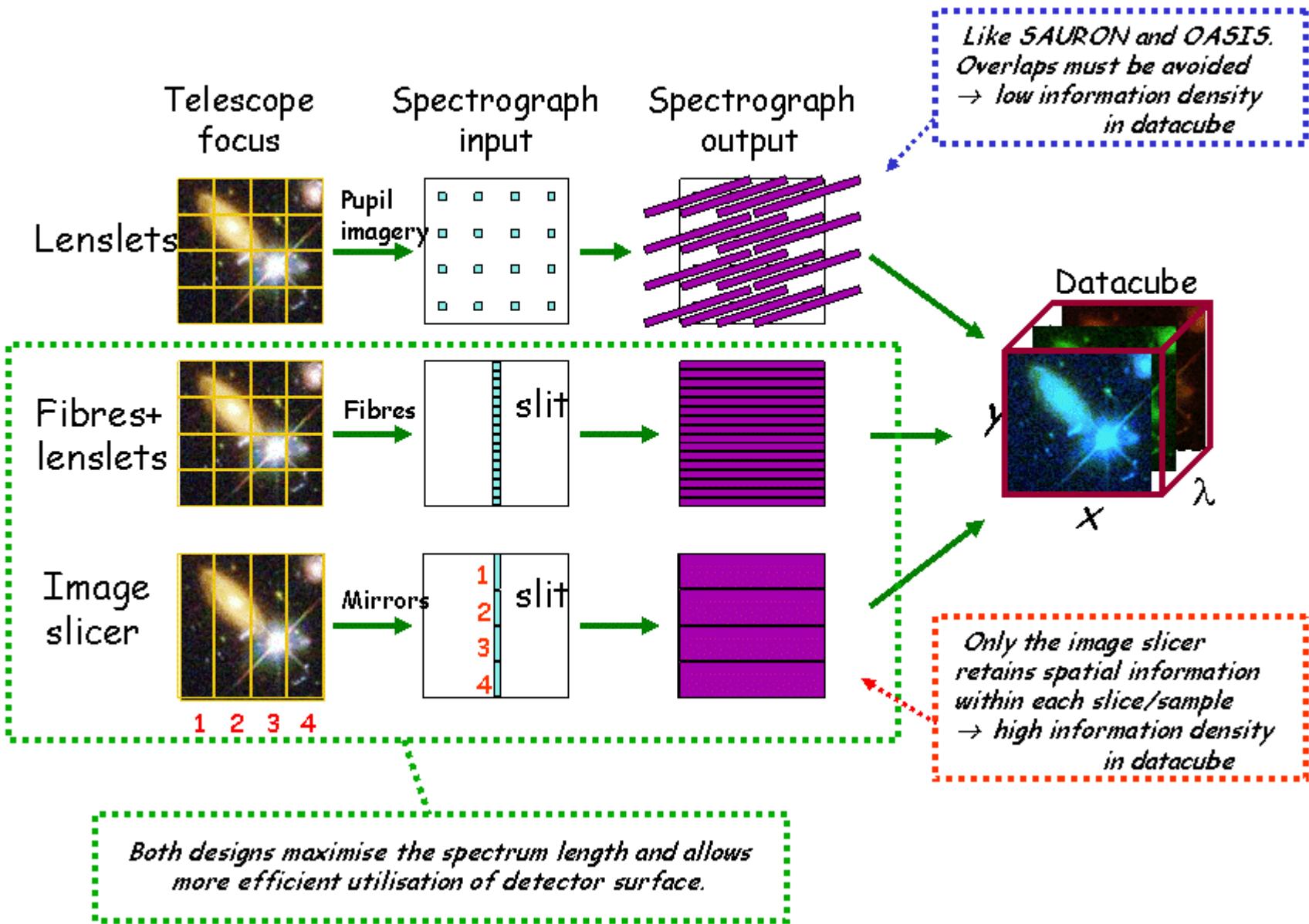




**2dF**

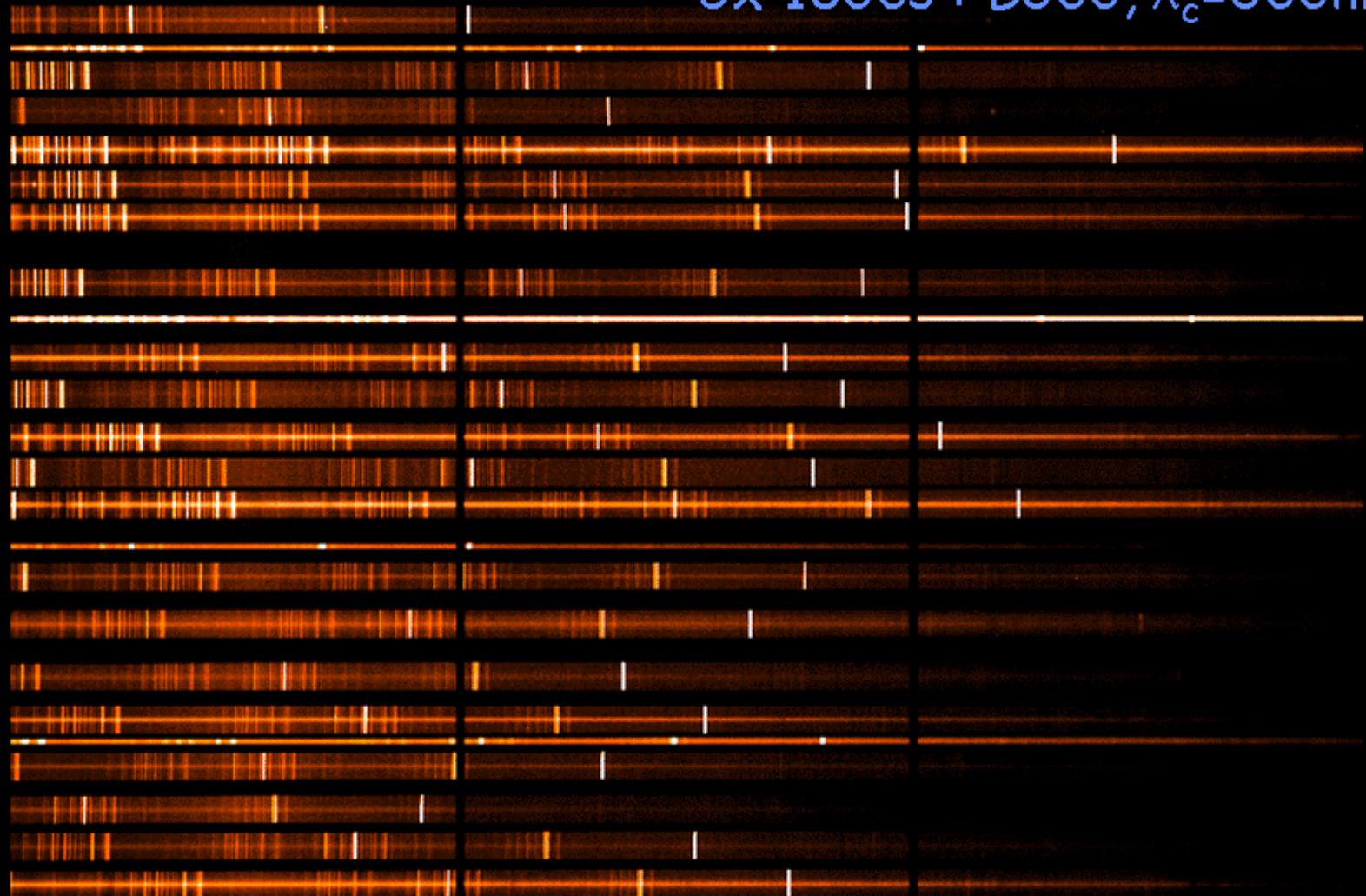


# Techniques of IFS



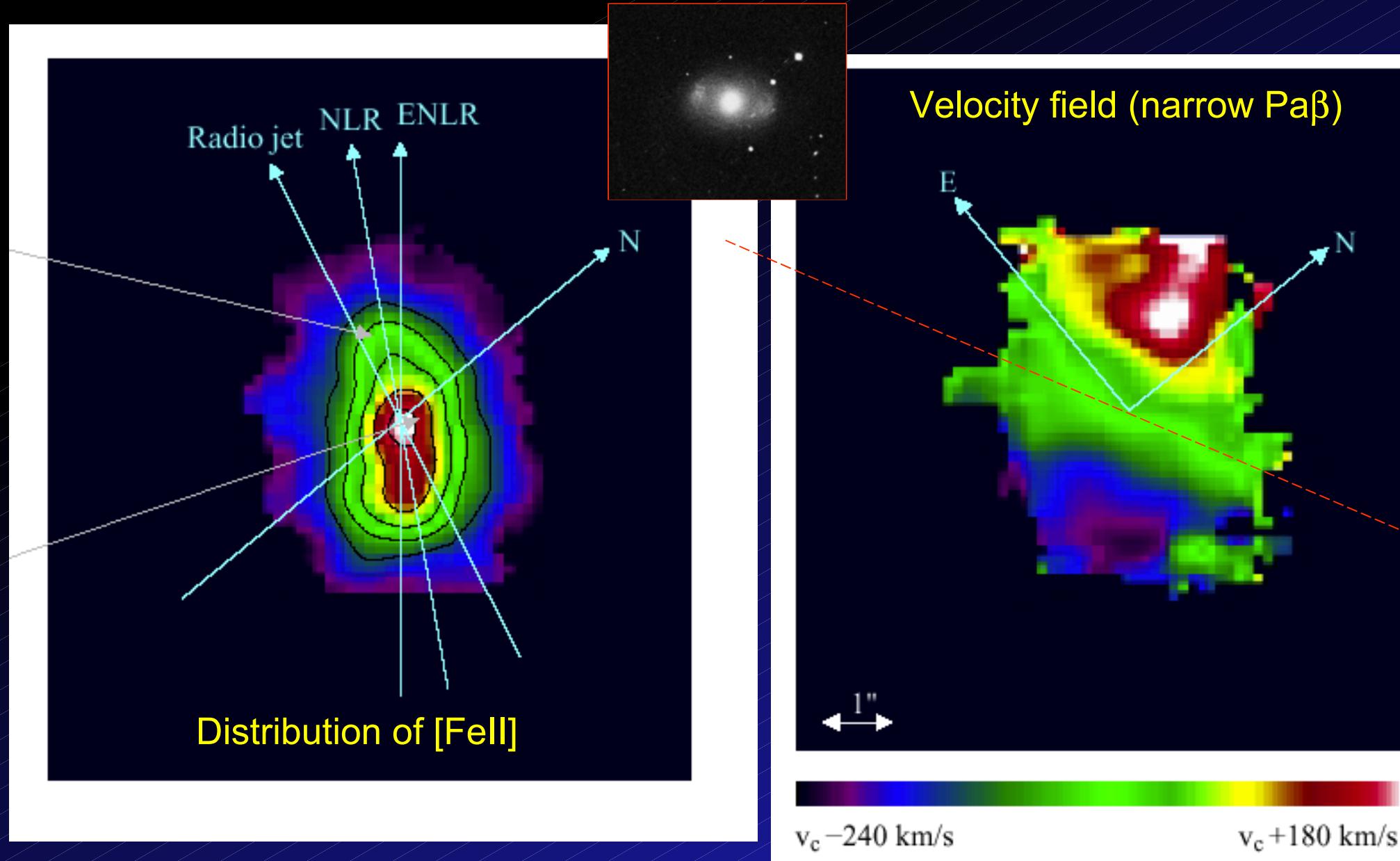
# GMOS multislit example

5x 1800s : B600,  $\lambda_c=600\text{nm}$



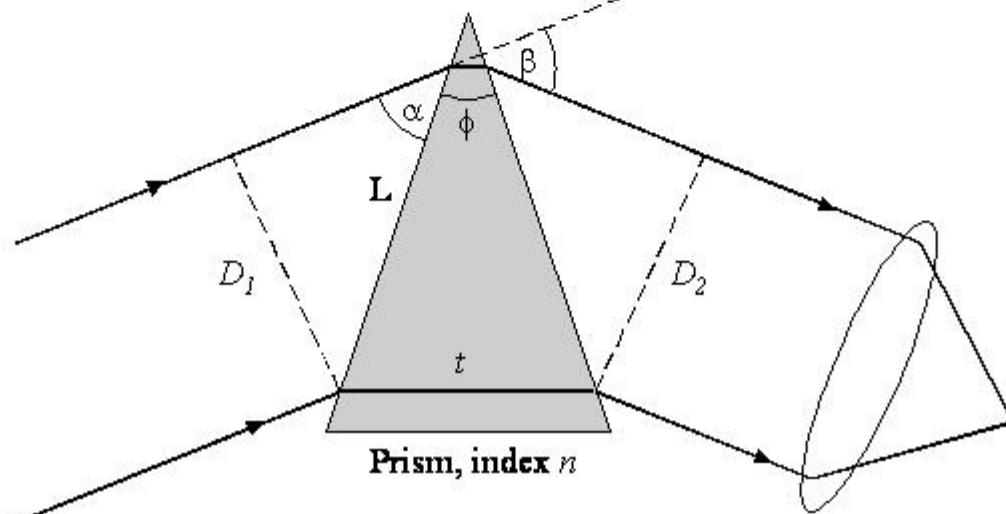
Note extra space required on detector to accommodate spectra

# Dissecting active galaxies



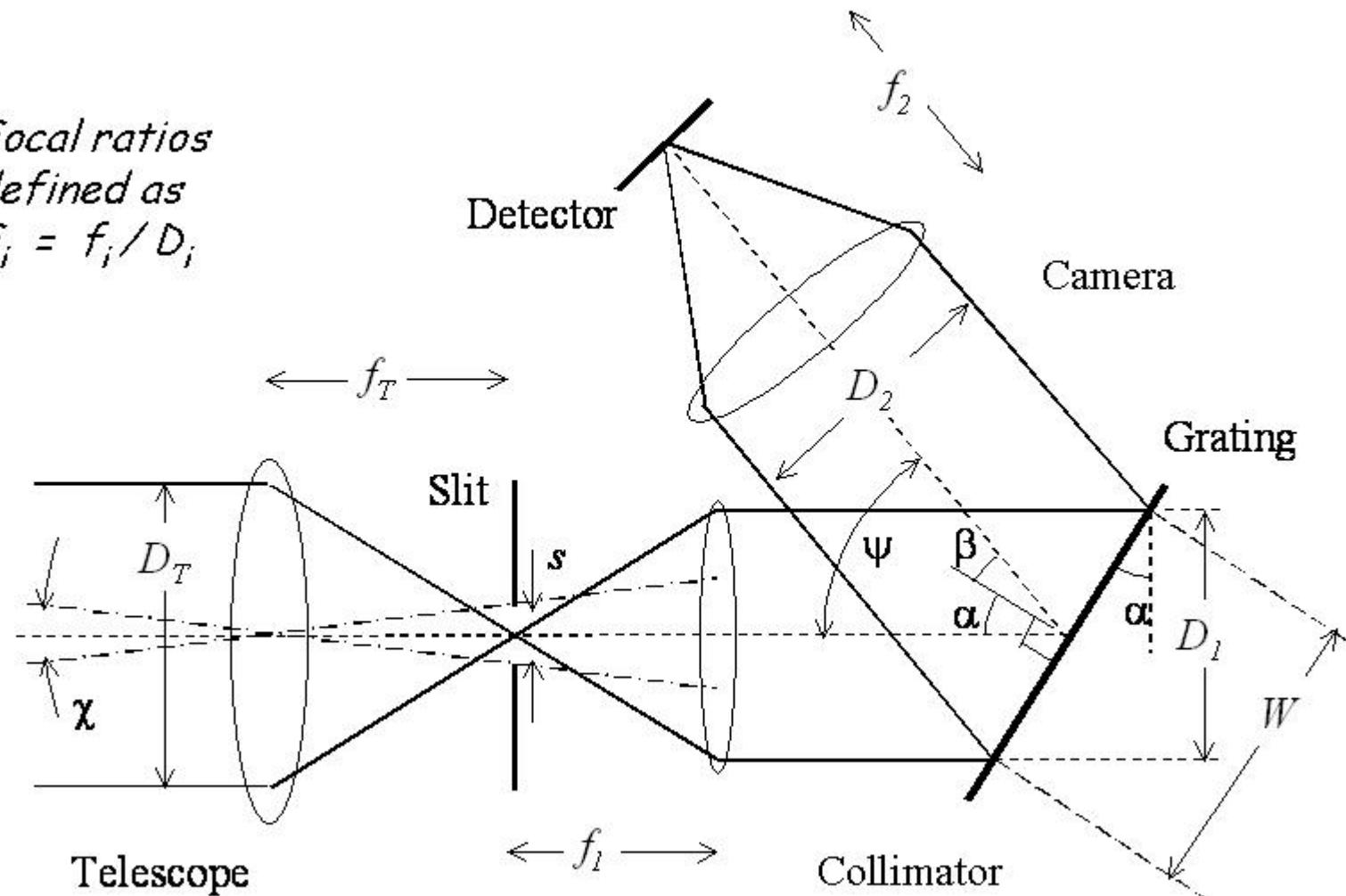
# Prisms

- Useful where only low resolving power is required
- Advantages:
  - simple - no rulings! (but glass must be of high quality)
  - multiple-order overlap not a problem - only one order!
- Disadvantages:
  - high resolving power not possible
  - resolving power/resolution can vary strongly with  $\lambda$

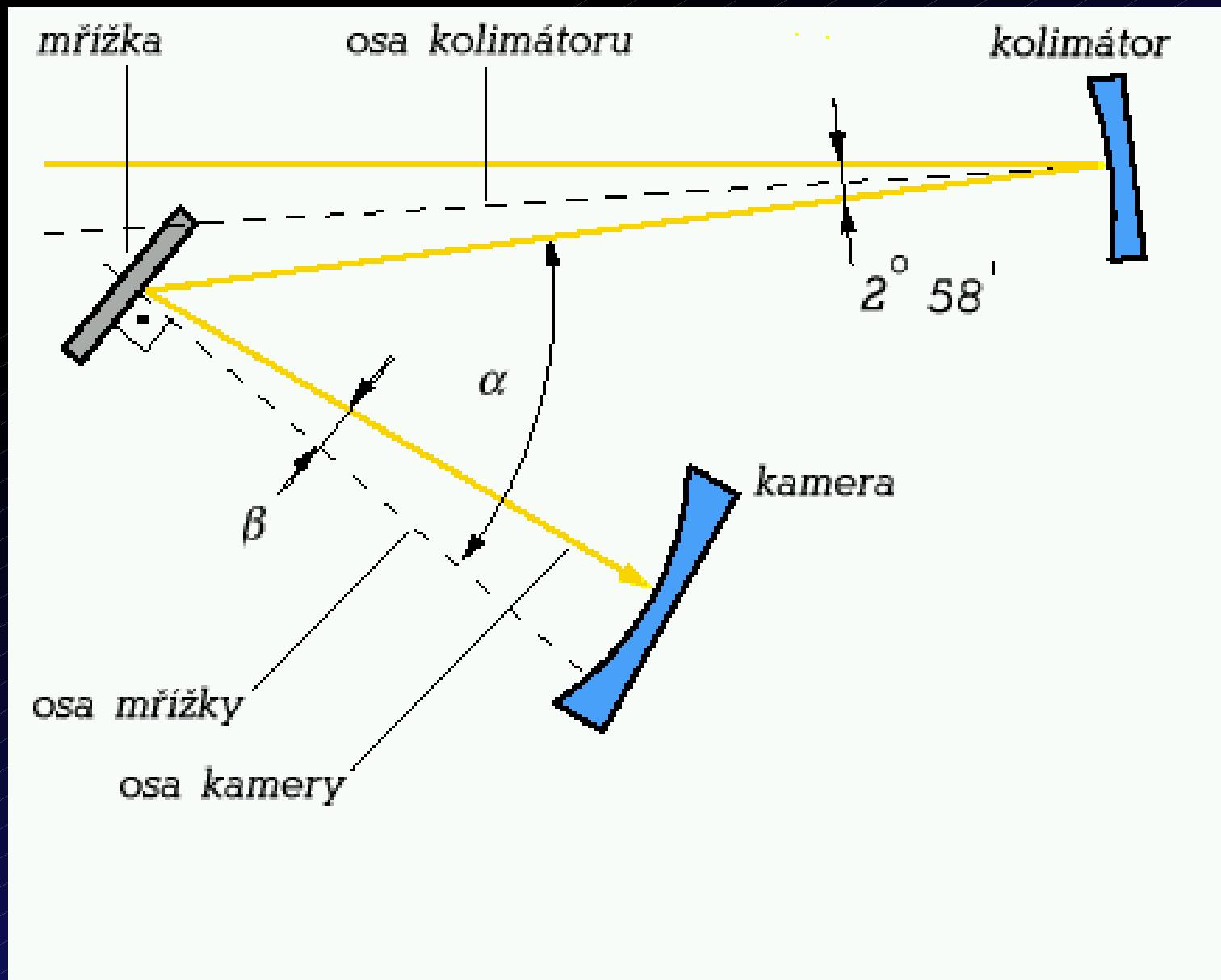


# Generic spectrograph layout

Focal ratios  
defined as  
 $F_i = f_i / D_i$



# Coudé spektrograf 2m v Ondřejově



# Grating equation

- Interference condition:

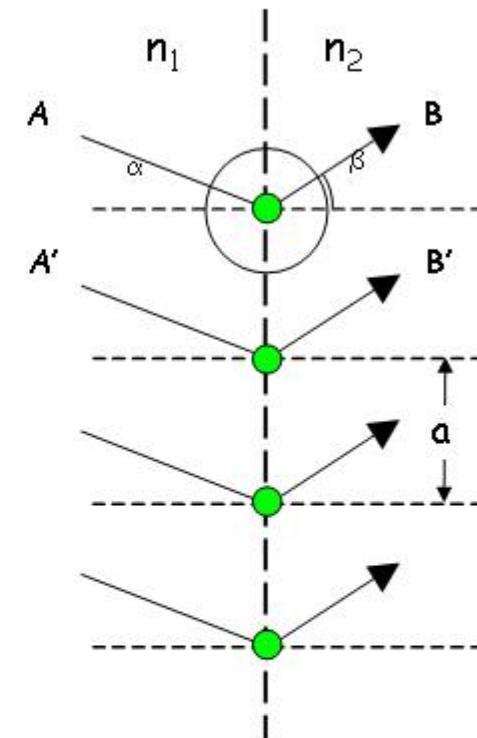
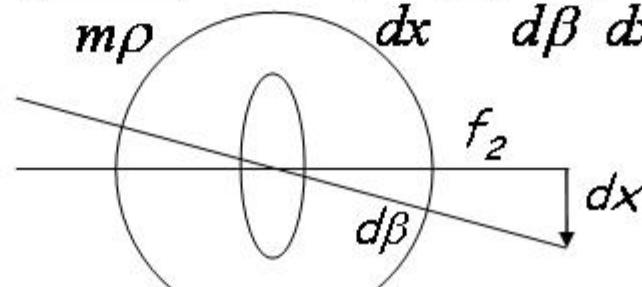
⇒ path difference between  $AB$  and  $A'B'$

- Grating equation:

$$m\rho\lambda = n_1 \sin \alpha + n_2 \sin \beta \quad \text{where} \quad \rho = \frac{1}{a}$$

- Dispersion:

$$\frac{d\lambda}{d\beta} = \frac{\cos \beta}{m\rho} \quad \frac{d\lambda}{dx} = \frac{d\lambda}{d\beta} \frac{d\beta}{dx} = \frac{\cos \beta}{m\rho f_2}$$



# "Spectral resolution"

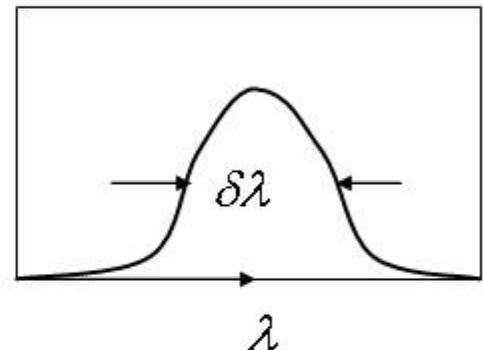
- Terminology (sometimes vague!)
  - Wavelength resolution  $\delta\lambda$
  - Resolving power  $R \propto \delta\lambda$
- Classically, *in the diffraction limit,*

Resolving power = total number of rulings  
x spectral order

I.e.  $R^* = m\rho W$

Total grating length

- But in most practical cases for astronomy ( $x < \lambda/D_T$ ), the resolving power is determined by the width of the slit, so  $R < R^*$



# Spectral resolution

- Spectral resolution:  $\delta\lambda = \left(\frac{d\lambda}{dx}\right)s' = \frac{\cos \beta}{m\rho f_2} s'$

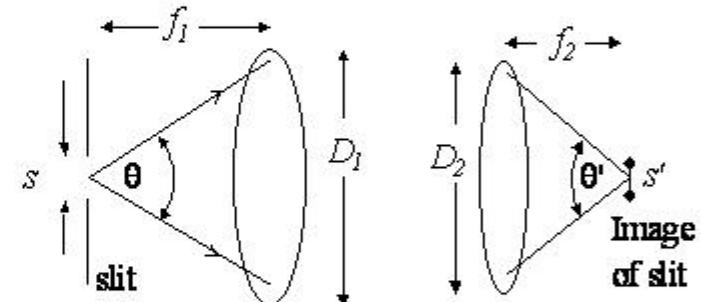
Image of slit  
on detector

- Projected slit width:

Conservation of *Etendue* ( $nA\Omega$ )

□

$$\square \Rightarrow \theta s = \theta' s' \Rightarrow s' = s \frac{\theta}{\theta'} = s \frac{F_2}{F_1}$$



$$\Rightarrow \delta\lambda = \left(\frac{d\lambda}{dx}\right)s' = \frac{\cos \beta}{m\rho f_2} s \frac{F_2}{F_1} = \frac{s D_1 \cos \beta}{m\rho D_2 f_1}$$

Camera focal  
length

# Resolving power

- Illuminated grating length:  $W = \frac{D_2}{\cos \beta}$

- Spectral resolution (width)

$$\delta\lambda = \frac{s}{m\rho F_1 W}$$

Collimator  
focal ratio

- Resolving power:

- expressed in laboratory terms

$$R \equiv \frac{\lambda}{\delta\lambda} = \frac{m\rho\lambda F_1 W}{s}$$

Physical  
slitwidth

- expressed in astronomical terms

$$R = \frac{m\rho\lambda W}{\chi D_T}$$

Grating  
length

since  $s = \chi f_T$  and  $\frac{f_T}{D_T} = \frac{f_1}{D_1} = F_T = F_1$

Angular  
slitwidth

Telescope  
size

*Size of spectrograph must scale with telescope size*

# Importance of slit width

- Width of slit determines:
  - Resolving power ( $R$ ) since  $R\chi = \text{constant}$
  - Throughput ( $\eta$ )
- Hence there is always a tradeoff between *throughput* and *spectral information*
- Function  $\eta(\chi)$  depends on *Point Spread Function (PSF)* and profile of extended source
  - generally  $\eta(\chi)$  increases slower than  $\chi^{+1}$  whereas  $R \propto \chi^{-1}$  so  $\eta R$  maximised at small  $\chi$
- Signal/noise also depends on slit width
  - throughput ( $\rightarrow$  signal)
  - wider slit admits more sky background ( $\rightarrow$  noise)

# Blazing

- Diffracted intensity:

Interference pattern

Single slit diffraction

$$I = \left( \frac{\sin^2 N\phi}{\sin^2 \phi} \right) \left( \frac{\sin^2 \theta}{\theta^2} \right)$$

$\Phi$  = phase difference between adjacent rulings

$\theta$  = phase difference from centre of one ruling to its edge

→ Shift envelope peak to  $m=1$

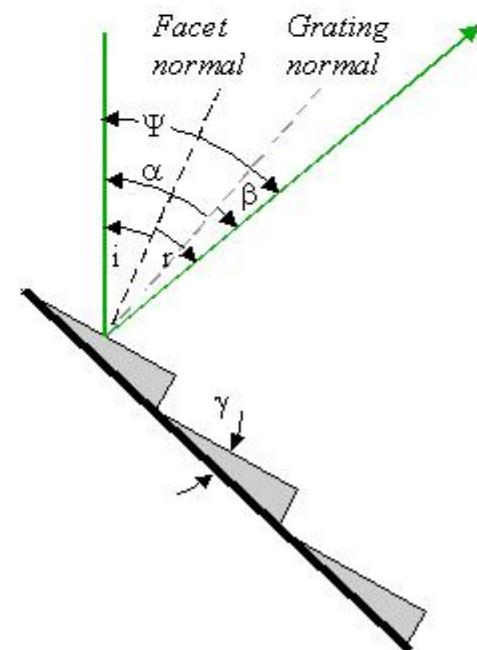
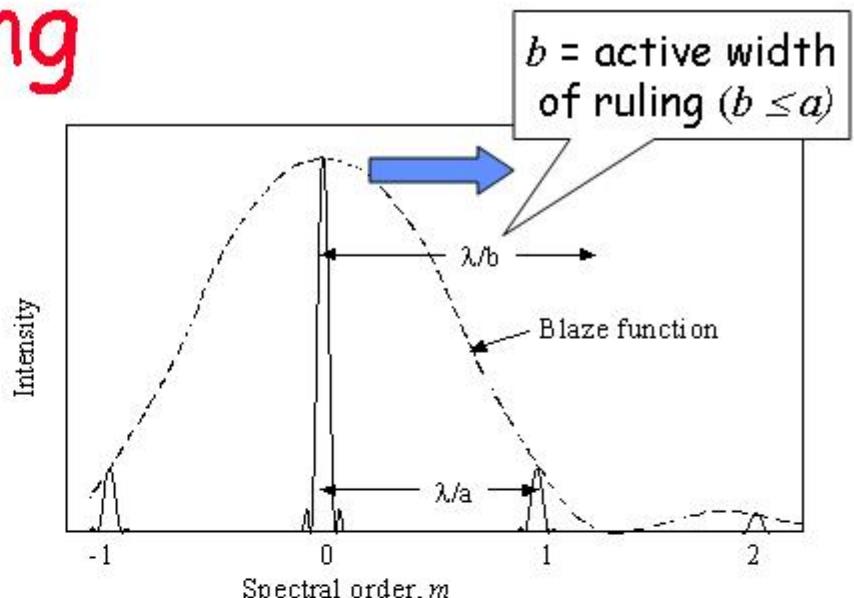
- Blaze condition

specular reflection off grooves:

$$\alpha + \beta = 2\gamma \text{ also } \Psi = \alpha - \beta$$

$$\Rightarrow \rho m \lambda_B = \sin \alpha + \sin \beta = 2 \sin \gamma \cos \frac{\Psi}{2}$$

$$\sin x + \sin y = 2 \sin \frac{x+y}{2} \cos \frac{x-y}{2}$$



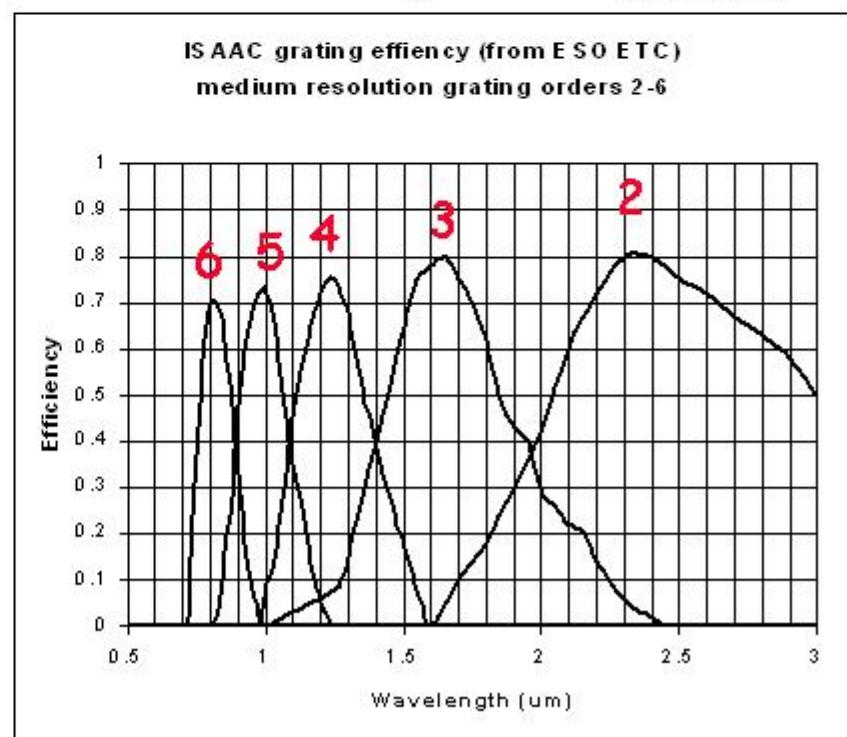
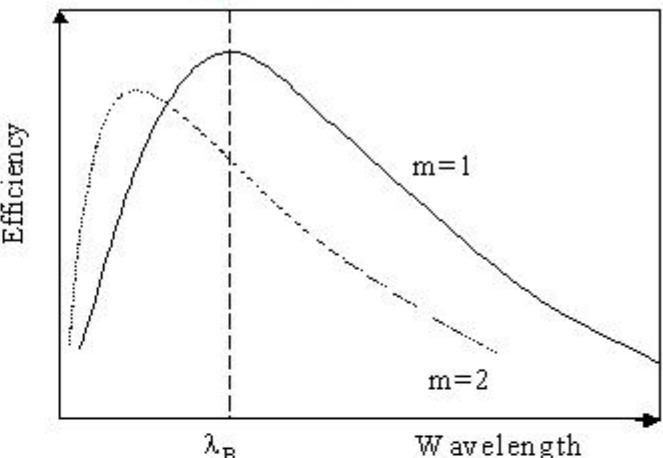
# Efficiency vs wavelength

- Approximation valid for  $a > \lambda$
- $\lambda_{max}(m) = \lambda_B(m=1)/m$
- Rule-of-thumb:  
40.5% x peak at

$$\lambda_+ = \frac{2m\lambda_B}{2m-1} \text{ and } \lambda_- = \frac{2m\lambda_B}{2m+1}$$

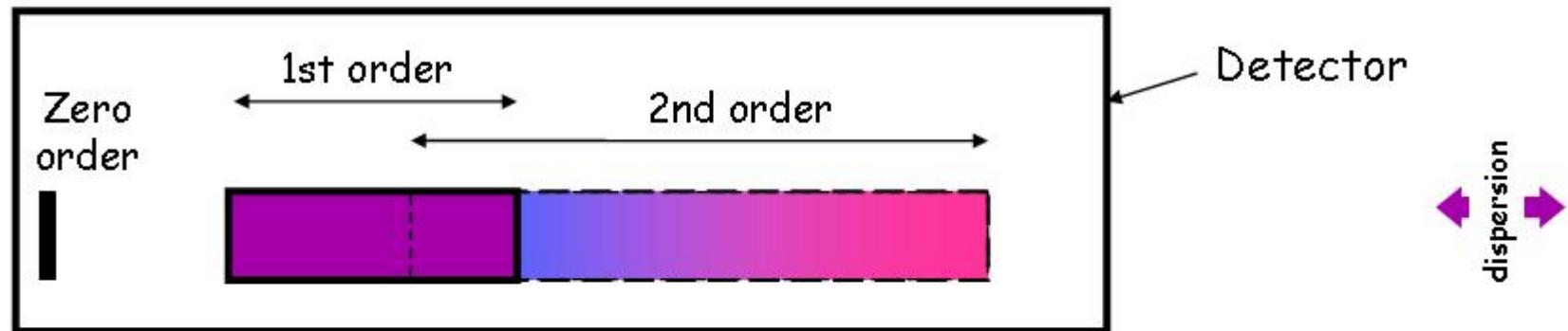
$$\Rightarrow \lambda_+ - \lambda_- \approx \frac{\lambda_B}{m} \quad (\text{large } m)$$

- Sum over all orders  $< 1$ 
  - reduction in efficiency with increasing order



(See: Schroeder, *Astronomical Optics*)

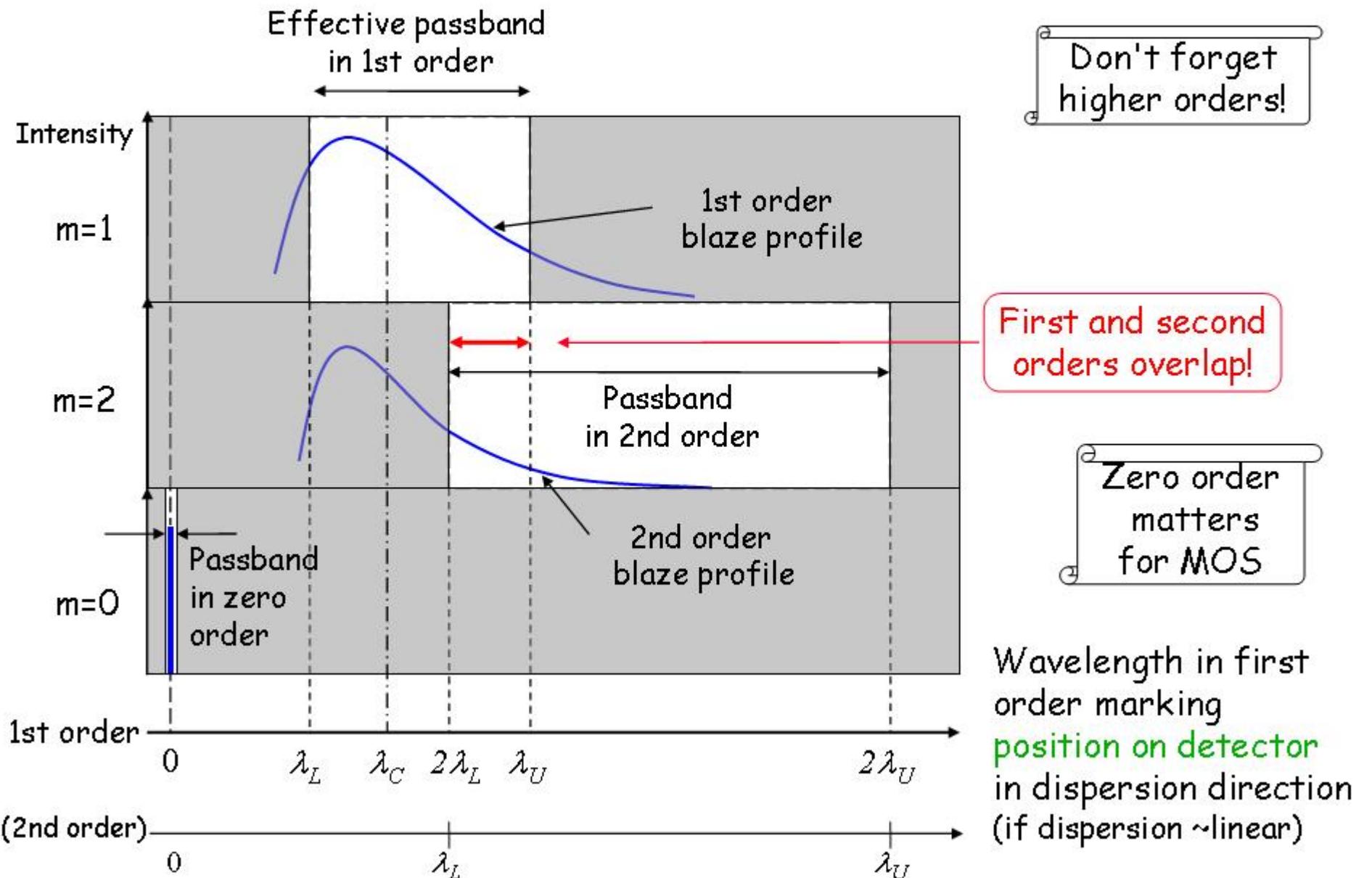
# Order overlaps



To eliminate overlap between 1st and 2nd order

- Limit wavelength range incident on detector using *passband filter* or *longpass* ("order rejection") filter acting with long-wavelength cutoff of optics or detector (e.g. 1100nm for CCD)
- Optimum wavelength range is 1 octave (then  $2\lambda_L = \lambda_U$ )
- *Zero order may be a problem in multiobject spectroscopy*

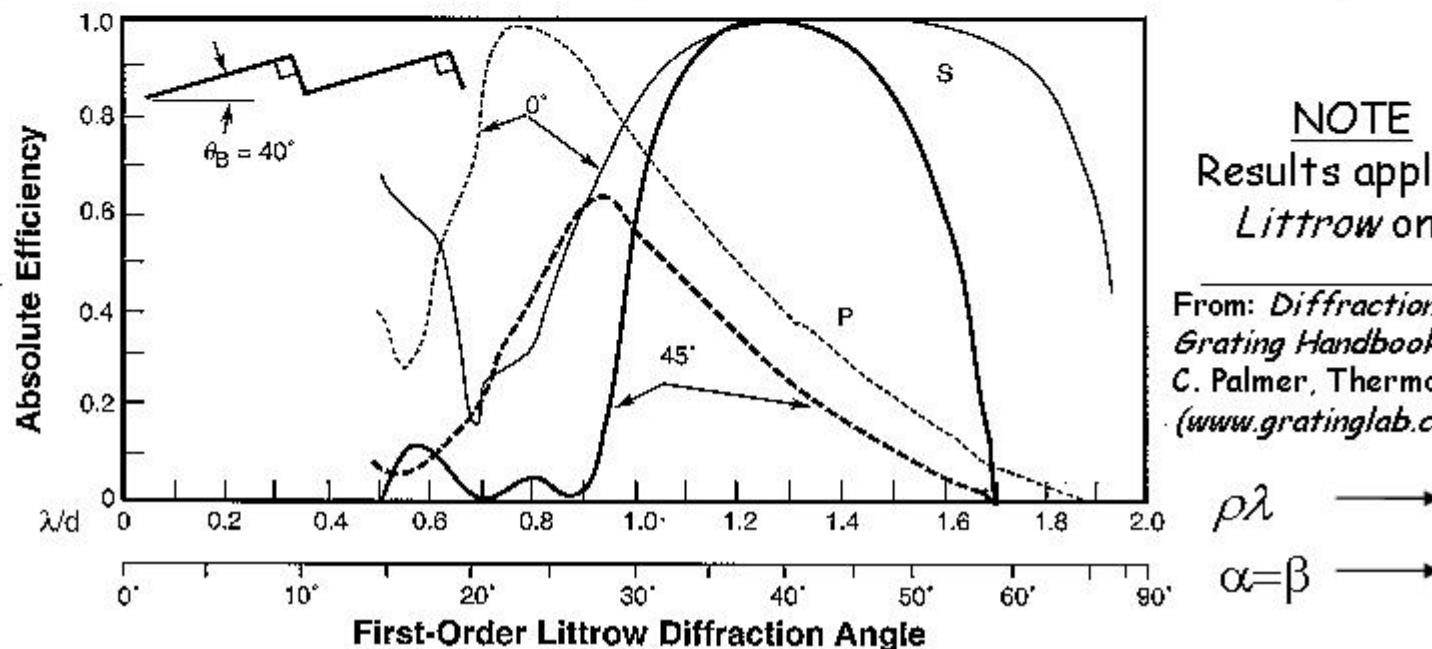
# Order overlaps



# Efficiency - semi-empirical (contd)

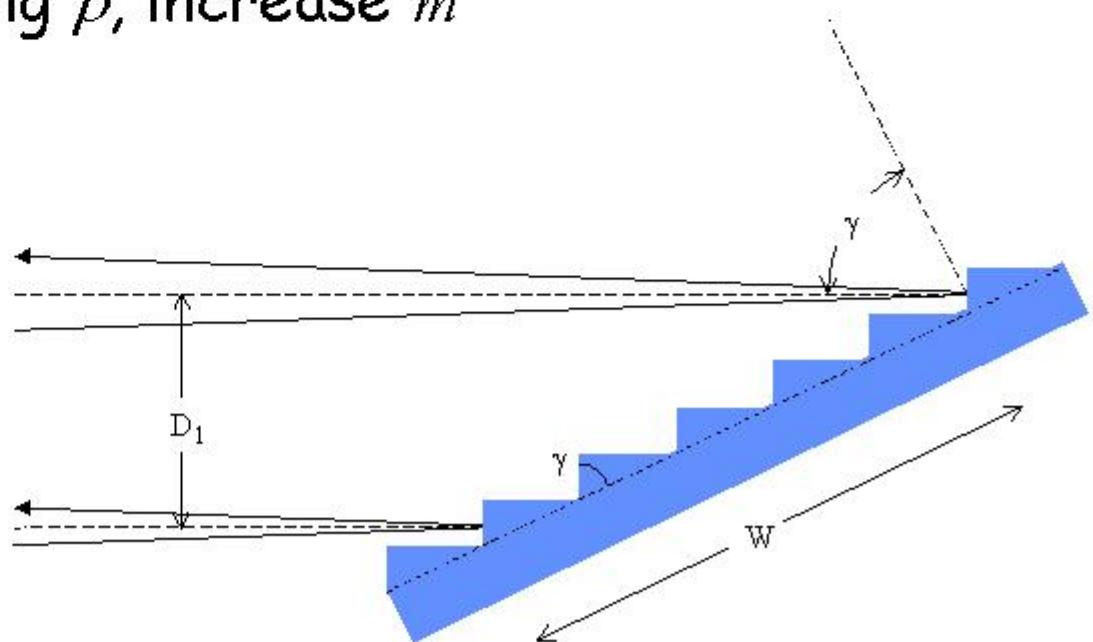
Different regimes for blazed (triangular) grooves

- |                          |  |
|--------------------------|--|
| $\gamma < 5^\circ$       | obeys scalar theory, little polarisation effect ( $P \approx S$ )                    |
| $5 < \gamma < 10^\circ$  | $S$ anomaly at $\rho\lambda \approx 2/3$ , $P$ peaks at lower $\rho\lambda$ than $S$ |
| $10 < \gamma < 18^\circ$ | various $S$ anomalies  |
| $18 < \gamma < 22^\circ$ | anomalies suppressed, $S \gg P$ at large $\rho\lambda$                               |
| $22 < \gamma < 38^\circ$ | strong $S$ anomaly at $P$ peak, $S$ constant at large $\rho\lambda$                  |
| $\gamma > 38^\circ$      | $S$ and $P$ peaks very different, efficient in Littrow only                          |



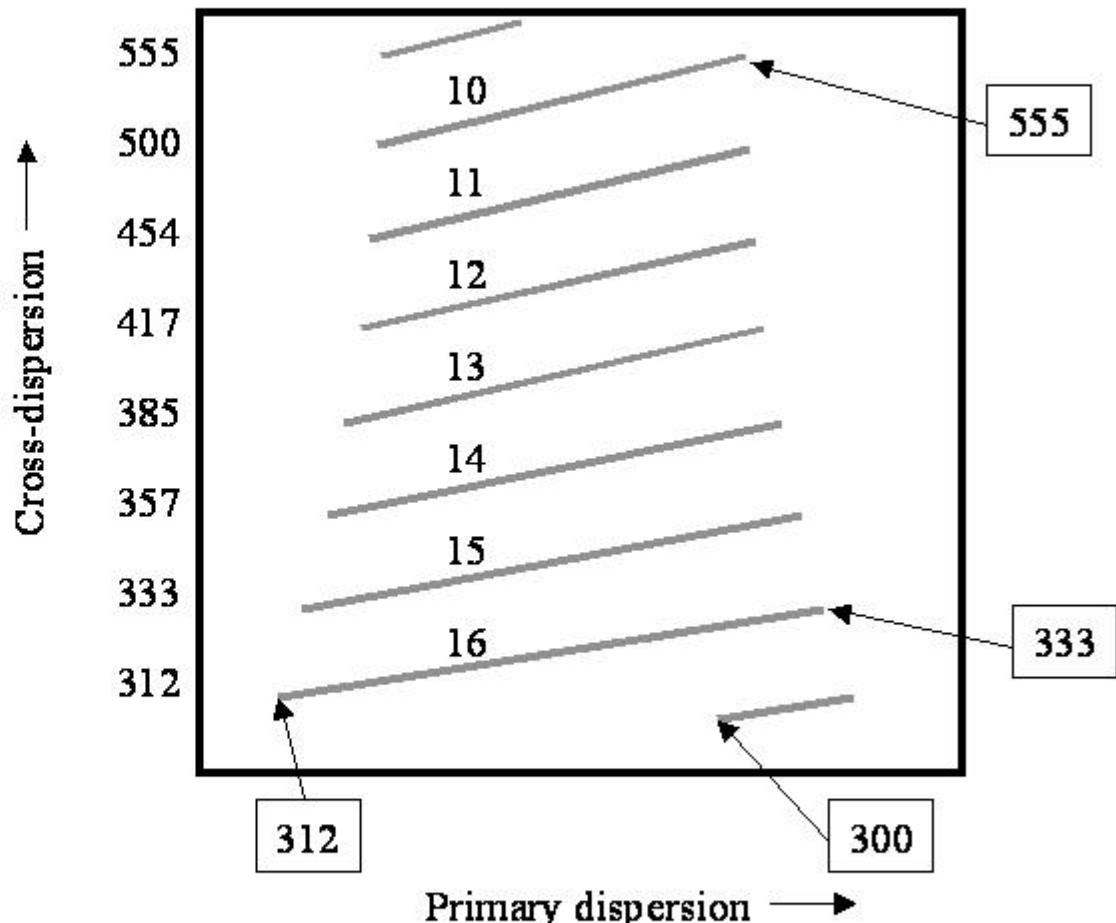
# Echelle gratings

- Obtain very high  $R (> 10^5)$  using very long grating
- In Littrow:  $R = \frac{m\rho\lambda W}{\chi D_T} = \frac{2D_1}{\chi D_T} \tan \gamma$  Groove angle
- Maximising  $\gamma$  requires large  $m\rho$  since  $m\rho\lambda = 2\sin\gamma$
- Instead of increasing  $\rho$ , increase  $m$
- *Echelle* is a coarse grating with large groove angle
- R parameter =  $\tan \gamma$  (e.g  $R2 \Rightarrow \gamma = 63.5^\circ$ )

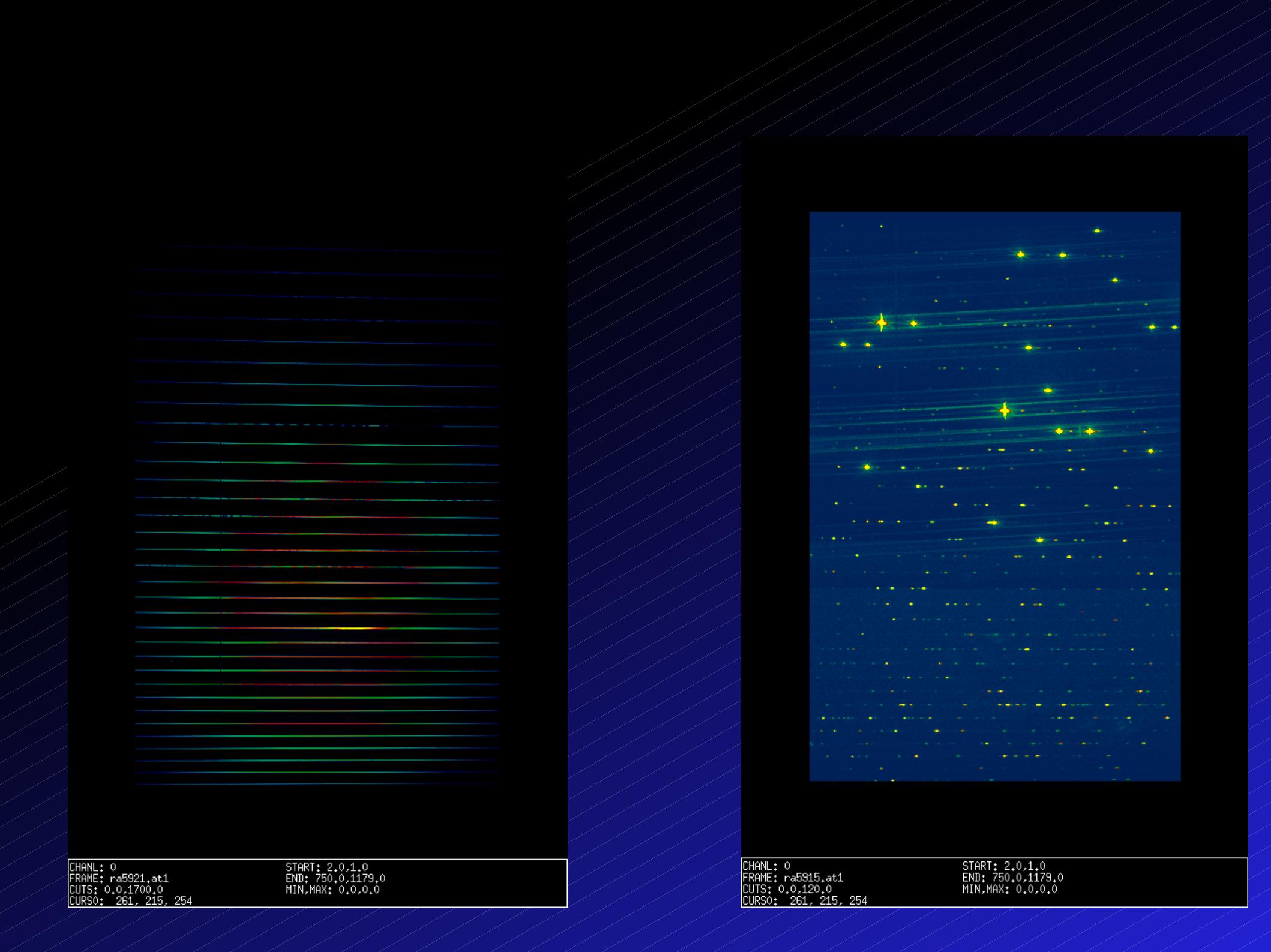


# Multiple orders

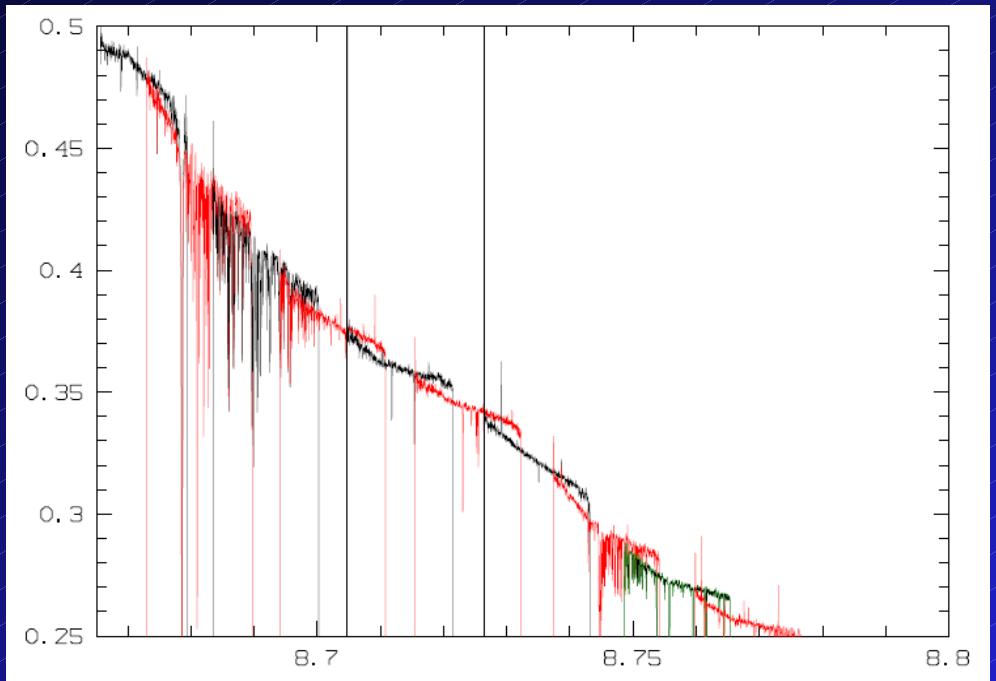
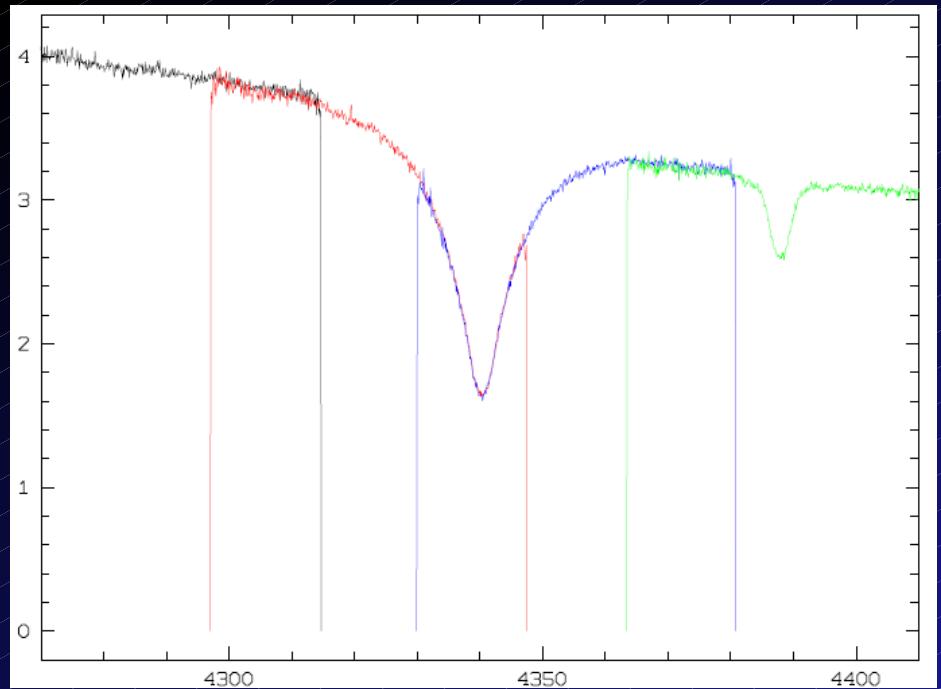
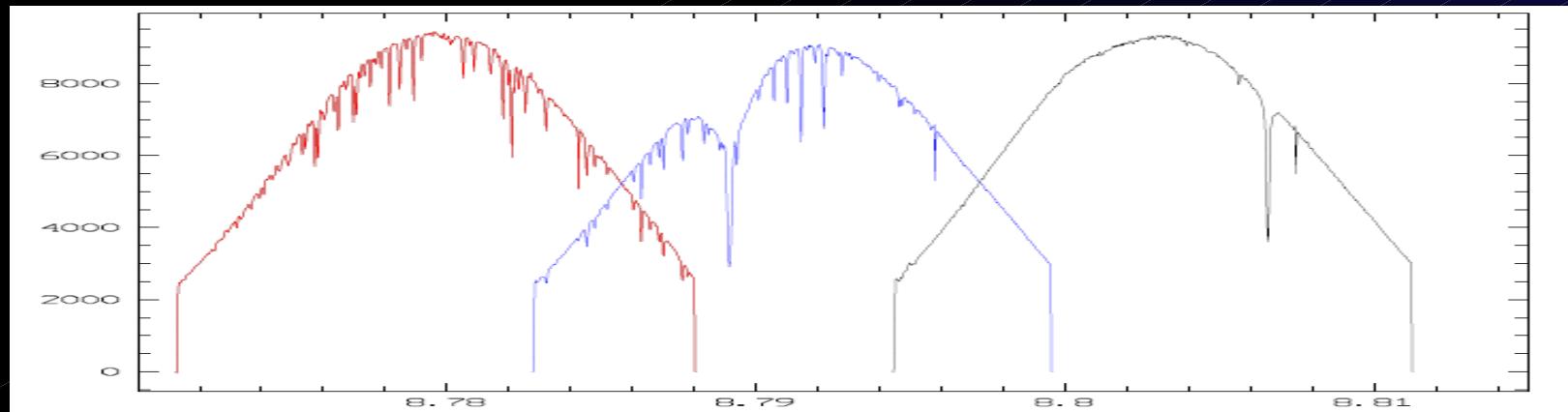
- Many orders to cover desired  $\lambda\lambda$ :  
*Free spectral range*  
 $\Delta\lambda = \lambda/m$
- Orders lie on top of each other:  
 $\lambda(m) = \lambda(n) \times (n/m)$
- Solution:
  - use narrow passband filter to isolate one order at a time
  - cross-disperse to fill detector with many orders at once



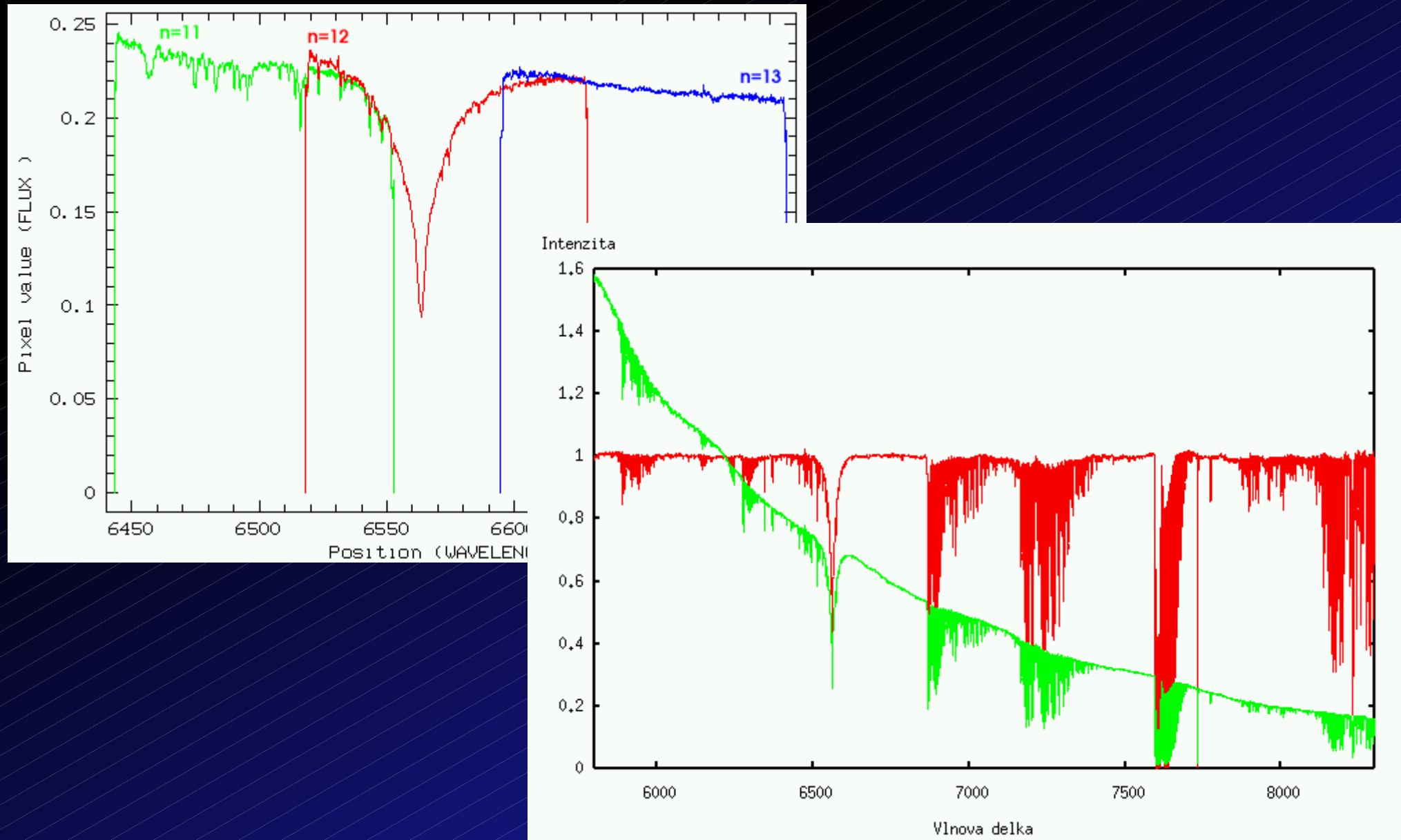
Cross dispersion may use prisms or low dispersion grating



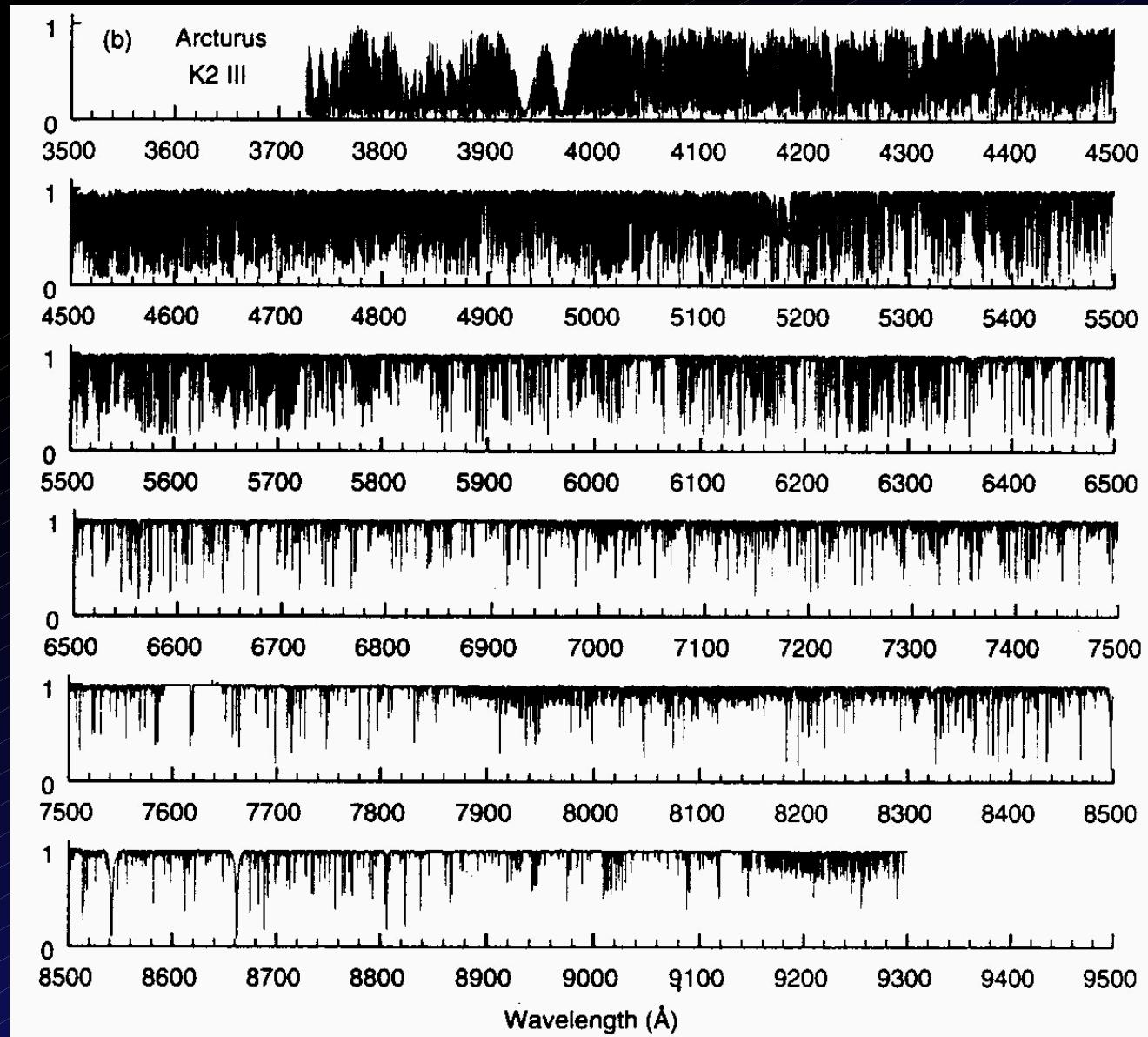
# Echelle Spectra Problems



# Echelle – spojování řádů



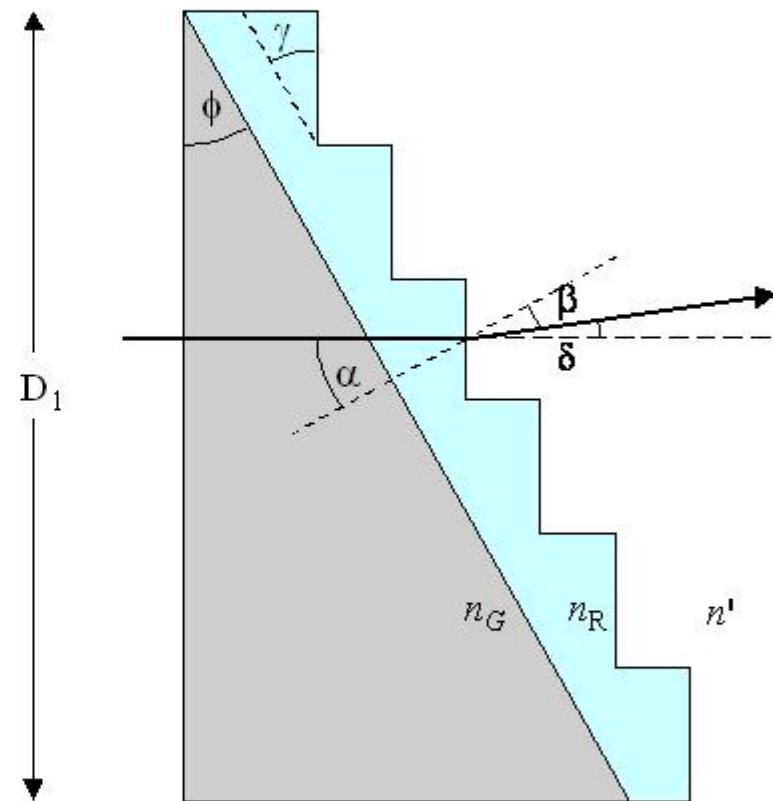
# Merged Echelle



Arcturus: Hinkle et al.

# Grisms

- Transmission grating attached to prism
- Allows in-line optical train:
  - simpler to engineer
  - quasi-Littrow configuration - no variable anamorphism
- Inefficient for  $\rho > 600/\text{mm}$  due to groove shadowing and other effects

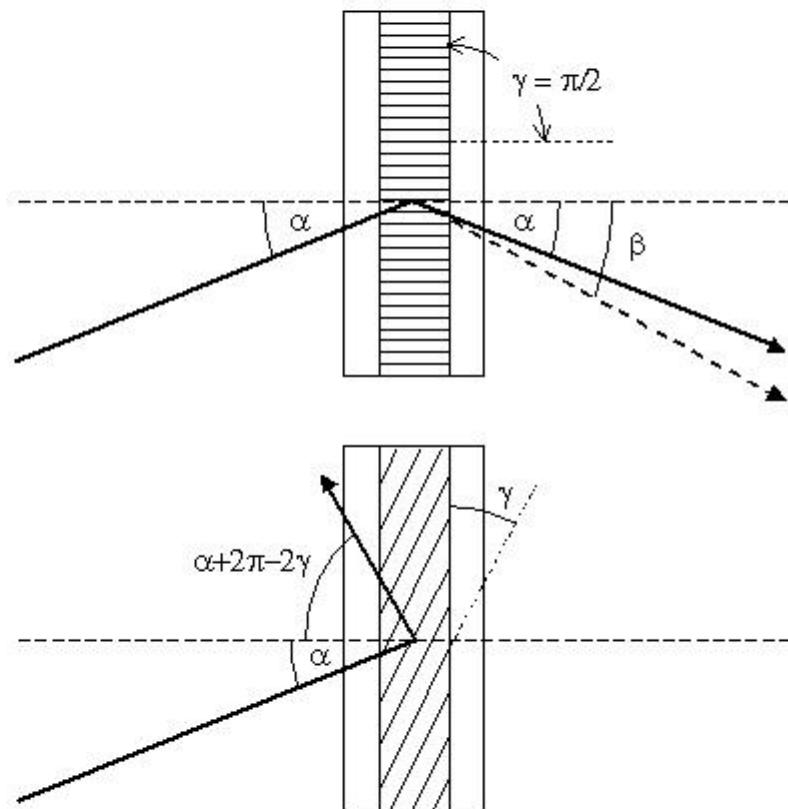


# Volume Phase Holographic gratings

- So far we have considered *surface relief* gratings
- An alternative is *VPH* in which refractive index varies harmonically throughout the body of the grating:  $n_g(x, z) = n_g + \Delta n_g \cos[2\pi\rho_g(x \sin \gamma + z \cos \gamma)]$
- Don't confuse with '*holographic*' gratings (SR)
- Advantages:
  - Higher peak efficiency than SR
  - Possibility of very large size with high  $\rho$
  - Blaze condition can be altered (*tuned*)
  - Encapsulation in flat glass makes more robust
- Disadvantages
  - Tuning of blaze requires *bendable spectrograph!*
  - Issues of wavefront errors and cryogenic use

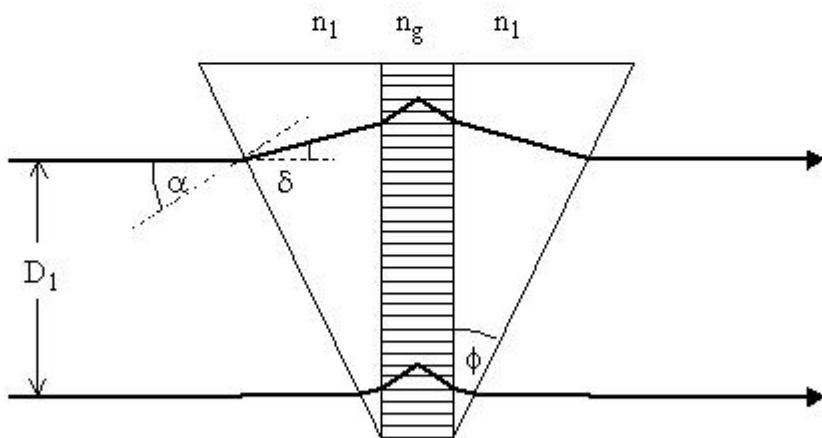
# VPH configurations

- *Fringes* = planes of constant  $n$
- Body of grating made from *Dichromated Gelatine (DCG)* which permanently adopts fringe pattern generated holographically
- Fringe orientation allows operation in transmission or reflection



# VPH 'grism' = vrism

- Remove bent geometry, allow in-line optical layout
- Use prisms to bend input and output beams while generating required Bragg condition



$$R = \frac{m\rho\lambda W}{\chi D_T} = \frac{m\rho\lambda}{\chi D_T} D_1 (1 + \tan \delta \tan \phi)$$

$$\delta = \phi - \arcsin\left(\frac{\sin \phi}{n_1}\right)$$

# Limits to resolving power

- Resolving power can increase as  $m$ ,  $\rho$  and  $W$  increase for a given wavelength, slit and telescope

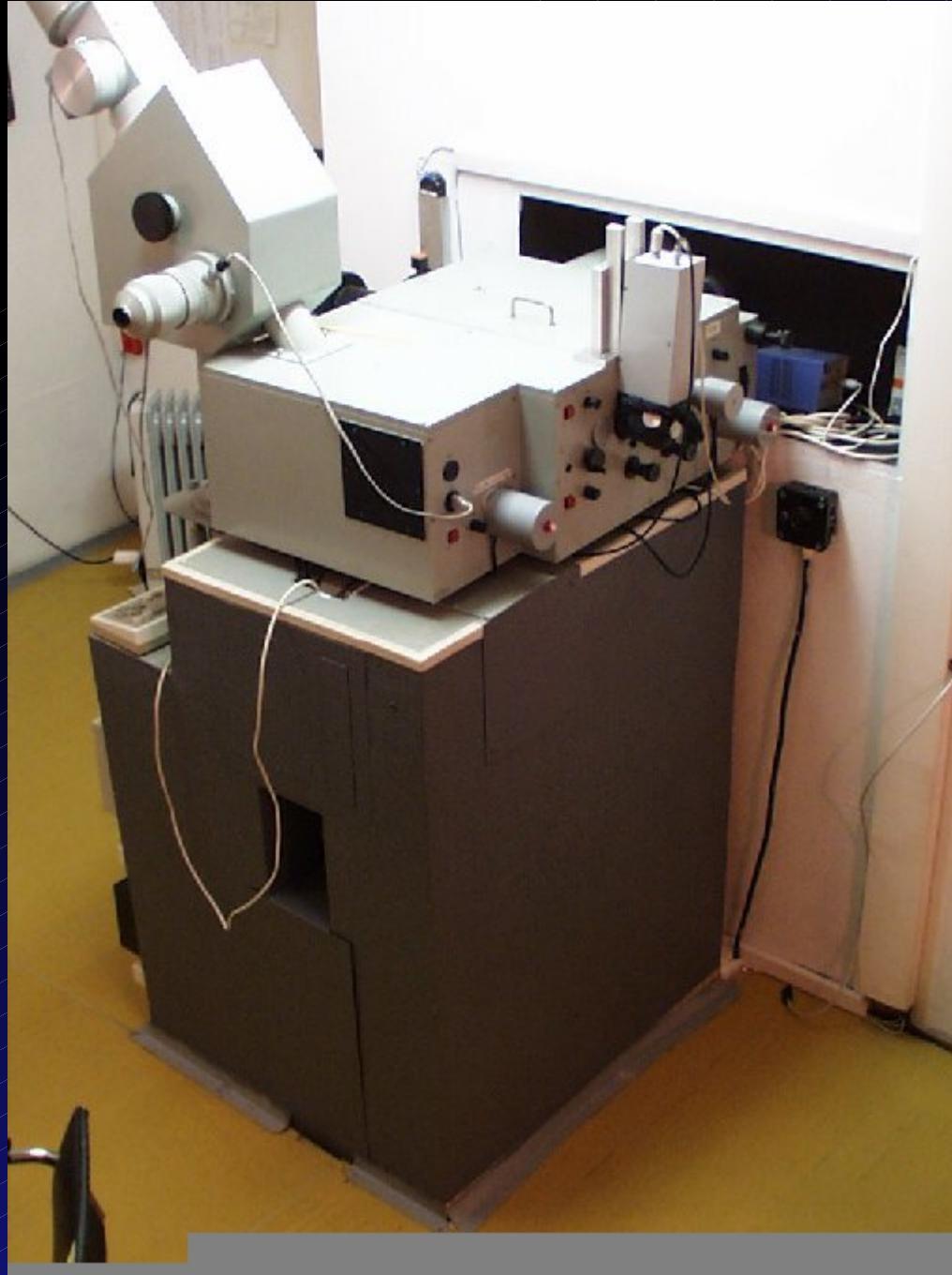
Grating  
parameters

$$R = \frac{m\rho\lambda W}{\chi D_T} = \frac{D_1}{\chi D_T} \left( \frac{\sin \alpha + \sin \beta}{\cos \beta} \right)$$

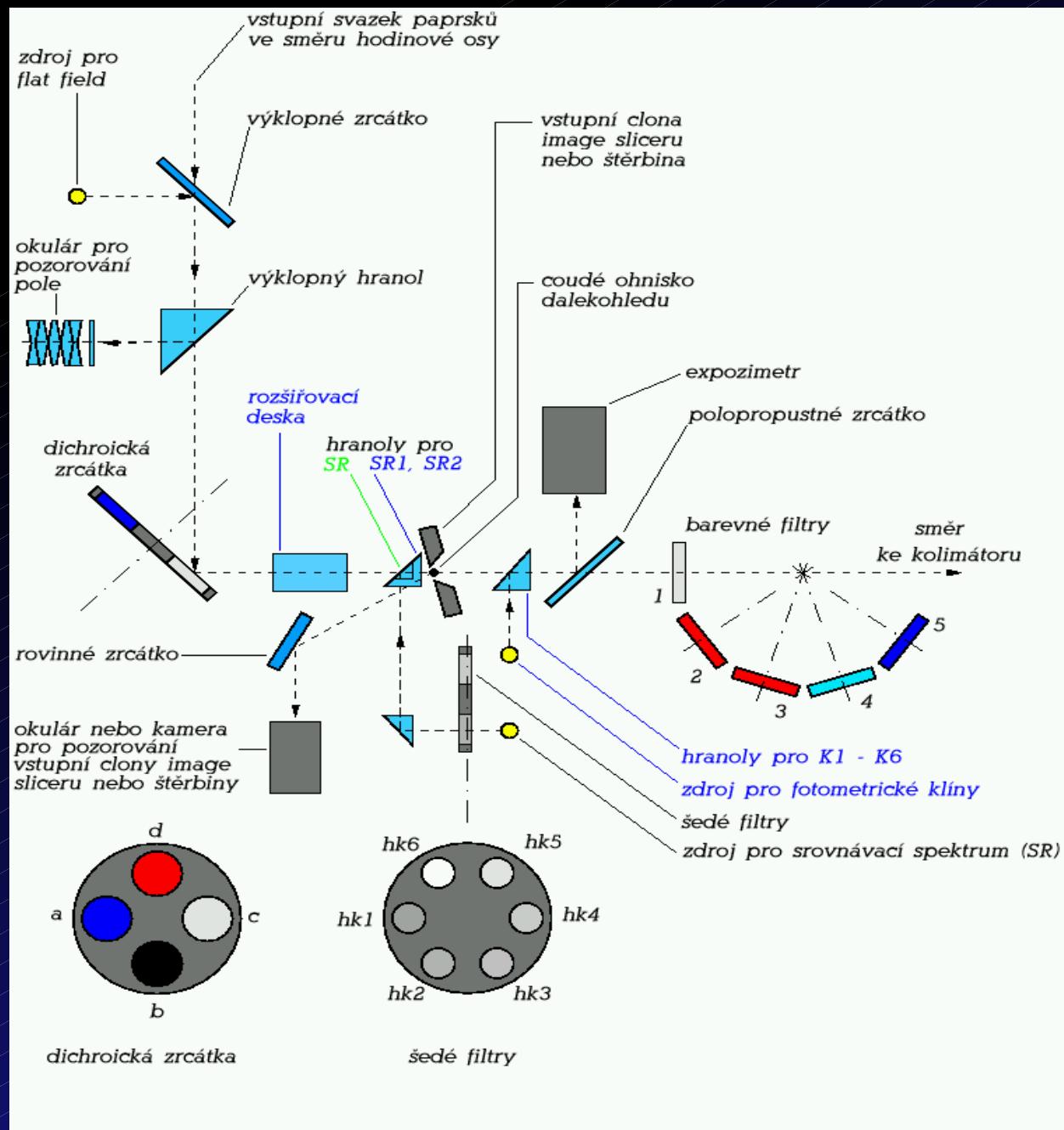
Geometrical  
factors

- Limit depends on geometrical factors only - increasing  $\rho$  or  $m$  will not help!
- In practice, the limit is when the output beam overfills the camera:
  - $W$  is actually the length of the intersection between beam and grating plane - not the actual grating length
  - $R$  will increase even if grating overfilled until diffraction-limited regime is entered ( $\lambda > \chi D_T$ )

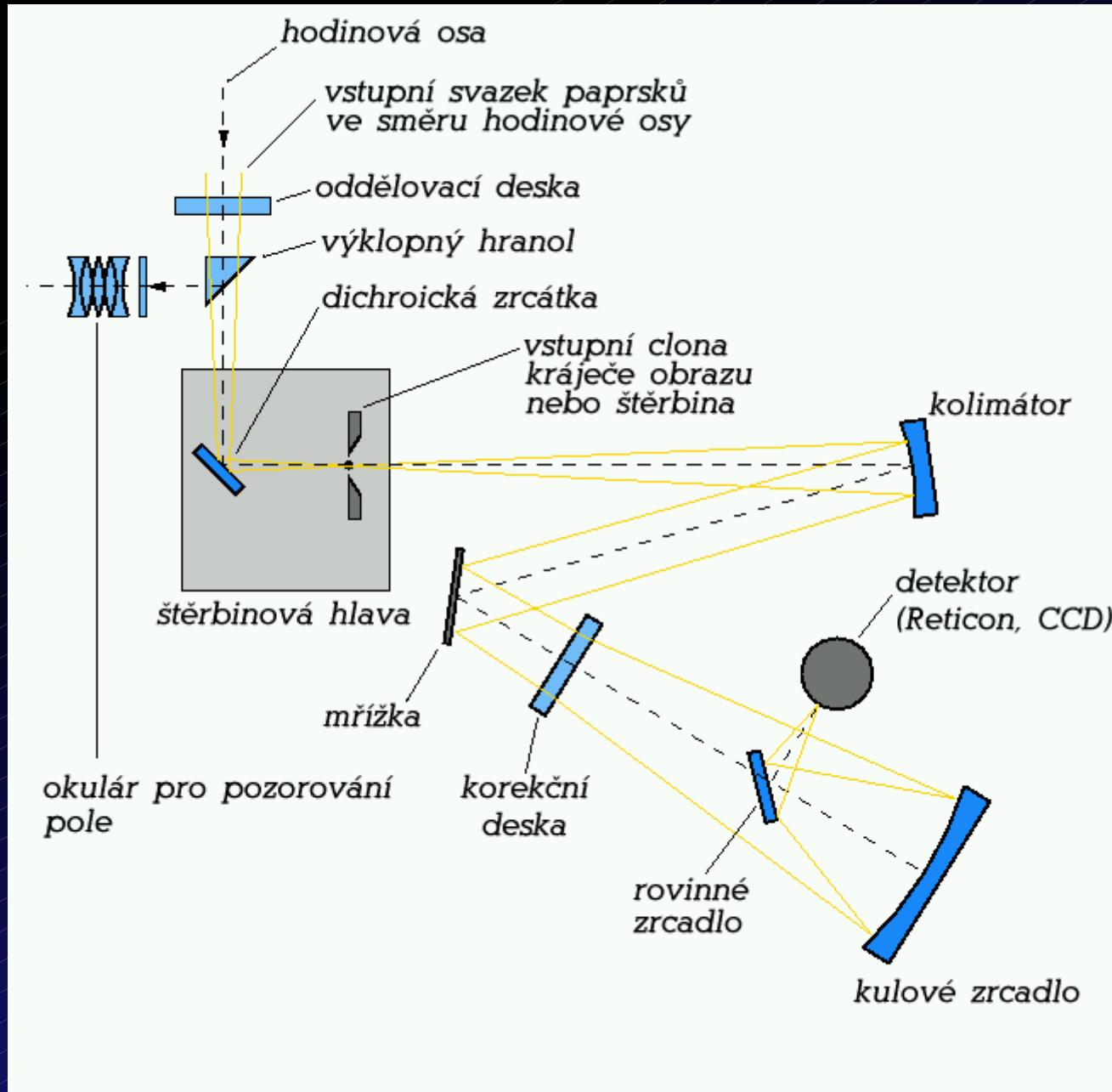
# 2m coudé

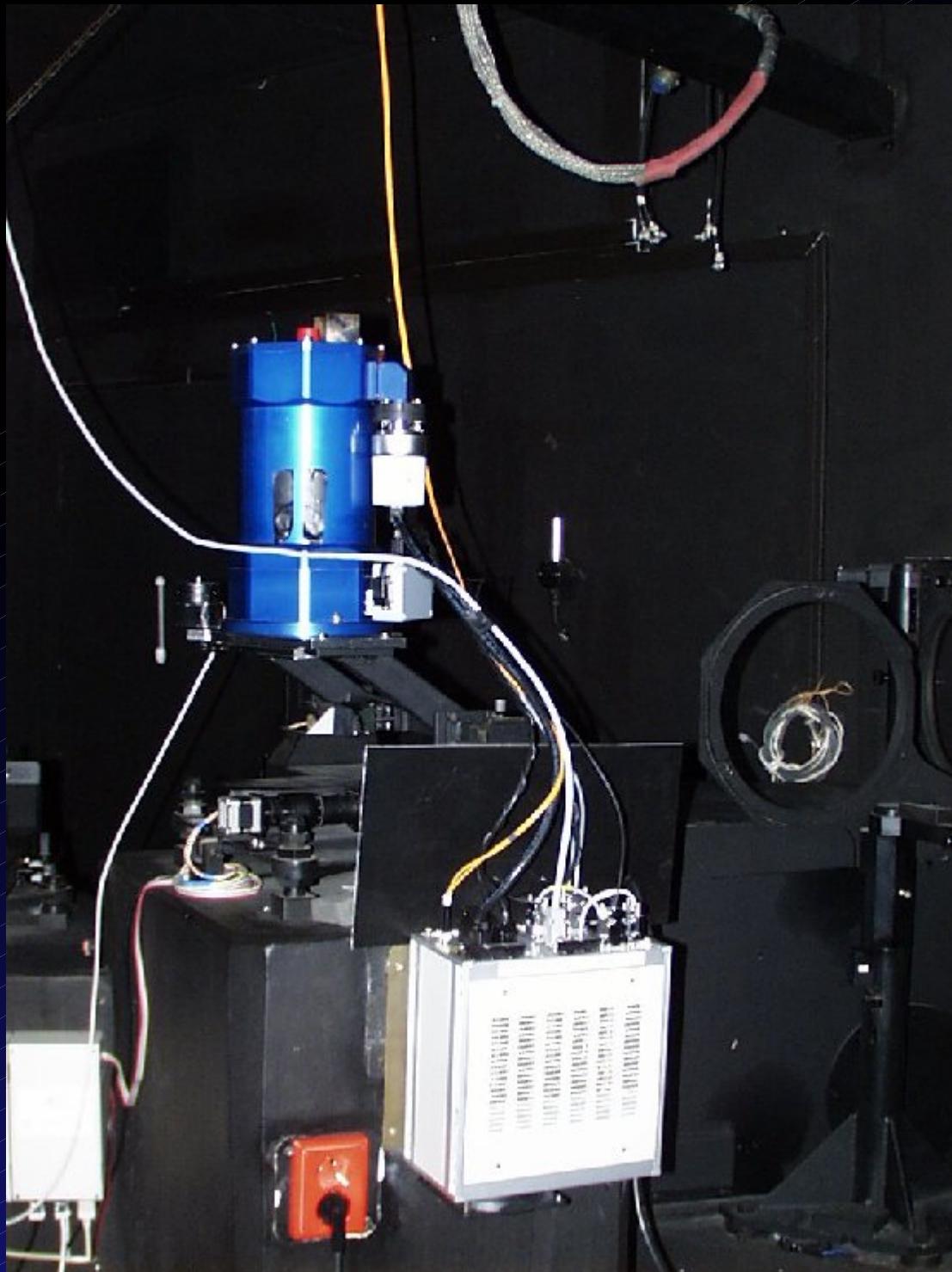


# Štěrbinová hlava spektrografu 2m

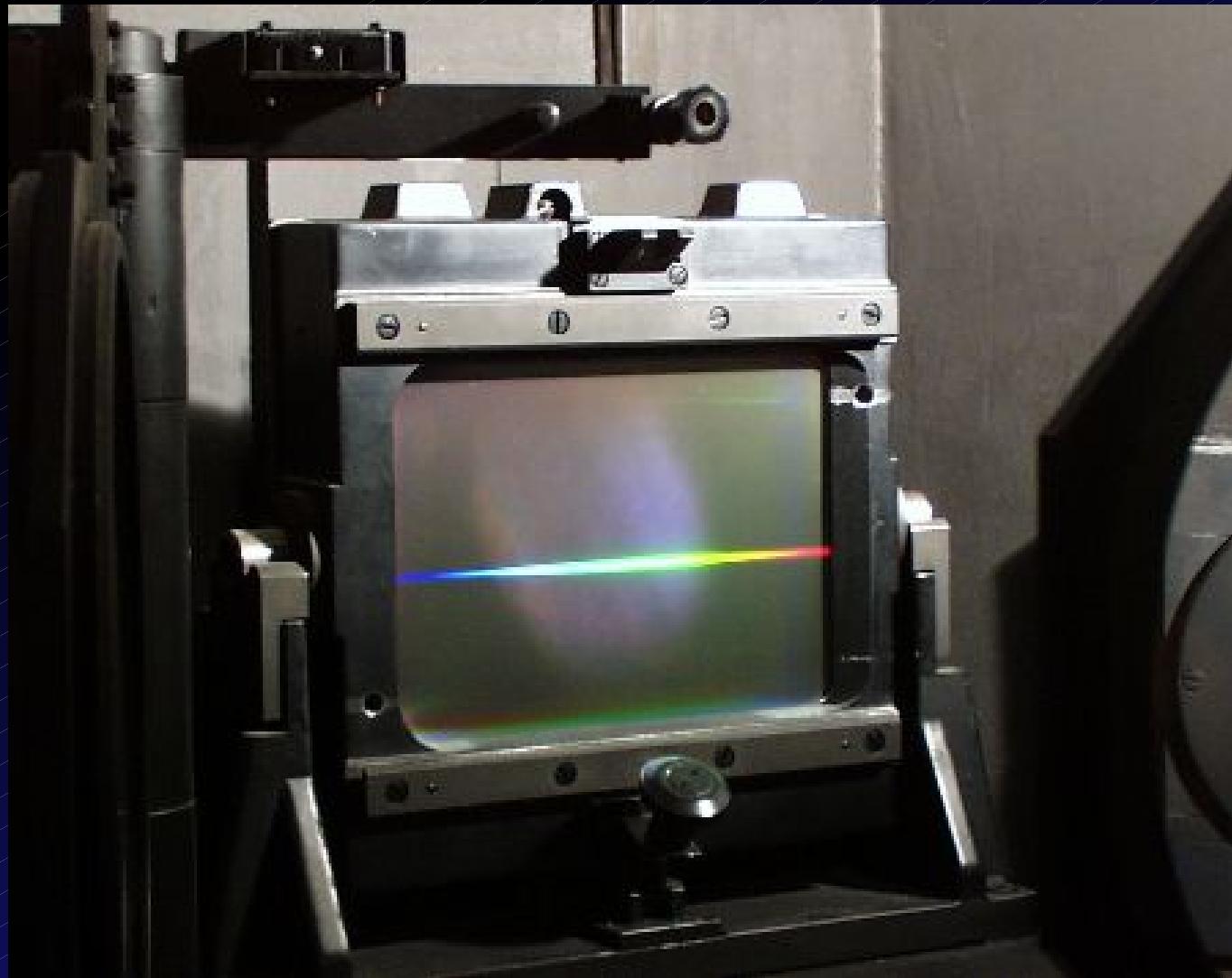


# Coudé spektroraf 2m

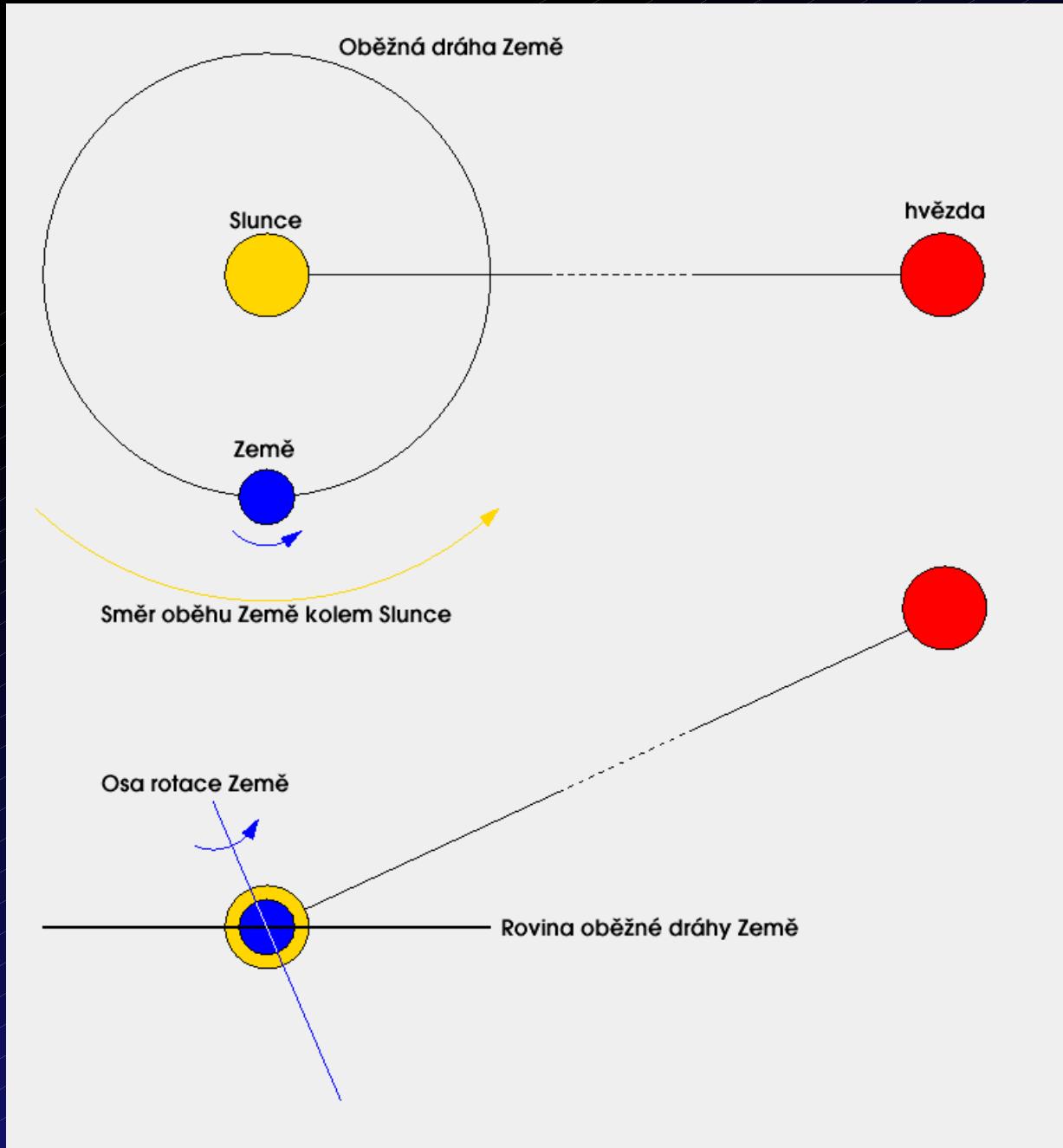




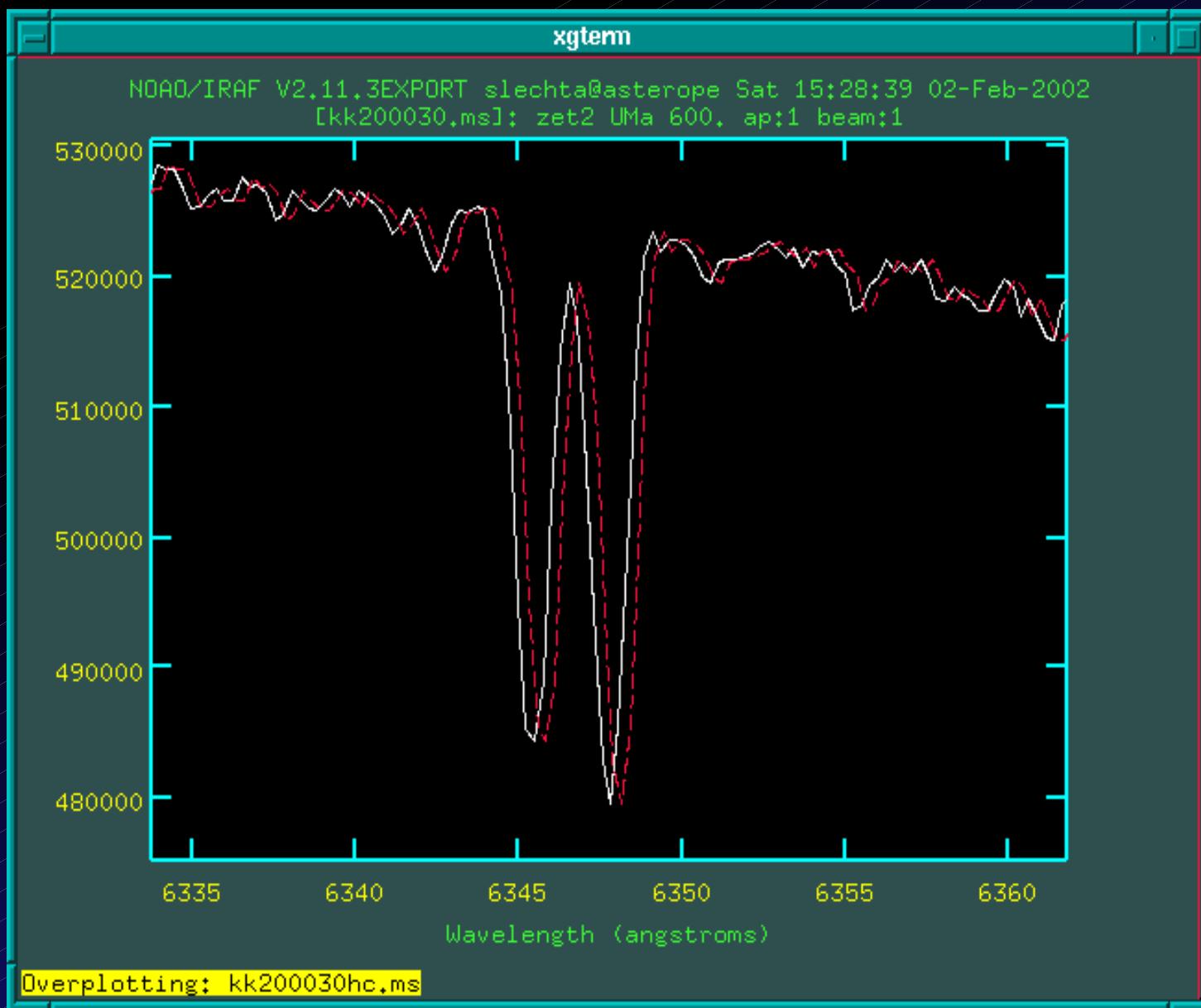
# Mřížka 833/mm



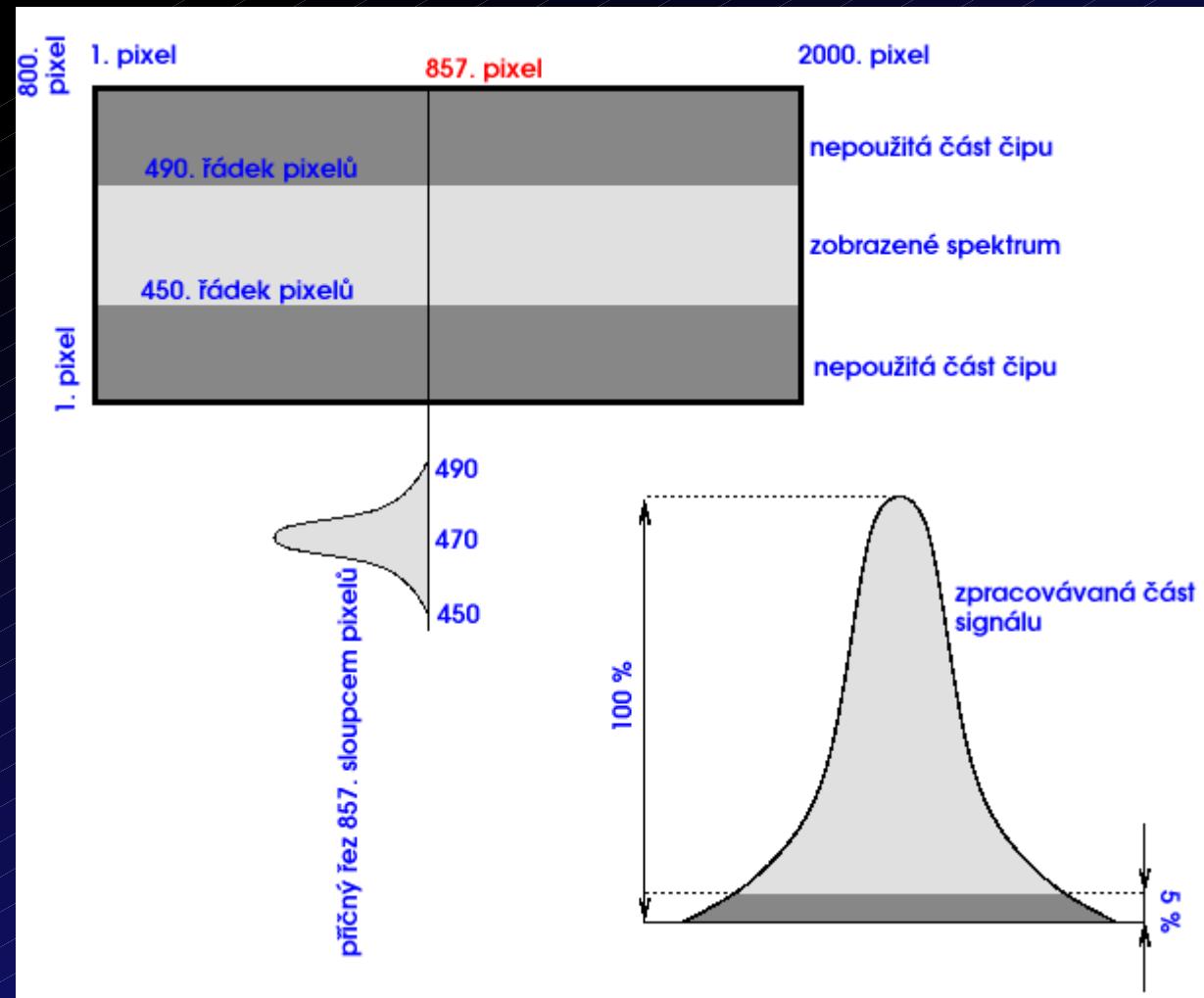
# Heliocentrická korekce



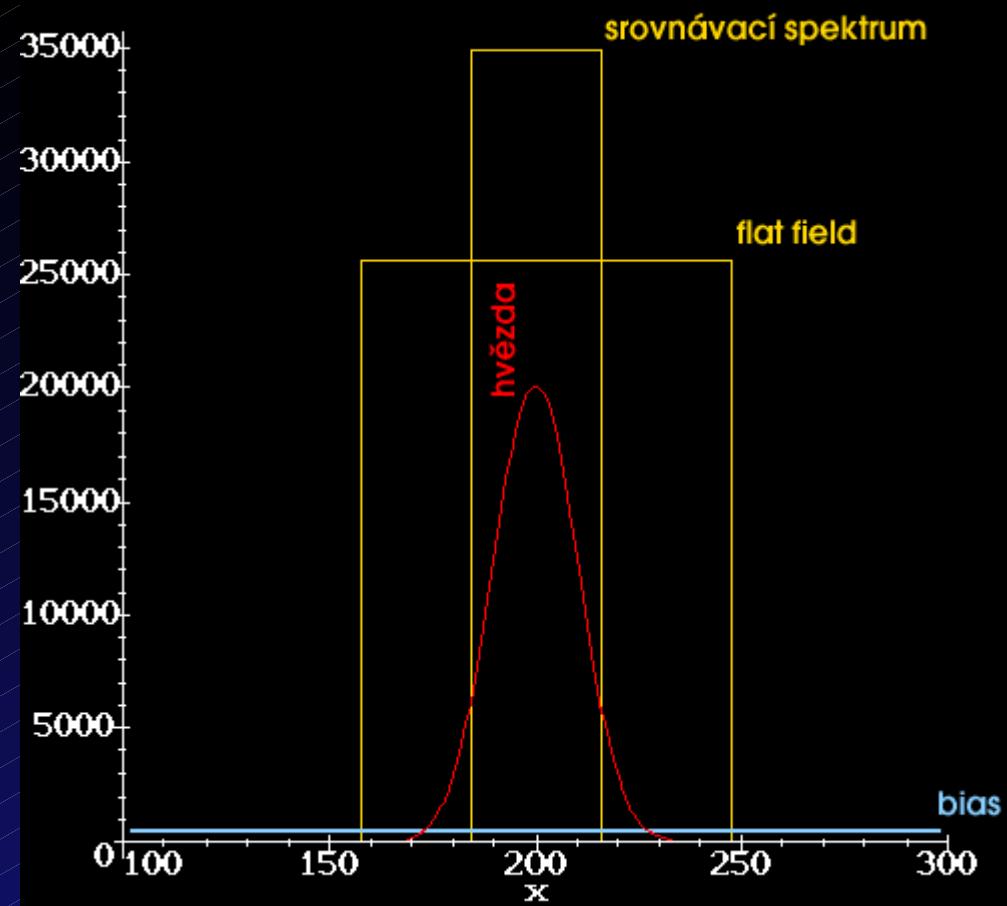
# Posun čar díky heliocentrické korekci



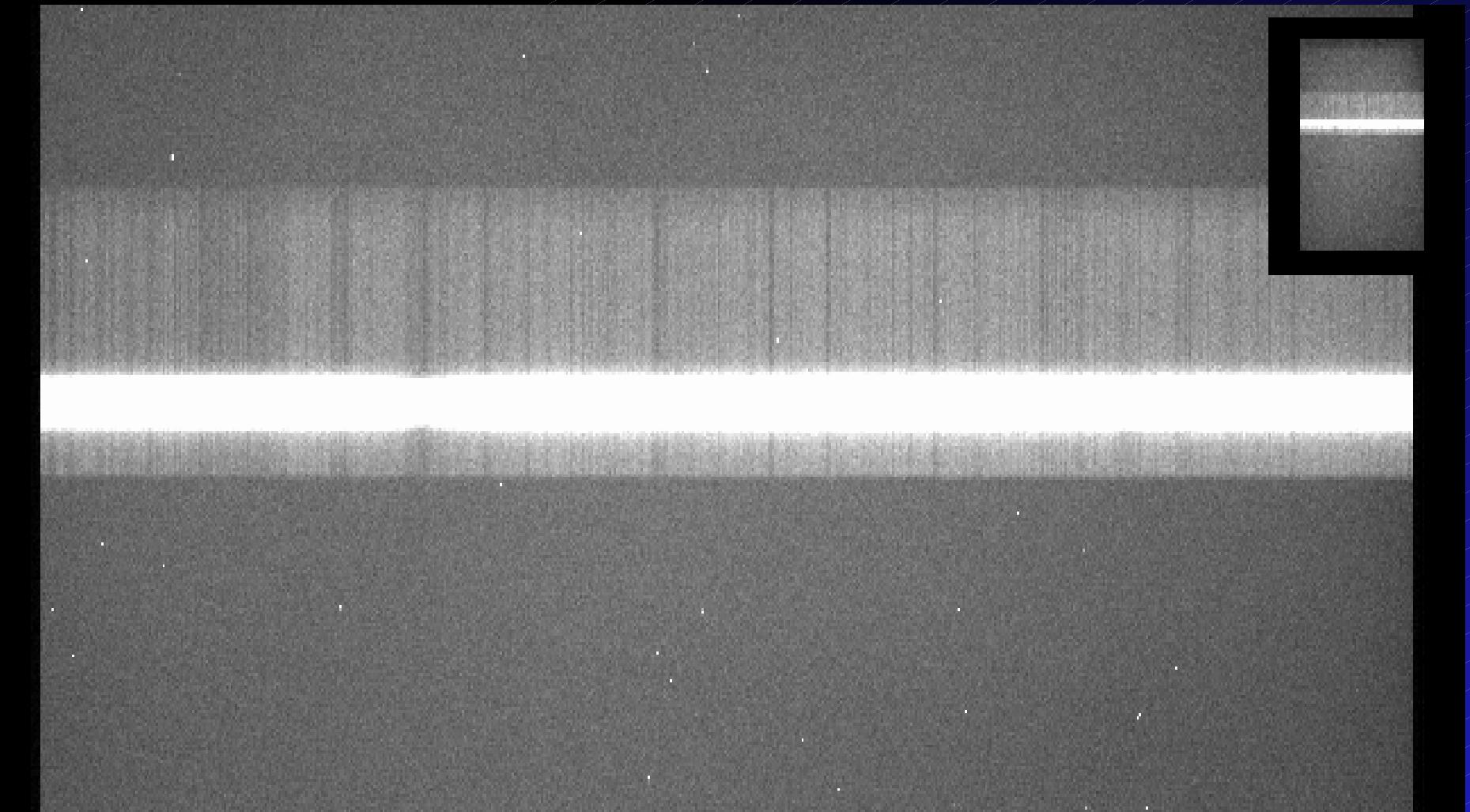
# Redukce – vyčtení COP



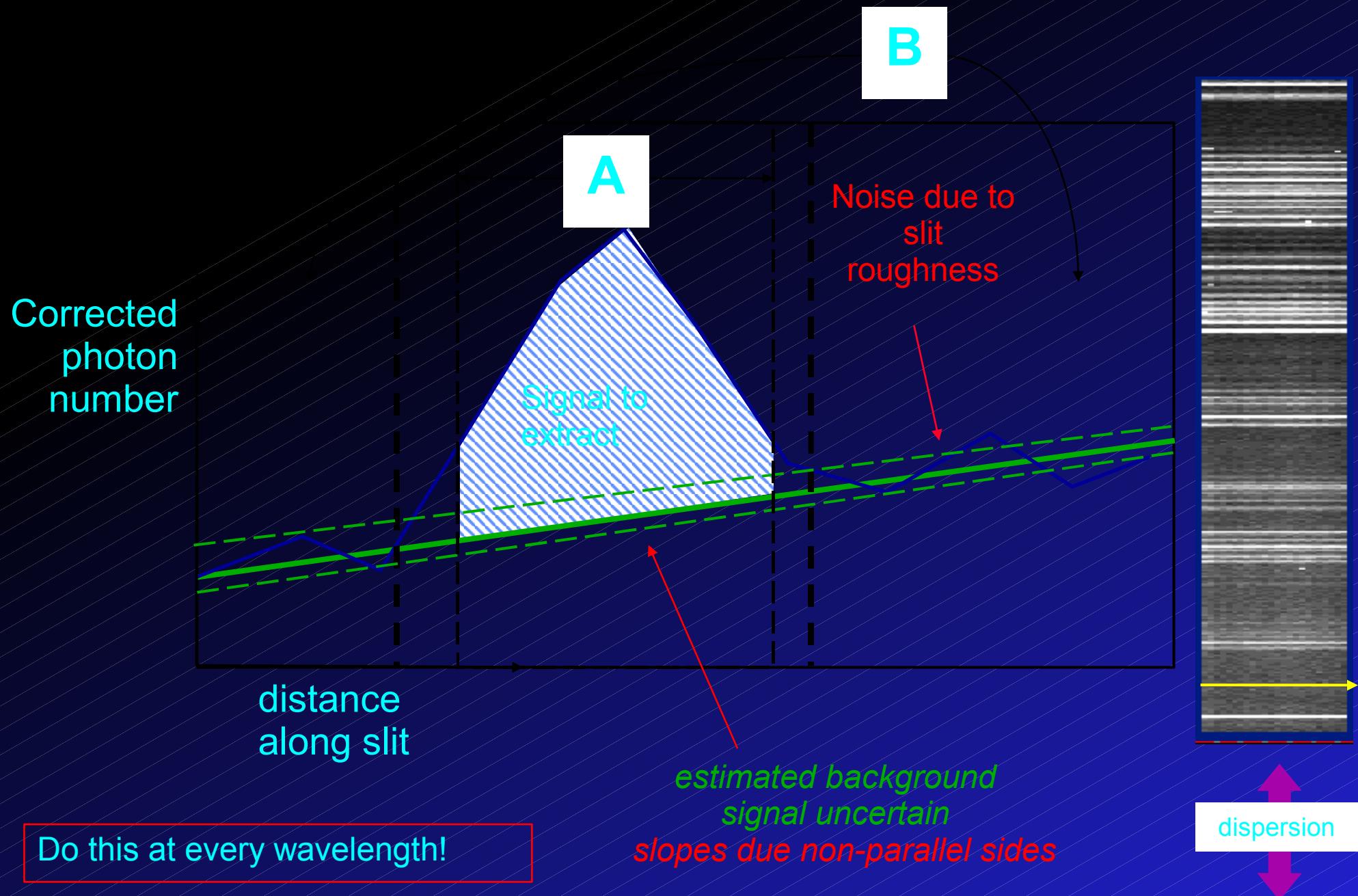
# Schéma COP



# Background a sky lines



# Sky subtraction with slit



# Sky subtraction near bright sky lines

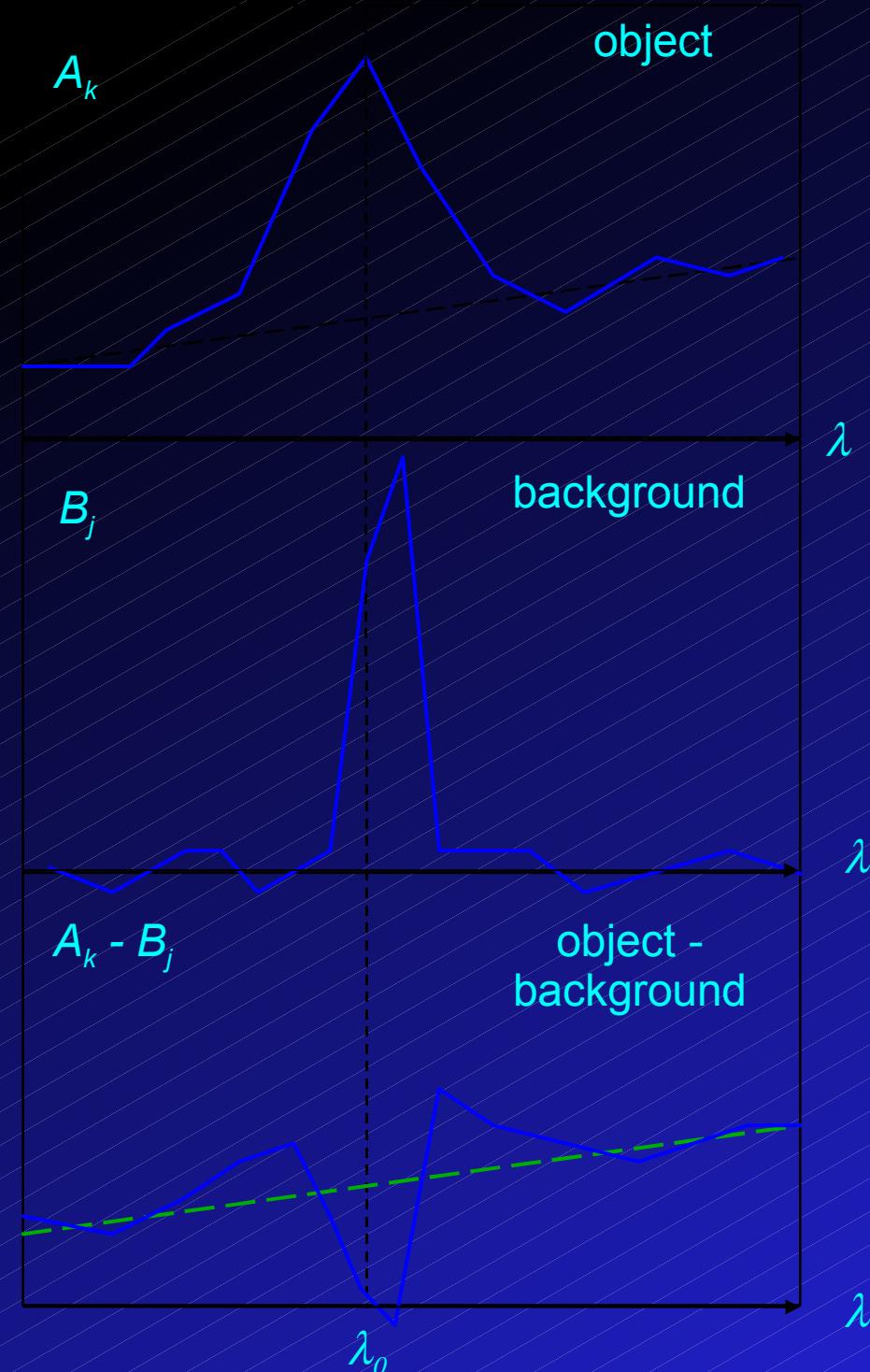
Poor cancellation of  
sky line due to:

Difference in line  
*profile* due to:

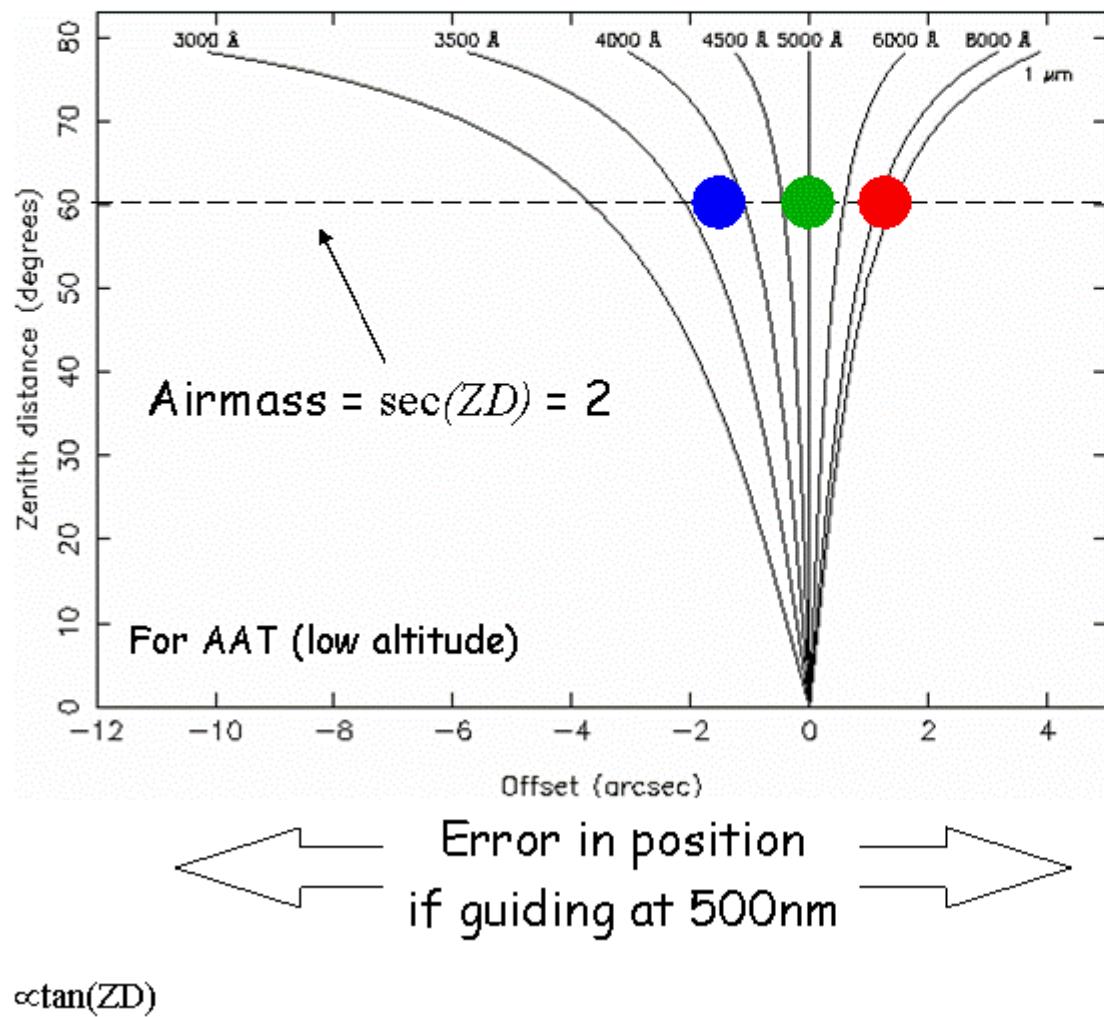
- uneven slit width
- IQ varies over field

Difference in line  
*location* due to:

- tilt of slit
- poor wavelength  
calibration/ solution/

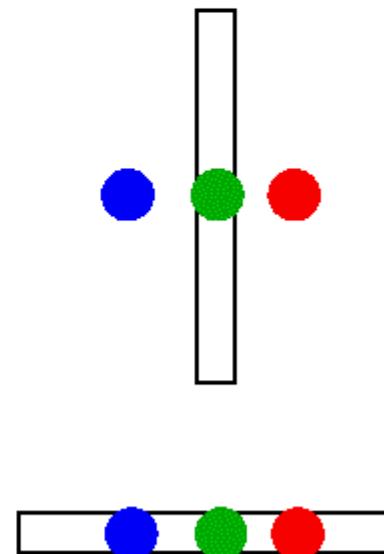


# Atmospheric dispersion (differential refraction)



To zenith

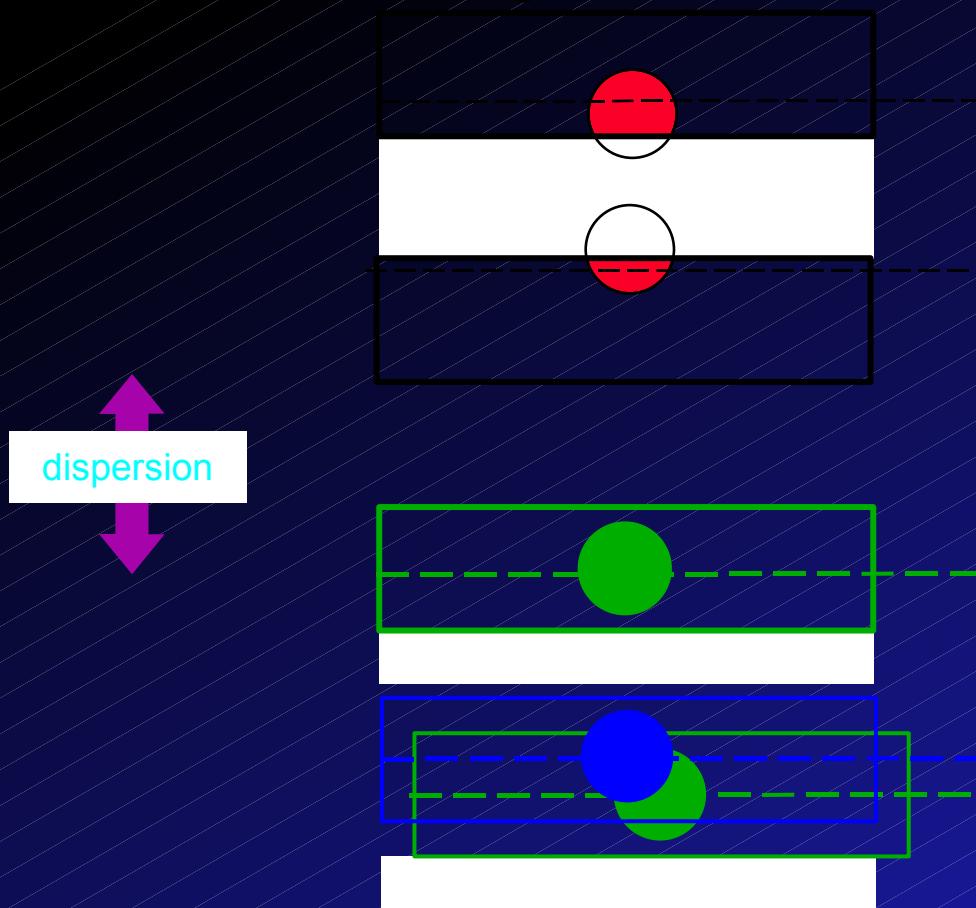
If slit is horizontal, light is lost at extreme wavelength



If slit is vertical, all light is in slit, but spectrum will be curved

# Errors in centroid of VRE

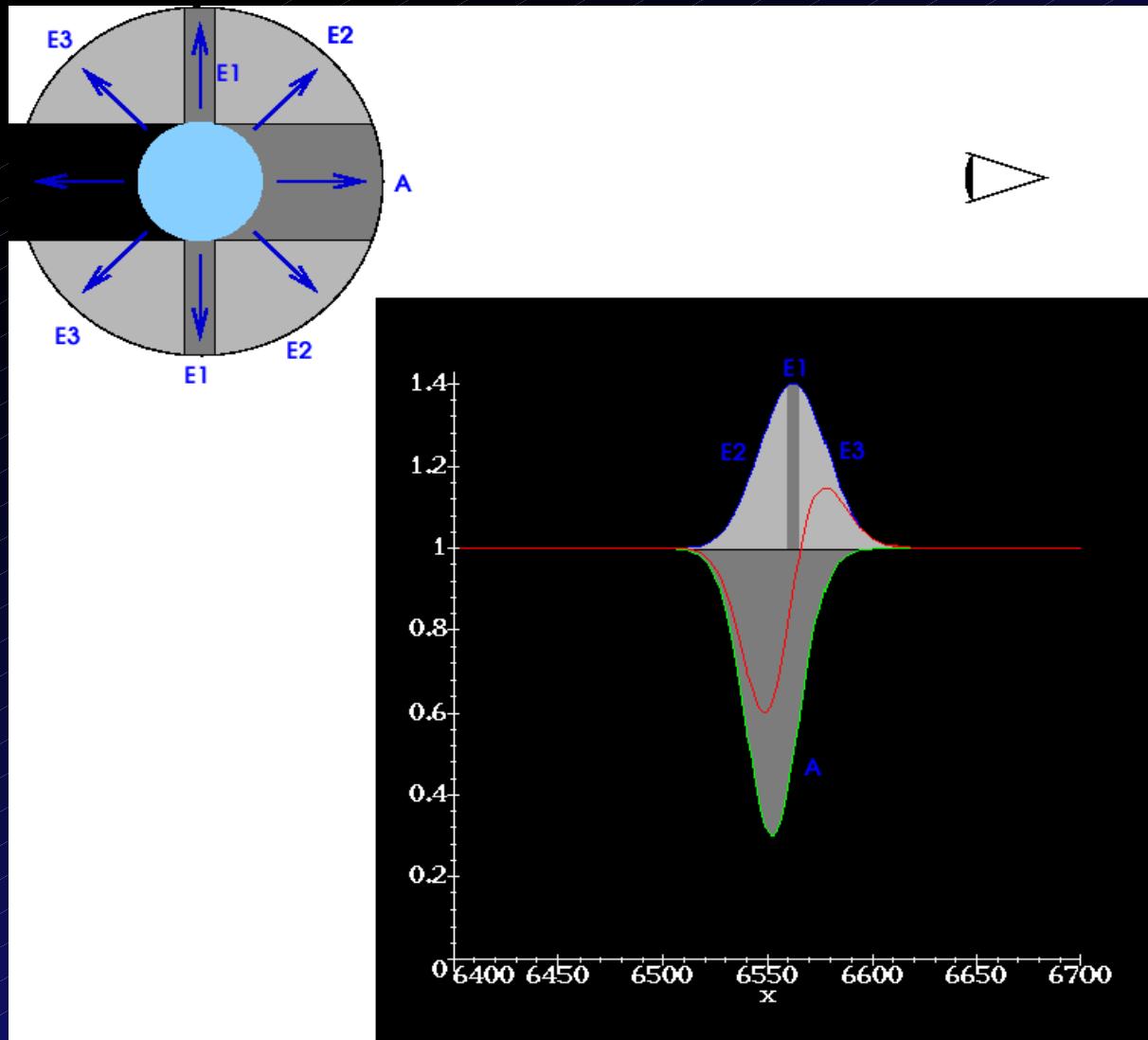
VRE = *velocity resolution element*,  
the monochromatic image of the slit as  
recorded by the detector



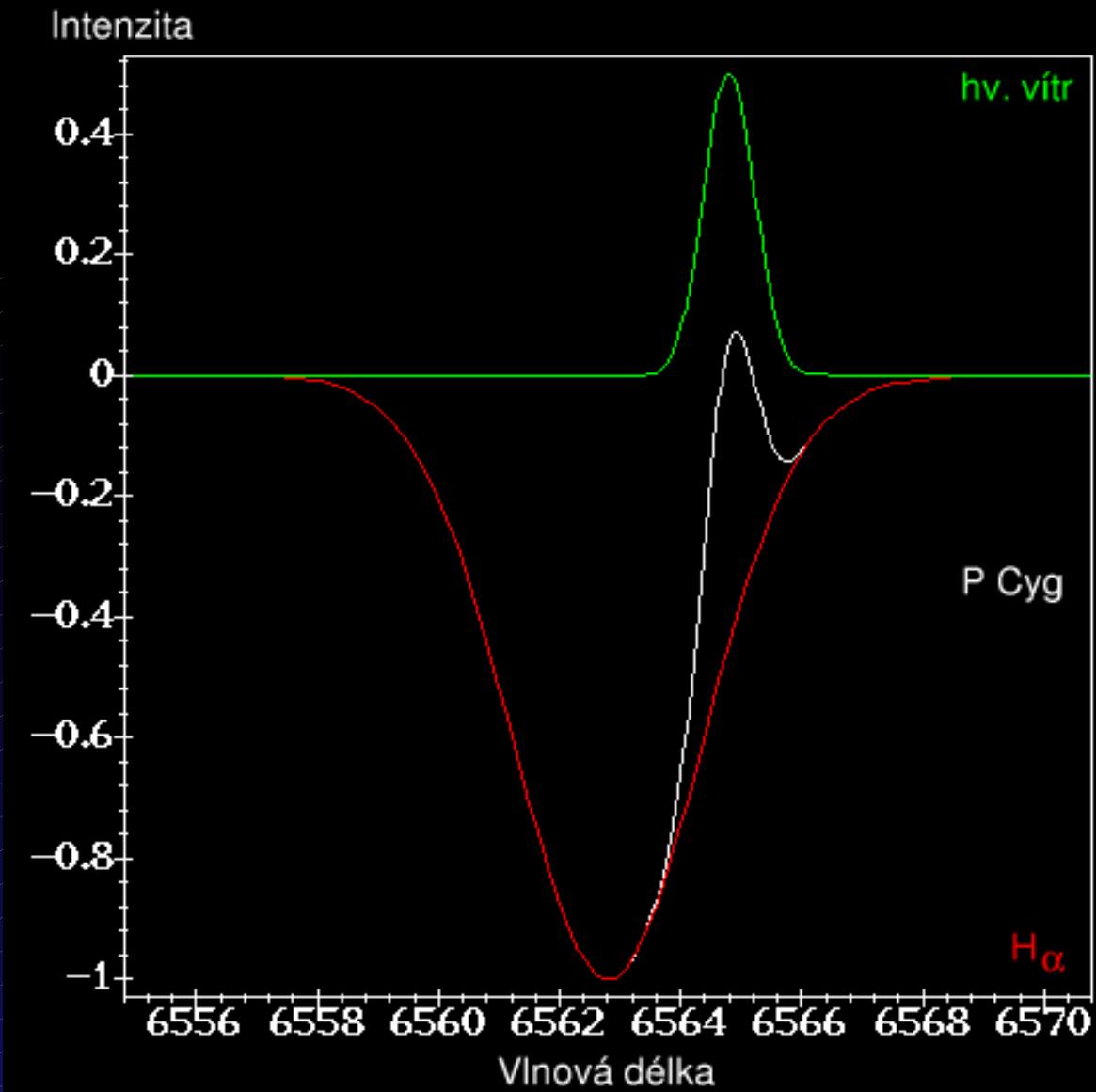
**Target-slit error:** Centroid varies depending on position of object with respect to slit due to guiding error or *movement between telescope and slit*

**Slit-detector error:** Centroid varies due to *movement between slit and detector*

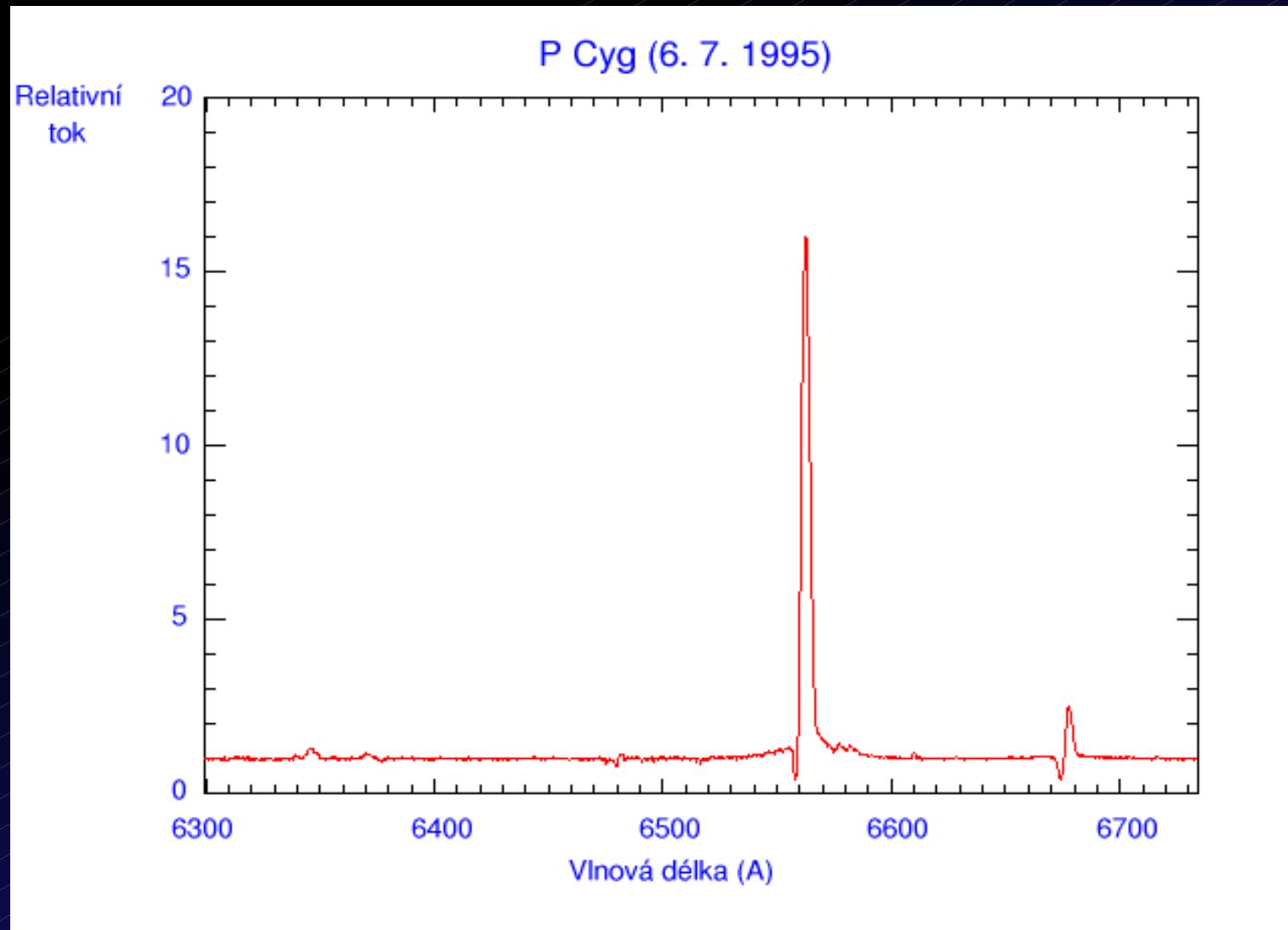
# Vznik P Cyg profilu



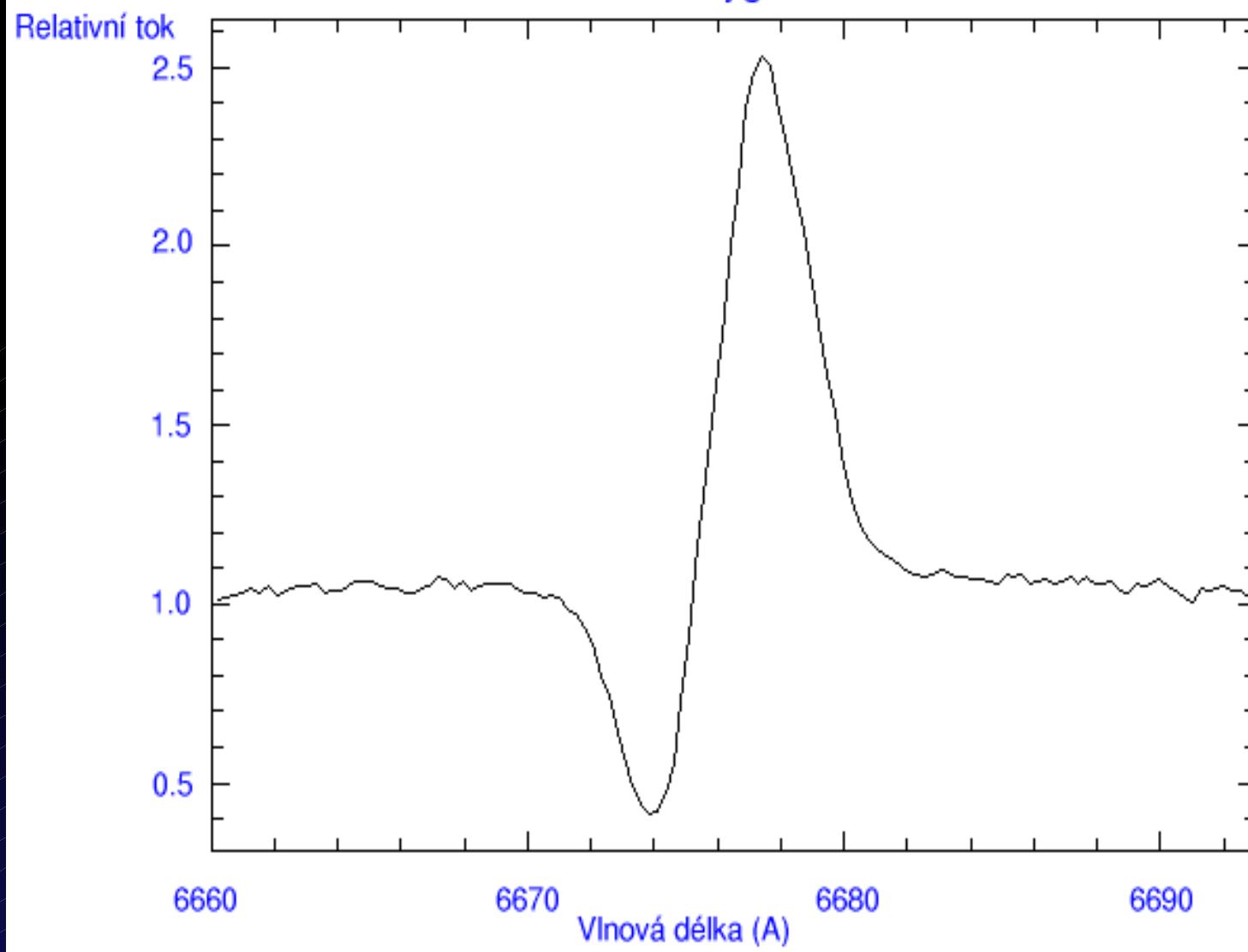
# Vznik P Cyg profilu



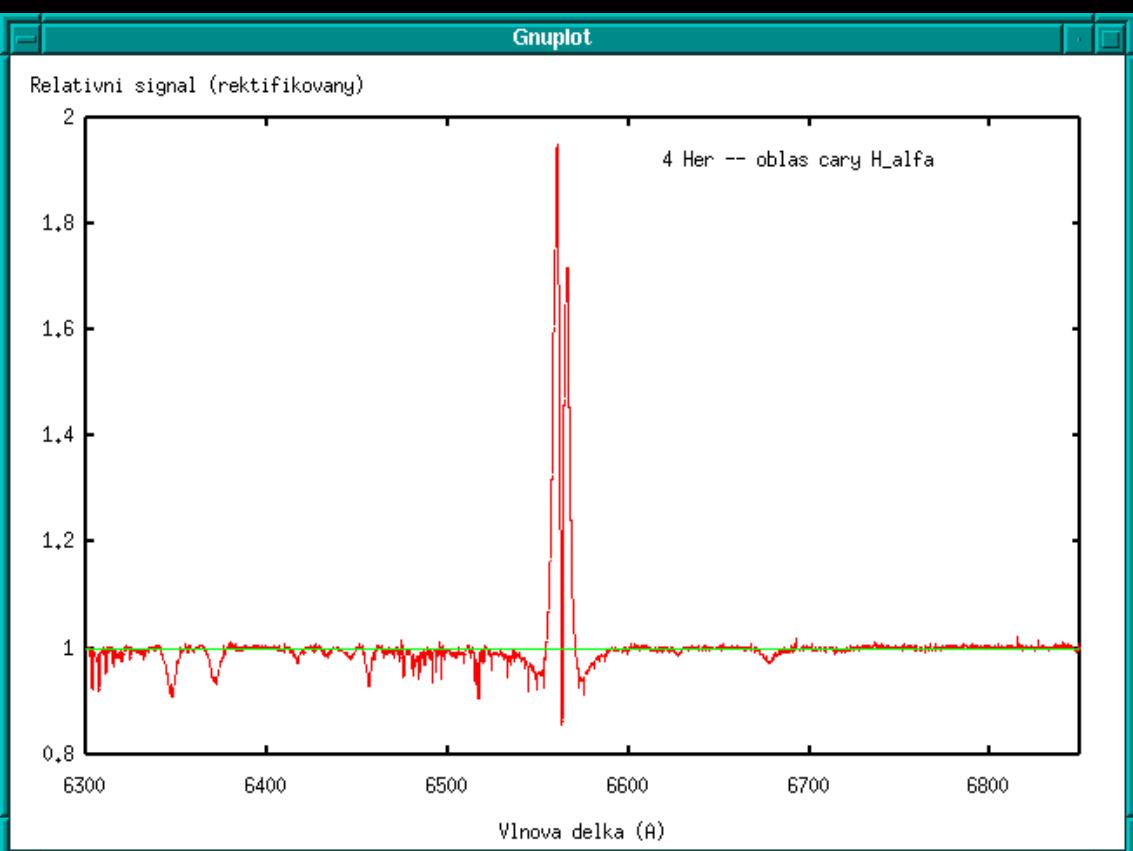
# P Cyg



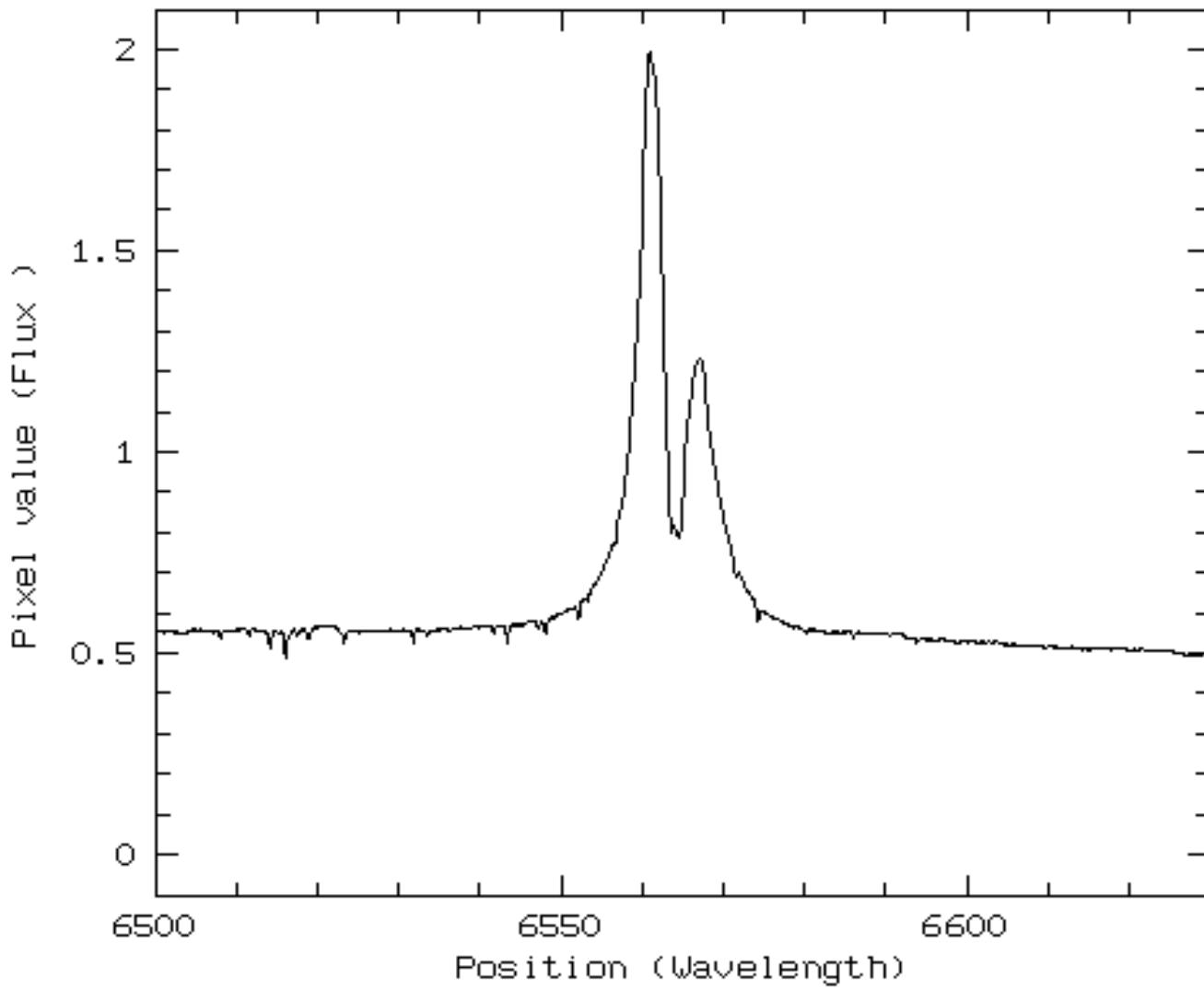
P Cyg



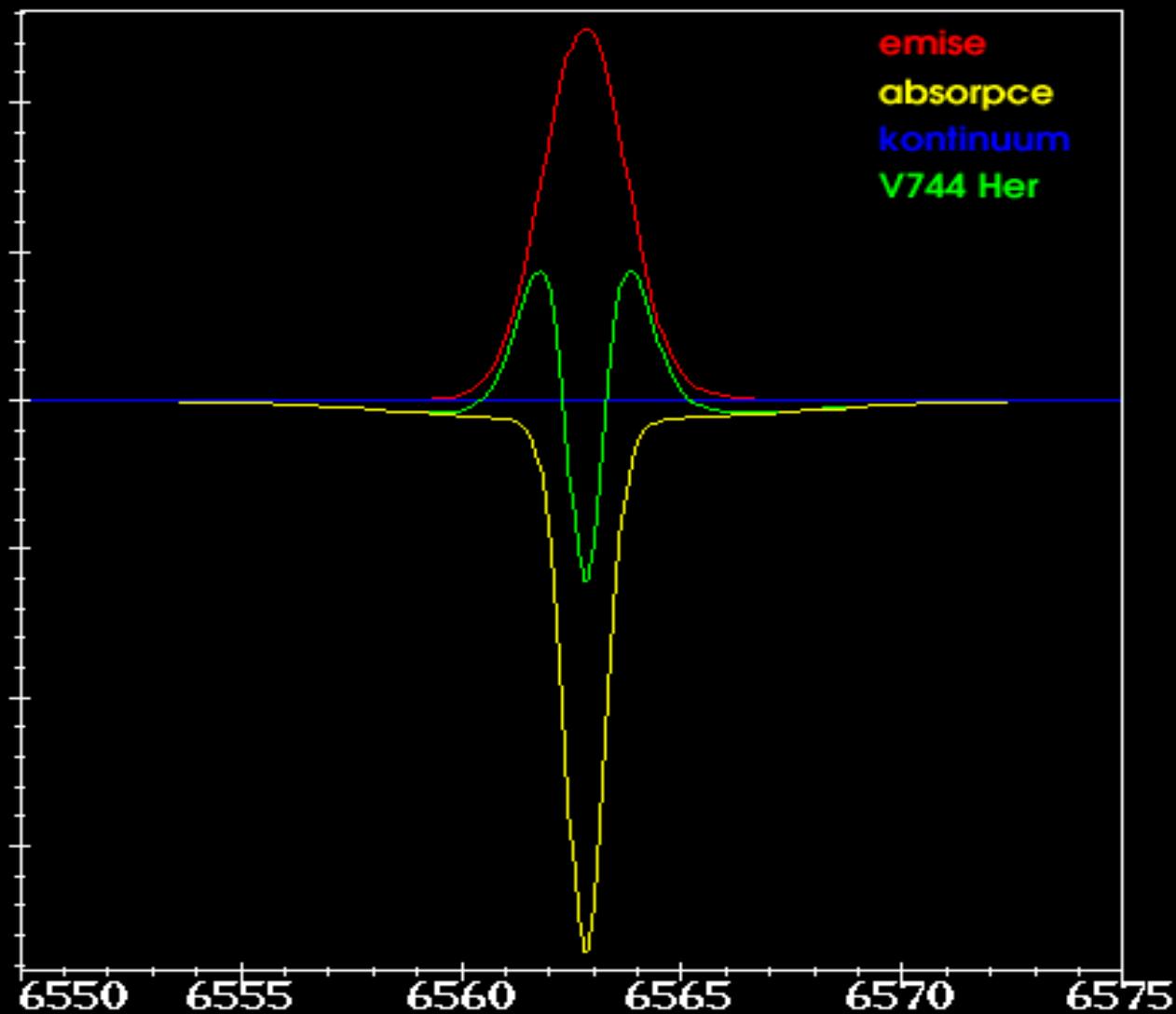
# 4 Her



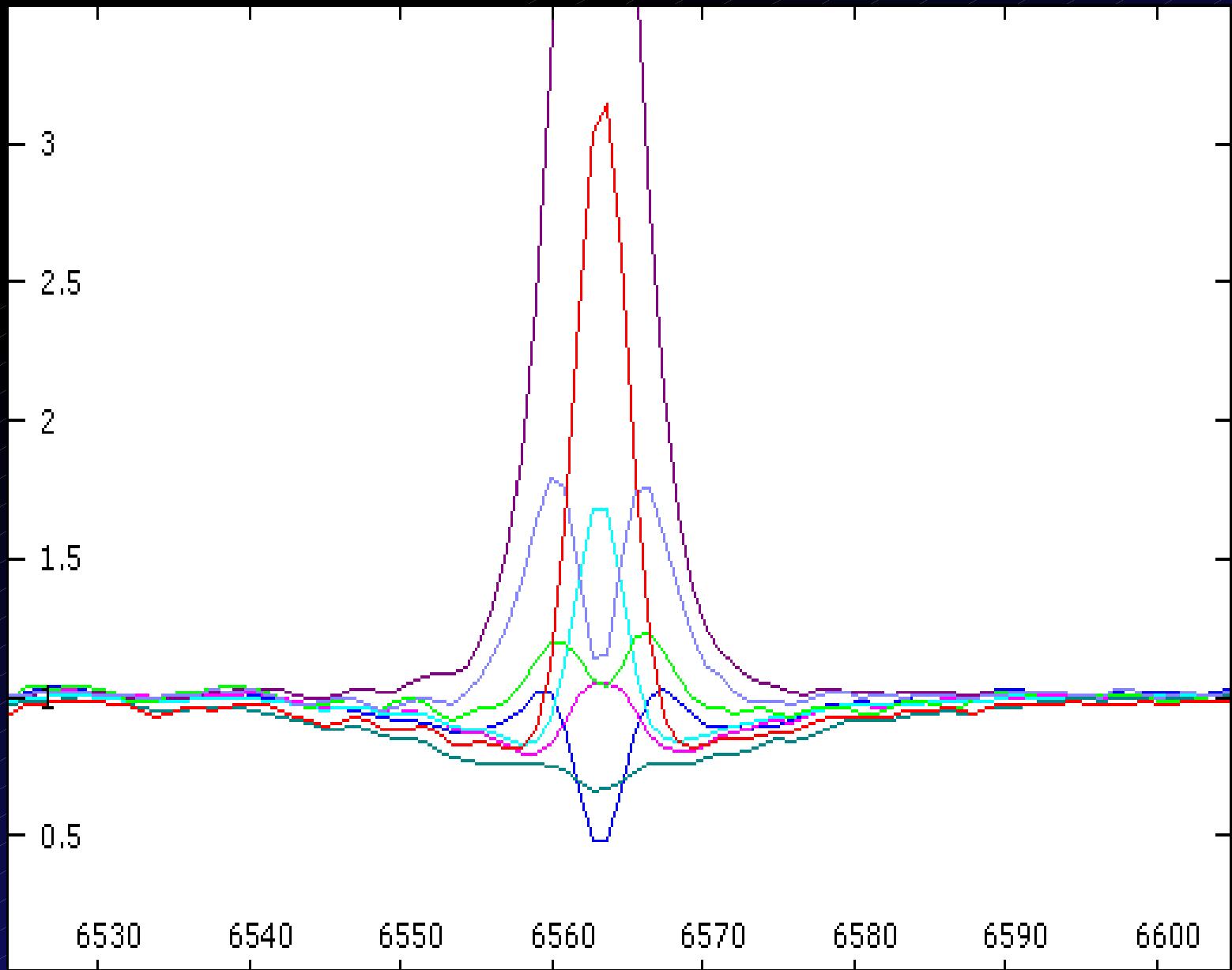
# Zet Tau



# Shell čára u Be hvězd



# Be profile (BuII)



# V 838 Mon

4. 3. 2002



28. 2. 2002



14. 2. 2002



6300

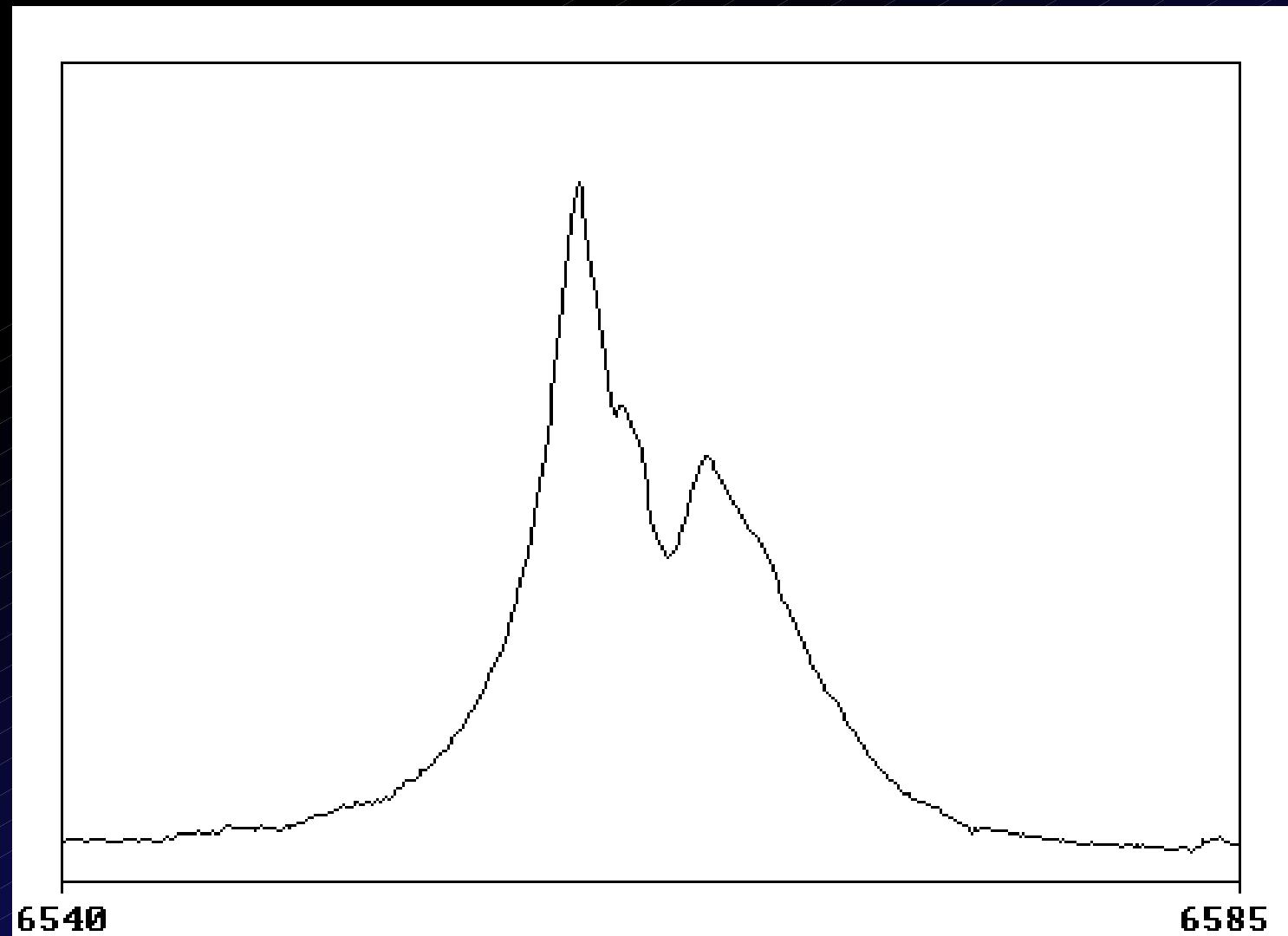
6400

6500

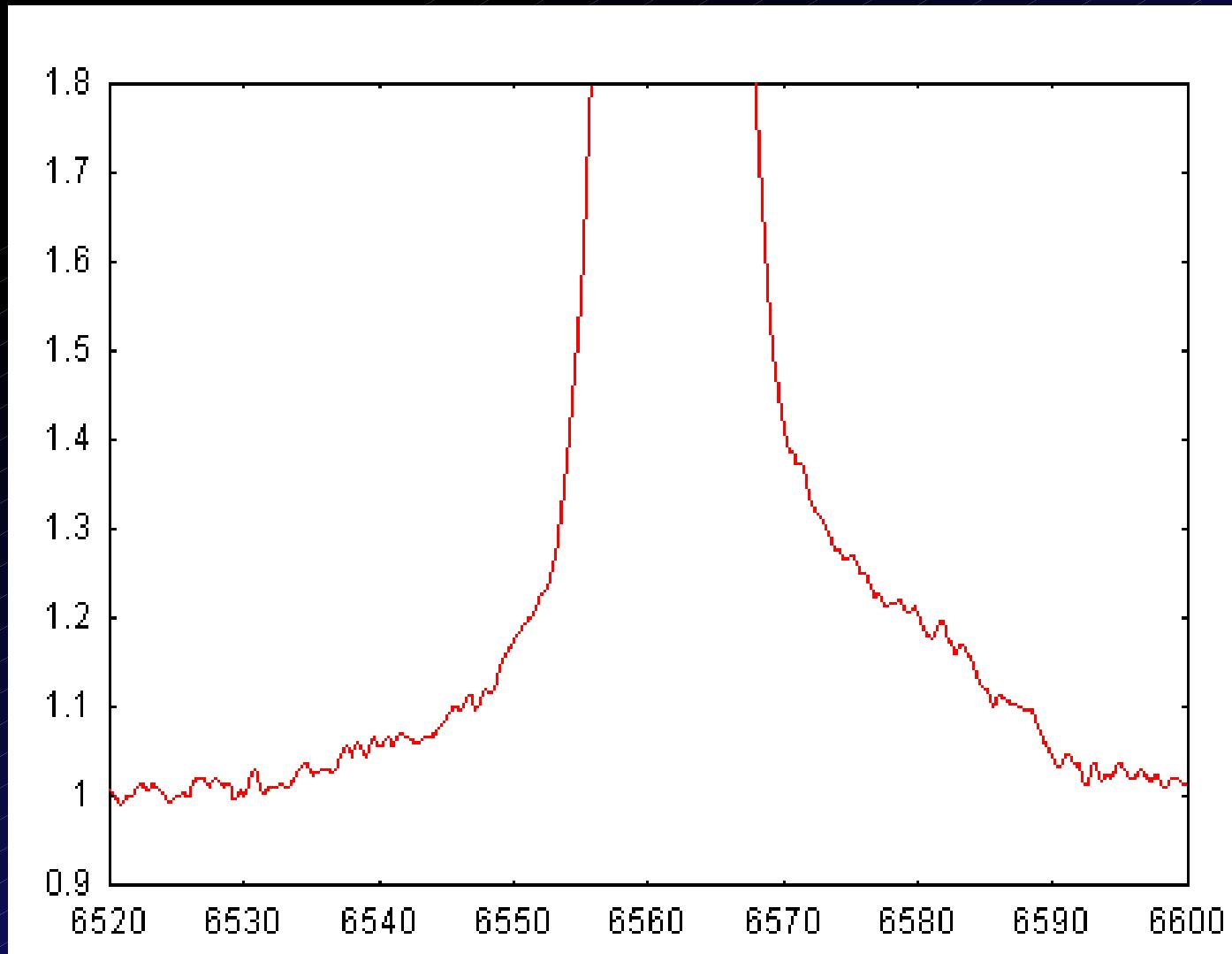
6600

6700

# Zet Tau (Buill)

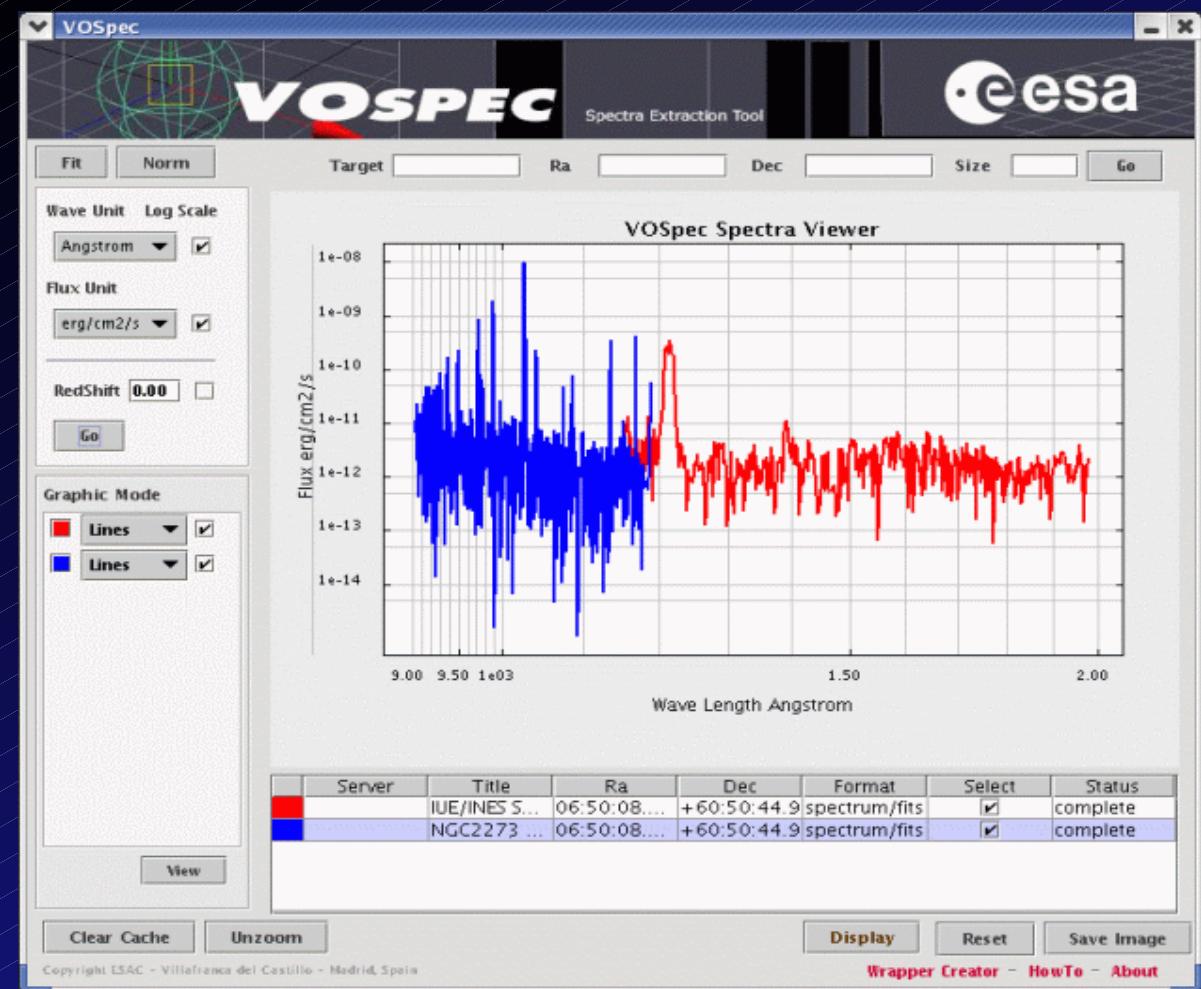


# HD 206773 (BuiII)

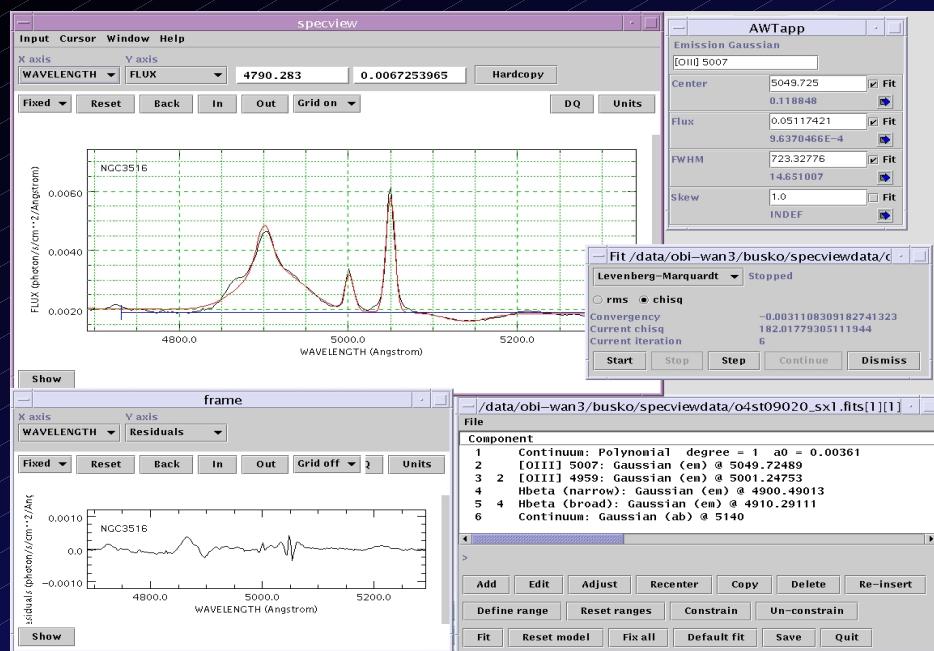
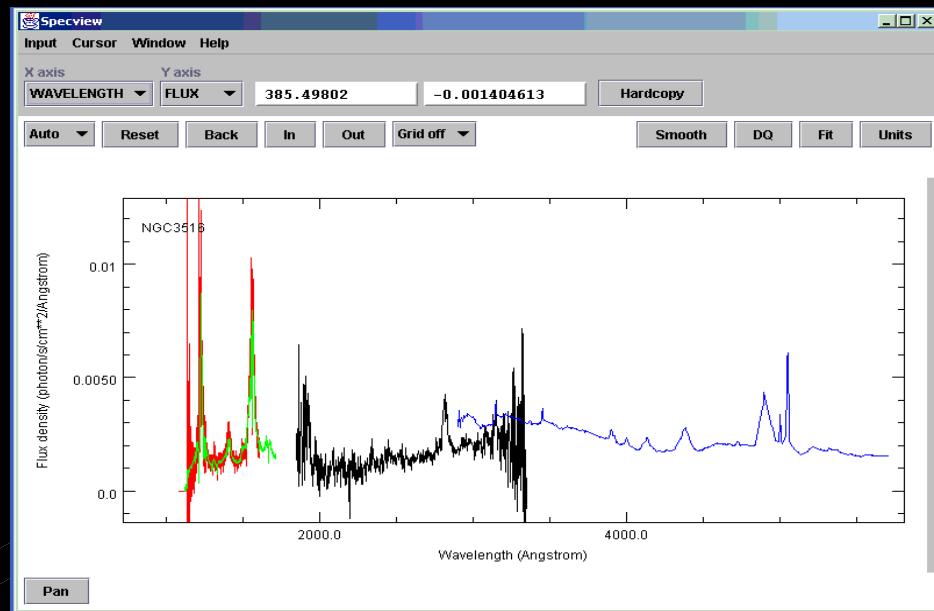


# VOSpec (ESAC)

- Very simple
- Polynomial fits
- No RV measurement
- No complex operations
- In VizieR now
- Can work with SLAP!
- Theoretical VO supported
- Rapid development :-)

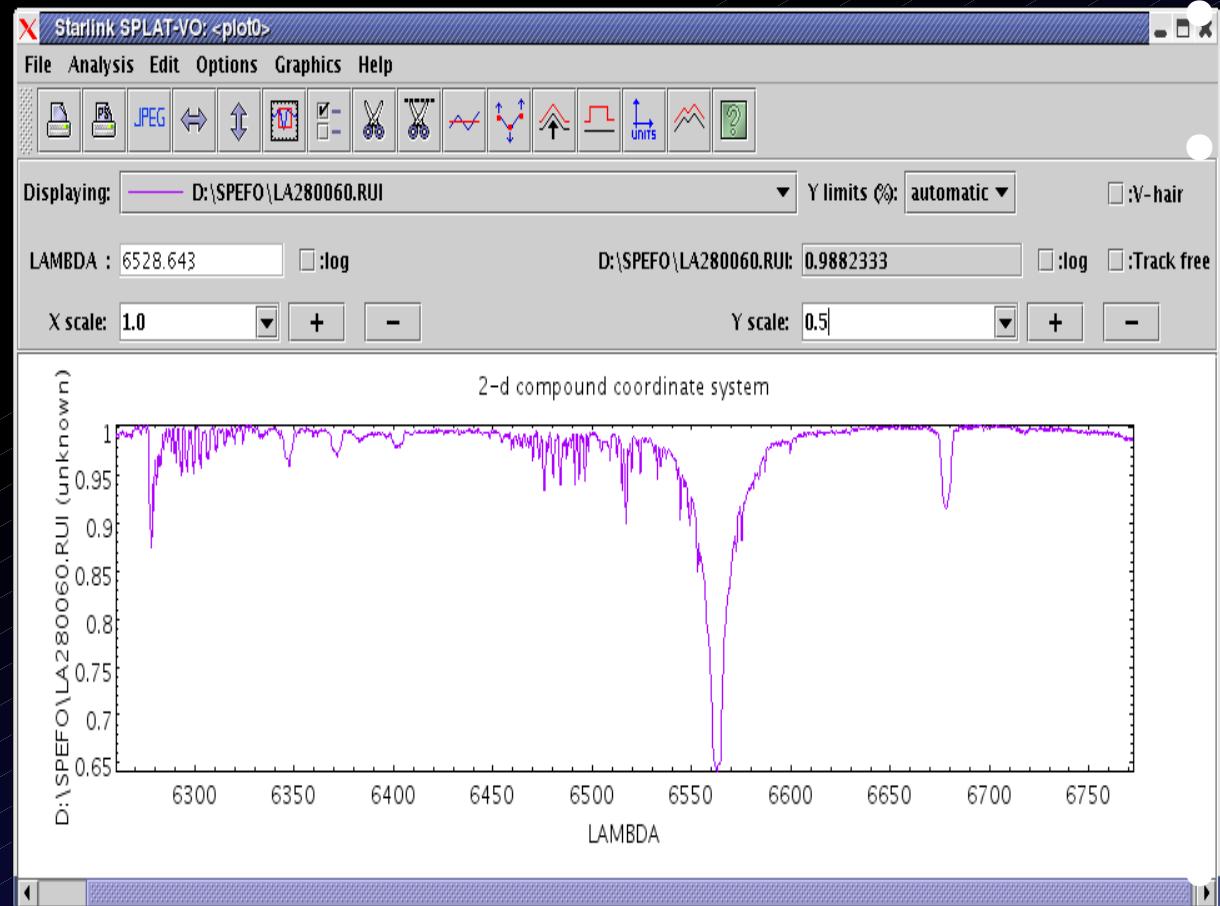


# SpecView (STScI)



- Fitting profiles from models
- Simple polynomials
- Analysis strong (deredening, CLOUDY)
- Supported !!
- Not good for IRAF WCS (1D FITS)
- BinTables+Extension

# SPLAT-VO



- Custom line list
- Development not justified ?
- Most advanced for stellar astronomy
- JCMT now
- Plastic
- Reads 1D FITS...